# New bismuth borophosphate $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ : Synthesis, crystal structure, optical and band structure analysis 

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## H I G H L I G H T S

- New bismuth borophosphate with composition $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ was synthesized.
- The crystal structure was determined by X-ray powder diffraction technique.
- Bismuth-oxygen part $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}$ forms endless strips of 4 bismuth atoms width.
- Electronic structure was modeled by DFT method.
- The calculated band gap ( 3.56 eV ) is very close to the experimental one ( 3.46 eV ).


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#### Abstract

New bismuth borophosphate $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ was obtained by spontaneous crystallization from the melt of correspondent composition at $804^{\circ} \mathrm{C}$. Crystal structure with orthorhombic lattice parameters: $\mathrm{a}=22.5731(3) \AA, \mathrm{b}=14.0523(2) \AA, \mathrm{c}=5.5149(1) \AA, \mathrm{V}=1749.34(4), \mathrm{Z}=8$, SG Pcab was determined by Xray powder diffraction technique. The $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]^{2+}$-layers, which are typical for bismuth oxide compounds, transform into cationic endless strips of 4 bismuth atoms width directed along the c -axis in $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$. The strips combining stacks are separated by flat triangle $\left[\mathrm{BO}_{3}\right]^{3-}$-anions within stacks. Neighboring stacks are separated by tetrahedral $\left[\mathrm{PO}_{4}\right]^{3-}$-anions and shifted relatively to each other. Bismuth atoms are placed in 5-7 vertex oxygen irregular polyhedra. $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ is stable up to $812{ }^{\circ} \mathrm{C}$, then melts according to the peritectic law. The absorption spectrum in the range $350-700 \mathrm{~nm}$ was obtained and the width of the forbidden band was estimated as 3.46 eV . The band electronic structure of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ was modeled using DFT approach. The calculated band gap ( 3.56 eV ) is in good agreement with the experimentally obtained data.


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## 1. Introduction

Steady interest to bismuth containing mixed oxides is supported over the years due to the variety of phases with interesting physical properties. Crystalline bismuth borates are well known due to
optical activity. Bismuth borate glasses have also found an application in optics. $\mathrm{BiB}_{3} \mathrm{O}_{6}$ crystals attracted attention by its non-linear optical properties [1]. The phase diagram of $\mathrm{Bi}_{2} \mathrm{O}_{3}-\mathrm{B}_{2} \mathrm{O}_{3}$ system was firstly described in [2]. There were data on five double oxides with $\mathrm{Bi}: \mathrm{B}$ ratio 12:1, 2:1, 3:5, 1:3 and 1:4. Later, the data on four polymorphs were added to this number [1]. The existence of six polymorphs of bismuth triborates $\mathrm{BiB}_{3} \mathrm{O}_{6}$ was reported in [3]. In addition, the metastable diagram was discussed in the literature [4]. Two compounds with $\mathrm{Bi}: \mathrm{B}$ ratio $5: 3$ and $1: 1$ were described.

The data on quasi binary system $\mathrm{Bi}_{2} \mathrm{O}_{3}-\mathrm{BiPO}_{4}$ were published in [5-7]. It appeared to be very rich for individual phases. The existence from four [5,6] to ten [7] double oxides have been mentioned. For example, the phases with $\mathrm{Bi}: \mathrm{P}$ ratio 17:1, 7:1, 5,7:1, 31:9, 3:1, 37:13, 17:7, 2:1, 7:4 11:7 were noted in [7].

One compound is known in $\mathrm{B}_{2} \mathrm{O}_{3}-\mathrm{P}_{2} \mathrm{O}_{5}$ system. It is boron orthophosphate $\mathrm{BPO}_{4}$, having tetrahedral and hexagonal modifications. The latter melts congruently at $1600^{\circ} \mathrm{C}$.

The abundance of compounds in binary systems is in the contrast with scarcity of the data on the ternary system $\mathrm{Bi}_{2} \mathrm{O}_{3}$ $-\mathrm{B}_{2} \mathrm{O}_{3}-\mathrm{P}_{2} \mathrm{O}_{5}$. The area near bismuth oxide in composition triangle was described in $[8,9]$ where ternary oxide with sillenite structure was detected. Boron and phosphorus atoms occupy the joint crystallographic positions in the structure. Limited information concerning an existence of two ternary compounds with the compositions $\mathrm{Bi}_{9.68} \mathrm{~B}_{2.58} \mathrm{P}_{0.65} \mathrm{O}_{20}$ and $\mathrm{Bi}_{10} \mathrm{~B}_{6} \mathrm{P}_{2} \mathrm{O}_{29}$ was reported in [10]. There are no data on ternary bismuth-boron-phosphorus oxides in the current version of ICSD database [version 1.9.4-20142]. However, variety of chemical compounds are already established in binary systems causing the assumption of the existence of a number of crystalline phases in the ternary system which detections are difficult for some reasons. The expectation is supported by the extensive surveys dedicated to the synthesis, structure and properties of borophosphates with other elements [11,12].

In this paper practically pure ternary oxide $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ was obtained by the spontaneous crystallization approach. The X-ray powder diffraction data were interpreted and the crystal structure of the phase was established. The temperature range of thermal stability was investigated. The band electronic structure was calculated and its correspondence to obtained spectroscopic data was considered.

