Magnetic field effect and dielectric anomalies at the spin reorientation phase transition of $GdFe_3(BO_3)_4$

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GdFe₃(BO₃)₄ exhibits a structural phase transition at 156 K, antiferromagnetic order of the Fe³⁺ moments at 36 K, followed by a spin reorientation phase transition at 9 K. The reorientation phase transition is studied through dielectric, magnetic, and heat capacity measurements under the application of external magnetic fields of up to 7 kOe. The dielectric constant indicates the existence of two distinct anomalies at T_{SR} =9 K that separate in temperature under external magnetic fields. The spin rotation phase transition is proven to be of the first-order nature through the magnetic analog of the Clausius-Clapeyron equation. Magnetodielectric effect of up to 1% is observed at 8 K and 7 kOe. The uniaxial magnetocaloric effect along the *c* axis is observed below the spin reorientation phase transition of 9 K.

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 $GdFe_3(BO_3)_4$ belongs to the trigonal system with space group R32. It is similar to huntite $CaMg_3(CO_3)_4$, a trigonal trapezohedral structure that is one of the five trigonal types. Borate crystals of this category are appealing because of their possible applications as single crystal minilasers due to their good luminescent and nonlinear optical properties. In particular for $GdFe_3(BO_3)_4$ single crystals, recent studies have focused on the better understanding of its optical properties, and at the same time on its magnetic properties through phase matching of absorption and second harmonic generation spectra.^{1,2} The magnetic properties of the rareearth iron borates are also of fundamental interest because of the existence and mutual interference of two magnetic subsystems (Fe and Gd). The understanding of the magnetic orders of the gadolinium and iron sublattices, and the coupling between the iron spins and the gadolinium moments that contributes to the crystal's rich magnetic properties is of fundamental importance.

The crystal structure of huntite has been analyzed and described elsewhere,^{3–5} it consists of GdO₆ bipyramids and FeO₆ octahedrons. The octahedrons form threefold helicoidal chains along the *c* axis. The bipyramids are located between three nearly equal distant octahedrons. Rare-earth iron borates, $RFe_3(BO_3)_4$ (R=Eu to Ho, and Y), undergo a structural transition at higher temperatures and an antiferromagnetic (AFM) transition involving the Fe spins at $T_N \approx 35$ K.⁶ For R=Gd a weakly first-order structural phase transition at $T_1=156$ K changes the structural symmetry from R32 to $P3_12_1$.⁵ A second-order phase transition at $T_N=36$ K results in the AFM ordering of the Fe³⁺ magnetic moments aligned in the basal plane. At $T_{SR}=9$ K, another sharp phase transition of the Fe³⁺ magnetic moments by 90° from the basal plane to the *c* axis.

The coupling between the Gd moments and the Fe spins

at low temperatures is strong in $GdFe_3(BO_3)_4$ and it was speculated that the reorientation of the AFM iron spin system is triggered by the anisotropy of the Gd moments aligned with the c axis.⁶ This exchange interaction is indirect and involves other ions such as oxygen in the structure. Below T_N , with decreasing temperature, the magnetic order grows, and that causes strain via the spin-lattice interaction. At the spin reorientation phase transition the magnetic order experiences a sudden change that is reflected in distinct anomalies of the dielectric constant, ϵ , as recently discussed in several rare-earth manganites.^{7,8} The dielectric constant can be measured with extraordinary precision and it monitors subtle changes of the magnetic system. We have therefore searched for dielectric anomalies at the magnetic phase transitions in $GdFe_3(BO_3)_4$ and its correlation with magnetic and heat capacity data. Below T_N , close to T_{SR} , we found two distinct anomalies of ϵ that separate in temperature with applied magnetic fields. A sharp drop of ϵ occurs at the reorientation of the Fe spins, whereas a maximum of $\epsilon(T)$ above T_{SR} indicates the onset of magnetic-field-induced ferroelectric order. The spin reorientation phase transition is proven to be of the first-order nature through the magnetic Clausius-Clapeyron equation. Lastly, a phase diagram is proposed for magnetic fields parallel or perpendicular to the crystalline c axis.

