

# COHERENT PION PRODUCTION AS VIRTUAL PION SCATTERING

V.F. DMITRIEV

*Budker institute of Nuclear Physics, Lavrentieva 11, Novosibirsk,  
630090, Russia*

*E-mail: dmitriev@inp.nsk.su*

M.A. KAGARLIS

*Gesellschaft für Schwerionenforschung (GSI), Darmstadt,  
64220 Germany*

*E-mail: kagarlis@gsi.de*

We explore coherent pion production in ( ${}^3\text{He}$ ,  ${}^3\text{H}\pi^+$ ) reaction as effective virtual pion scattering, in calculations of cross sections to the ground state and low-lying excitations of the target nucleus. Our coupled channel model developed in <sup>1</sup> includes a source term emulating a virtual pion beam and an optical potential for the interaction of the pion in the medium. We demonstrate that the lowering of the peak in the energy-transfer spectra is entirely determined by the re-scattering of the pion. The calculations are compared with the data on coherent pion production from  ${}^{12}\text{C}$  and  ${}^{40}\text{Ca}$  targets, where the target nuclei were left either in the ground state or in the first excited state.

## 1 Outlines of the Model

In our approach, the wave function of the outgoing created pion satisfies the inhomogeneous coupled channels Klein-Gordon equation.

$$\left( \frac{1}{r^2} \frac{d}{dr} r^2 \frac{d}{dr} - \frac{l_\beta(l_\beta + 1)}{r^2} - U_{l_\beta l_\beta J}^{l_\beta l_\beta}(r) + k_\beta^2 \right) \times R_{l_\beta l_\beta J}^{l' l' J'}(r) - \sum_{\alpha} U_{l_\beta l_\beta J}^{l_\alpha l_\alpha}(r) \times R_{l_\alpha l_\alpha J}^{l' l' J'}(r) = \rho_{l_\beta l_\beta J}^{l' l' J'}(r), \quad (1)$$

where  $R_{l_\alpha l_\alpha J}^{l' l' J'}(r)$  is the radial wave function of the outgoing pion in exit channel  $\alpha$  with the set of quantum numbers  $l_\alpha l_\alpha J$ . Here  $l$  is the spin of a final nuclear state,  $l$  is the angular momentum of the outgoing pion, and  $J$  is the total angular momentum in the channel  $\alpha$ . The set of primed quantum numbers  $l', l', J'$  refers to the virtual object transferred from  ${}^3\text{He}$  to the target nucleus as a result of a charge exchange reaction.  $U_{l_\beta l_\beta J}^{l_\beta l_\beta}(r)$  is the diagonal optical potential responsible for elastic pion nucleus scattering.  $U_{l_\beta l_\beta J}^{l_\alpha l_\alpha}(r)$  is the off diagonal potential responsible for the excitation of intermediate states of the target nucleus during pion re-scattering. It is constructed from the

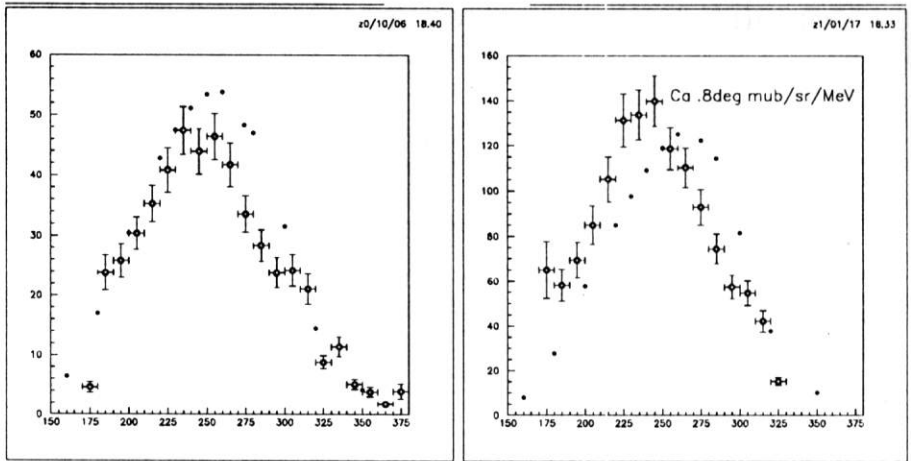


Figure 1: The cross sections of coherent pion production in  $\mu\text{b}/\text{Sr}/\text{MeV}$  from  $^{12}\text{C}$  (left picture) and from  $^{40}\text{Ca}$  (right picture) as a function of transferred energy  $\omega$  in  $\text{MeV}$ . Black dots represent the calculated cross section.

pion nucleon elastic scattering amplitude obtained from the phase-shifts and weighted with the one-body transition densities obtained from the shell model calculations for  $^{12}\text{C}$  and  $^{40}\text{Ca}$ .

The source term in r.h.s. of Eq (1) is constructed using the amplitude  $T_{NN \rightarrow NN\pi}$  of pion production in  $NN$ -collisions, and the distorted waves of  $^3\text{He}$  and  $^3\text{H}$ . The calculations were performed for finite triton angle. For the moment, we use the simplest model of pion production via  $\Delta_{33}$ -resonance.

## 2 Comparison with data

In Fig.1, we compared the results of the calculations of coherent pions spectra with the data. The calculations reproduce the magnitude of the cross section rather well for both targets. However, the shape of the calculated spectra is slightly different, especially for  $^{40}\text{Ca}$ .

## References

1. M.A. Kagarlis, V.F. Dmitriev, *Phys. Lett. B* **408**, 12 (1997).
2. Nadya Smirnova, private communication.
3. P. Oltmans, F. Osterfeld and T. Udagawa *Phys. Lett. B* **299**, 194 (1993).
4. M.Roy-Stephan, et al., Proc. of the Int. Workshop XXVIII on Gross Properties of Nuclei and Nuclear Excitations, Hirschegg 2000, p. 55.