The single crystal GdFe₃(BO₃)₄ was grown as described elsewhere.⁹ The transparent crystal (shining green in color) was analyzed and oriented using a GADDS x-ray diffractometer. The heat capacity data was acquired via Quantum Design's physical property measurement system (PPMS) under the application of magnetic fields of up to 6 kOe both along the *a* and *c* axes (we use the hexagonal coordinate system in which $a \perp c$). Direct current magnetization data was measured employing Quantum Design's magnetic prop-



FIG. 1. (Color online) Dielectric data showing all three major anomalies. $T_1=156$ K, $T_N=36$ K, and $T_{SR}=9$ K. The inset shows the behavior of $\epsilon(T)$ around T_N when ϵ is measured along the hexagonal *a* and *c* axis for H=0.

erty measurement system (MPMS) in magnetic fields parallel to *a* and *c*. Smaller portions of the crystal were cut from an original crystal in order to align the two desired crystallographic orientations for dielectric investigations. Silver paint was used as electrodes for the dielectric measurements and the sample was mounted onto a homemade capacitance probe that was adapted to the PPMS. The capacitance was measured by the high precision capacitance bridge AH2500A (Andeen Hagerling) operating at a frequency of 1 kHz. The temperature and magnetic fields were controlled by the PPMS when the dielectric constant was measured.

The three known phase transitions are reflected in different anomalies of the dielectric constant (Fig. 1). At T_1 =156 K, the dielectric constant drops significantly since the transition is a structural one. T_1 does not depend on magnetic field. The magnetic transition into the AFM2 phase at T_N is distinguished by a change in slope of ϵ_c and a minimum of ϵ_a at 36 K. Below T_N , ϵ_a starts increasing with decreasing T and develops the peaklike feature at T_{SR} , the transition into the AFM1 phase, as shown in Fig. 1. This is a clear signature of lattice softening and it has to be correlated with the changes in the magnetic order at and below T_N . A similar, but positive slope change at T_N is observed in ϵ_c . This behavior is analogous to the magnetic data that will be discussed later. In a system where there are two magnetic subsystems present with one of them being a *d*-metal and the other one an f-metal subsystem, the f metal is magnetically polarized upon the ordering of the *d*-metal subsystem.¹⁰ In $GdFe_3(BO_3)_4$ the gadolinium develops an AFM order along the c axis through interplanar exchange interactions mediated by the Gd-O-Fe bonds below T_N . The dielectric anomalies observed at the magnetic phase transitions are an indication of strong spin-lattice interactions and are attributed to magnetoelastic effects similar to those observed in some rareearth manganites;¹¹ a strong coupling of the dielectric response with the rare-earth magnetic moment was also reported in these compounds.^{7,8} The softness of the lattice [as expressed by the sharp increase of $\epsilon_a(T)$ is therefore an indication of the softening of the magnetic order as T ap-



FIG. 2. (Color online) Splitting of the spin reorientation phase transition under fields parallel to the *c* axis. T_{SR} shifts lower while T_M stays the same.

proaches T_{SR} , resulting in the Fe-spin reorientation triggered by the Gd moments and the abrupt decrease of ϵ_a . Thermal hysteresis was observed in $\epsilon(T)$ above T_{SR} at zero magnetic field. The hysteretic behavior of $\epsilon_a(T)$ extends over several degrees just above T_{SR} . Upon cooling in zero field the dielectric constant below T_N increases continuously for $T \rightarrow T_{SR}$ and drops rapidly right below T_{SR} . However, upon heating, after the sharp increase at T_{SR} there appears a distinct maximum of ϵ_a at T_M about 0.7 K higher in temperature (Fig. 2). This second anomaly at T_M needs to be explored in more detail.

The external magnetic field, *H*, shows an interesting effect on both dielectric anomalies $(T_{SR} \text{ and } T_M)$. If H is aligned with the c axis, the spin reorientation transition is suppressed and T_{SR} quickly decreases with H_c in accordance with recent magnetic data.⁹ However, T_M is barely affected by H_c , and the separation of both anomalies increases in magnetic fields as shown in Fig. 2. In contrast, for magnetic fields parallel to a, T_{SR} remains constant but T_M shifts to higher temperature (Fig. 3). At the same time, the enhancement of $\epsilon_a(T)$ is largely reduced and disappears for fields exceeding 7 kOe. This qualitative behavior of the dielectric constant in magnetic fields is closely correlated with the magnetic properties of the coupled system of the Fe spins and the Gd moments. It is interesting to note that recent measurements of the magnetic field induced electric polarization, P, of $GdFe_3(BO_3)_4$ have shown a sudden increase of P in crossing T_{SR} with increasing field.¹² This may indicate the existence of a fieldinduced ferroelectric phase (FIP) and it was proposed that higher-order magnetoelectric couplings are responsible for the observed phenomena. From our dielectric measurements we can uniquely identify the boundaries of this new phase by the sudden drop of $\epsilon_a(T)$ at T_{SR} and the distinct maximum of $\epsilon_a(T)$ at the high temperature end (T_M) . Therefore the phase diagram of GdFe₃(BO₃)₄ includes three distinct phases (AFM2, AFM1, and FIP) below the AFM ordering temperature, T_N , of the iron system.

The results of magnetization measurements with fields oriented parallel to a and c are summarized in Fig. 4. Sur-



FIG. 3. (Color online) Splitting of the spin reorientation phase transition under fields parallel to the *a* axis. T_{SR} remains constant while T_M shifts higher.

prisingly, the *a*- and *c*-axes dc susceptibilities are equal above T_N within the experimental resolution, i.e., GdFe₃(BO₃)₄ is magnetically isotropic at high temperatures although there is evidence for easy plane anisotropy of the Fe spins and easy axis anisotropy of the Gd spins.⁶ The anisotropies of both magnetic ions are obviously correlated resulting in a complete isotropic balancing just like some rare-earth metal ferrite-garnets and orthoferrites.¹³ The high temperature Curie-Weiss extrapolation yields a Curie-Weiss temperature of Θ_{CW} =-34 K, and an effective magnetic moment μ_{eff} =12.2 μ_B in good agreement with other reports¹⁴ and the theoretically expected value of μ_{eff} =12.96 μ_B (Gd³⁺, S=7/2 and Fe³⁺, S=5/2). Deviations from the Curie-Weiss behavior due to short-range AFM correlations are detected below 100 K.



FIG. 4. (Color online) Mass susceptibility data at different magnetic fields parallel and perpendicular to the *c* axis. T_{SR} shifts lower and ΔM increases under magnetic fields parallel to the *c* axis (open). T_{SR} stays the same if magnetic fields are aligned with the *a* axis (solid). χ_a is only affected between $T_{SR} < T < T_N$.

Below T_N the magnetic response becomes anisotropic and depends on the direction of the probing field. For $H \parallel c$, the dc susceptibility, $\chi_c(T)$, does not exhibit any anomaly at T_N and it is independent of the magnetic field (up to 10 kOe) between T_N and T_{SR} . χ_c decreases suddenly at T_{SR} as a result of the spin reorientation aligning the Fe spins with the c axis (Fig. 4). The major effect of H_c is the shift of T_{SR} to lower T and eventually the suppression of the spin reorientation for fields above 8 kOe. It is obvious that the magnetic response strongly depends on the angle between the external field and the Fe spins. This is justifiable since it is energetically unfavorable to keep the Fe spins aligned with the external magnetic field. This qualitative behavior is reflected in the field dependence of the dielectric constant (Fig. 2). $\epsilon_a(T)$ increases below T_N and exhibits a distinct maximum at $T_M \approx 10$ K. The sharp drop of $\epsilon_a(T)$ at lower temperature coincides with $T_{SR}(H)$ as determined magnetically. $\epsilon_a(T)$ is only weakly dependent on the field H_c between T_N and T_M as is the magnetic susceptibility, χ_c . Whereas the value of T_M is not affected by the field oriented along the c axis $T_{SR}(H)$ decreases rapidly reaching zero at about 8 kOe and separating the two dielectric anomalies in the magnetic field. The peak of $\epsilon_a(T)$ indicating the phase boundary between the AFM2 phase and the FIP phase exists well above 8 kOe, the critical field that suppresses the AFM1 phase. Details of the phase diagram will be discussed later.

The magnetic response to an in-plane magnetic field, H_a , is completely different. At low magnetic fields, the susceptibility χ_a levels off below T_N and is clearly lower than χ_c (Fig. 4). This can be attributed to the AFM order of the Fe spins below T_N , reducing the susceptibility for $H \parallel a$. Close to T_{SR} , however, χ_a increases again and its temperature dependence below T_{SR} appears to be a continuation of the *c*-axis susceptibility, χ_c (discussed above). This behavior agrees well with the observation that the magnetic susceptibility is little affected by the AFM order if the field is perpendicular to the Fe spins. At T_{SR} the Fe spins rotate towards the c axis and align themselves with the magnetic field. $\chi_a(H)$ rapidly increases with H in the temperature range $T_{SR} < T < T_N$, and it approaches the values of χ_c above 7 kOe. T_{SR} is independent of H_a , as is also reflected in the dielectric data of Fig. 3 [the sharp drop of $\epsilon_a(T)$ marks the spin reorientation transition]. $\epsilon_a(T)$ between T_{SR} and T_N , however, is strongly affected by H_a , and its enhancement below T_N is reduced by the magnetic field. Thereby the maximum of $\epsilon_a(T)$ is shifted to higher temperatures (Fig. 3) reaching the Néel temperature at a relatively low field of 4 to 5 kOe. This limits the AFM2 phase and extends the temperature range of the FIP phase to $T_N = 36$ K.

The dielectric anomalies observed in GdFe₃(BO₃)₄ at the magnetic transitions reveal an interesting correlation between the different magnetic subsystems (Fe and Gd) and the spin-lattice coupling leading to the modifications of $\epsilon(T)$. To arrive at a deeper understanding the magnetic correlations have to be considered in more detail. The phase diagram and the magnetic order of GdFe₃(BO₃)₄ was recently investigated by AFM resonance experiments and it was suggested that the Fe spins at high temperatures are aligned in the *a-b* plane (easy plane anisotropy) whereas the Gd moment experience a

strong easy axis anisotropy orienting them along the c axis.⁶ The AFM order of the iron moments below T_N couples to the gadolinium moments resulting in an AFM alignment of the Gd spins ("magnetic polarization"). With decreasing temperature the Fe-Gd coupling grows stronger and eventually triggers the reorientation of the Fe spins resulting in a transition from the noncollinear $(T_{SR} < T < T_N)$ to a collinear $(T < T_{SR})$ magnetic order of both subsystems along the c axis. This phenomenon, related to the strong single ion anisotropy of rare-earth ions, is not uncommon and it was observed in a number of different compounds involving rareearth ions and d elements.^{15–17} Depending on the strength of the anisotropy factors, the coupling between the f moments and d spins results in the rotation of the d spins towards the f moments (such as in R_2 CuO₄, R=Pr,Nd,Sm,Eu)^{15,18} or vice versa (e.g., in orthorhombic HoMnO₃).¹⁶ In rare cases the f-d exchange can result in an in-plane rotation of the dspins as observed in hexagonal HoMnO₃.¹⁹ Dielectric anomalies associated with spin reorientation transitions have been observed in several manganites,^{7,20} and the significance of the spin-lattice coupling and magnetoelastic effects has been shown.¹¹ The coupling between the f and d spins forming a 90° angle can be mediated by the antisymmetric Dzyaloshinskii-Moriya interaction (which is proportional to the vector product of f and d moments and gives rise to weak ferromagnetism), or by a pseudodipolar interaction arising from the anisotropy of the f-d exchange.¹⁴ In any case, the exchange interaction maximizes if the two moments are perpendicular to each other.

The Fe spin reorientation observed in $GdFe_3(BO_3)_4$ at T_{SR} is triggered by this f-d exchange mechanism. We propose that the observed enhancement of the dielectric constant below T_N (Figs. 1 to 3) is closely related to the indirect f-d exchange coupling and the magnetic polarization of the Gd moments. The increase of $\epsilon_a(T)$ as T approaches T_{SR} at H=0 reflects the increased coupling strength and AFM Gd sublattice polarization. The spin-phonon coupling causes the lattice to soften as the magnetic order becomes unstable for $T \rightarrow T_{SR}$. The combined effects on ϵ_a saturate at $T_{SR}(H=0)$ and it disappears abruptly with the spin reorientation of the iron at lower T resulting in the sudden decrease of the dielectric constant. With the magnetic field applied along the c axis T_{SR} is lowered but the polarizing effect on the Gd moments and the enhancement of $\epsilon_a(T)$ still reaches its maximum at 9 K explaining the peak of ϵ_a remaining H independent at $T_M \approx 9$ K. With the magnetic field applied along the *a* axis, the Gd moments are tilted away from the c axis and the in-plane AFM order of the Fe spins is gradually reduced, as can be concluded from the field effect on the susceptibility, χ_a (Fig. 4). Both effects reduce the *f*-*d* exchange coupling, and the magnetic polarization of the Gd-spins and its effect on the lattice is reduced. The saturation of the lattice softness happens at higher temperature in the in-plane magnetic field, the maximum of $\epsilon_a(T)$ is suppressed, and T_M increases with H (Fig. 3). Although this discussion is qualitative it does explain the two anomalies observed in the temperature dependence of the dielectric constant and their opposite dependence on the magnetic fields parallel or perpendicular to the c-axis. The softening of the lattice at T_M eventually results in



FIG. 5. (Color online) Heat capacity data at different magnetic fields parallel to the *c* axis. T_{SR} shifts lower and ΔS decreases with H_c .

a ferroelectric displacement as observed in recent polarization measurements¹² that indicate the existence of a sizable field-induced polarization between T_{SR} and T_M for both orientations (*c* axis and in-plane) of the magnetic field. The corresponding magnetostriction data provide the experimental proof for the lattice anomalies at the phase boundaries of the FIP phase, T_{SR} and T_M .

The thermodynamic signature of the magnetic phase transitions at T_N and T_{SR} is given by sharp peaks of the zero-field heat capacity²¹ at the phase transitions. In external magnetic fields, $H \parallel c$, the heat capacity peak at T_{SR} shifts to lower T, in accordance with the magnetic and dielectric data discussed above. Figure 5 shows the heat capacity close to T_{SR} at different values of H_c . All peaks are relatively sharp and symmetrical indicative of a first-order phase transition. The heat capacity peak does not shift with $H \parallel a$, which is consistent with our dielectric and magnetic data. From the structural point of view the exchange interaction between gadolinium ions should be weak since they are interconnected by BO₃ triangles that are 2.4 Å apart. Thus T_M is not observed in the heat capacity or magnetization data but only in dielectric data.

The magnetic phase diagram of GdFe₃(BO₃)₄ at lower temperatures derived from the heat capacity, magnetization, and dielectric measurements is shown in Fig. 6 for both orientations of the magnetic field. T_{SR} is not affected by H_a , however; it decreases quadratically with H_c , in agreement with the results of recent resonance⁶ and magnetoelectric experiments.¹² The field dependence of T_M is also shown in Fig. 6. T_M merges with T_N for $H_a \approx 5$ kOe in good agreement with the anomalies detected in polarization and magnetostriction measurements. However, for $H \parallel c$, $T_M(H)$ is almost constant and extends to far higher fields than T_{SR} . T_{SR} and T_M form the phase boundaries of the FIP phase where magnetic field-induced polarization was observed.¹² It is interesting to note that the heat capacity does not show any anomaly at T_M as it does at T_{SR} . The transition across T_M is obviously not



FIG. 6. (Color online) Phase diagram of $GdFe_3(BO_3)_4$ at low temperatures including T_{SR} , T_M , and T_N derived from dielectric data. AFM1 is the state where the Fe spins are ordered antiferromagnetically along the basal plane, AFM2 is the state where the Fe spins are ordered antiferromagnetically along the *c* direction. FIP is the state where there is field-induced polarization.

accompanied by anomalies such as a sizable change of volume, etc. This indicates a more subtle change in the correlated magnetic systems of Gd and Fe spins coupled to the lattice that results in the distinct peak of the dielectric constant.

Given the sharp nature of the heat capacity peak anomaly at T_{SR} as well as its sudden drop in magnetization and dielectric constant, a first-order phase transition is presumed to occur. To further verify the validity of the first-order nature at T_{SR} we make use of the magnetic analog of the Clausius-Clapeyron equation,

$$-\Delta S(B)/\Delta M(B) = dB/dT_{SR}(B)$$

where ΔS is the change in entropy, ΔM is the change in magnetization, and dB/dT_{SR} is the inverse slope of $T_{SR}(B)$ with respect to the internal magnetic field *B*. The set of values for ΔS are obtained from integrating the area underneath the peak anomaly of Cp/T at different fields (Fig. 5). The set of values for ΔM is obtained from the change of the magne-



FIG. 7. (Color online) The Clausius-Clapeyron equation satisfied at different magnetic fields H_c .

tization at T_{SR} (Fig. 4). dB/dT_{SR} is extracted from the phase diagram of Fig. 6 and $B = \mu_0(H+M)$. For the case of $H \parallel c$, Eq. (1) is well fulfilled as shown in Fig. 7. This proves the first-order nature of the spin reorientation transition.

In conclusion, we have demonstrated a strong correlation between the magnetic order and the dielectric properties of GdFe₃(BO₃)₄. Below the AFM ordering temperature of the Fe spins, T_N , $\epsilon_a(T)$ increases and reaches a maximum at the spin reorientation transition temperature, T_{SR} , in zero magnetic field. We interpret the apparent lattice softness as a consequence of the indirect exchange coupling between the Gd and Fe spins. For nonzero magnetic fields the $\epsilon_a(T)$ maximum (at T_M) and the spin reorientation transition are separated and appear at different temperatures. The spin reorientation transition is proven to be a first-order phase transition through the magnetic analog of the Clausius-Clapeyron equation.

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