## 2. Materials and methods

### 2.1. Synthesis of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$

The synthesis of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ was carried out with correspondence thermal analysis data. $\mathrm{Bi}_{2} \mathrm{O}_{3}$ and $\mathrm{B}_{2} \mathrm{O}_{3}$ (highest purity grade, REAKHIM, RF) have been used as starting chemicals for preparation of initial melt. Phosphorus was introduced into the system in the form of $\mathrm{BPO}_{4}$, previously prepared according to [13]. Initial reagents were calcined in a platinum crucible: boron oxide - at $1000-1100^{\circ} \mathrm{C}$ for $6-10 \mathrm{~h}$, the other components at $700^{\circ} \mathrm{C}$. Starting components were loaded into a platinum crucible, melted at $900^{\circ} \mathrm{C}$ and kept at this temperature until complete homogenization. The melt cooling was carried out in several steps. At the first step the melt was cooled down to the intermediate temperature $820^{\circ} \mathrm{C}$ with the rate about $5^{\circ} \mathrm{C} / \mathrm{min}$ and exposed for about an hour. At the second step the melt was cooled down to $806-810^{\circ} \mathrm{C}$ with the rate $1-3^{\circ} \mathrm{C} / \mathrm{h}$. Then the platinum wire was introduced in the melt as a seed and temperature was gradually adjusted to $800-806{ }^{\circ} \mathrm{C}$. Under these conditions, intergrowth crystals of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ grew on the platinum wire with the size up to 5 mm . The crystals were taken from the melt and cooled in air. The weight lost of the melt due to evaporation was not higher than $1 \%$ in the course of the synthesis.

### 2.2. Thermal analysis

The simultaneous thermal analyzer Neitzsch STA 449S was used for thermal analysis. The heating rate was $5^{\circ} / \mathrm{min}$. Fig. 1 presents the thermograms of initial mixture and $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ heating.

### 2.3. The spectroscopic data (FT-IR and VIZ)

IR spectra were recorded in the $400-4000 \mathrm{~cm}^{-1}$ region with resolution $2 \mathrm{~cm}^{-1}$ on Nicolet 6700 IR spectrophotometer (Fig. 2). The sample was prepared by mixing approximately 1 mg of material $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ with 1 g KBr . The resulting mixture was milled and pressed into the tablet.

The absorption spectrum in the visible and UV ranges were obtained on Shimadzu UV-3600 spectrophotometer in the wavelength range $350-700 \mathrm{~nm}$ with 1 nm resolution. According to the absorption edge the band gap was determined. Elemental analysis was carried out by EPMA approach using SEM TM3000 (Hitachi) with SwiftED3000 detector (Oxford Instruments Analytical Ltd.).

### 2.4. Crystal structure determination

The X-ray powder diffraction data were obtained using X'Pert PRO diffractometer (PANalytical) with PIXcel detector, equipped with a graphite monochromator and $\mathrm{CuK} \alpha$ radiation. The substance for sample was grinded in an agate mortar and placed in the cuvette of 25 mm diameter by means of direct loading. The excess of the substance was cut off with a razor to prevent particle preferred orientation on the surface. The scan was performed at $\mathrm{T}=22^{\circ} \mathrm{C}$ in the range from 5 to $110^{\circ} 2 \theta$, step $0.026^{\circ}, \Delta t-50^{\circ} \mathrm{C}$. The angular limit for the scan was caused by the lack of significant diffraction peak in the far angle region.

Unit cell parameters were determined and refined using the programs described in [14,15]. Approximate bismuth atom locations were established by direct methods using EXPO2004 program [16]. The positions of light atoms were determined on the basis of electron density maps and refined with the help of programs [17,18]. The restrictions as weight coefficients were imposed on refined coordinates to ensure compliance with expected intermolecular geometry (interatomic distances and angles) for known structural groups. The structure refinement was carried out by gradual removal of restrictions. Thermal parameters of bismuth atoms were refined in the anisotropic approximation, others - in the isotropic. The final correspondence between the calculated and experimental X-ray diffraction patterns for the final structural model is shown in Fig. 3. Table 1 summarizes crystallographic data experimental conditions and Figs. 4-6 shows the crystal structure of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.


Fig. 1. The heating curves of the sample $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ phase (DSC 1) and the starting mixture $\mathrm{Bi}_{2} \mathrm{O}_{3}$ and $\mathrm{BPO}_{4}$ (DSC 2).


Fig. 2. IR-FT spectrum of the phase $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.

### 2.5. Quantum chemical modeling

Quantum chemical modeling of band structure was carried out using the software package VASP 5.2. (Vienna Ab-initio Simulation Package) $[19,20]$. The density functional theory (DFT) was applied $[21,22]$ with the plane wave basis set and PAW formalism [23,24]. The calculations were carried out using the generalized gradient approximation (GGA) - exchange-correlation functional PBE (Per-dew-Burke-Ernzerhof). By optimization of geometry and construction of the states densities for the integration by the first Brillouin zone (1BZ), which was automatically divided into a grid 4.4 .6 selected by scheme Monhorsta-Pak [25]. The lattice reciprocal space was divided into 20 intermediate $k$-points along each symmetry directions for the band structure constructing. The cutoff energy of the plane waves in the calculations was 400 eV . The structure modeling was carried out to maximum values of the forces, acting on atoms, equal to $0.01 \mathrm{eV} / \AA \AA$.


Fig. 3. XRD pattern for $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$. The experimental (dots) and calculated (solid line), the difference (solid line), position of calculated reflections in bottom.

## 3. Results and discussion

### 3.1. Phase formation and thermal properties

Studying the system $\mathrm{Bi}_{2} \mathrm{O}_{3}-\mathrm{B}_{2} \mathrm{O}_{3}-\mathrm{P}_{2} \mathrm{O}_{5}$ it was found that $2 \mathrm{Bi}_{2} \mathrm{O}_{3}$ : $\mathrm{BPO}_{4}$ mixture annealing at $700^{\circ} \mathrm{C}$ leaded to formation of new ternary oxide $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$. A sample of the same composition obtained by quenching from the melt, followed by annealing, was virtually identical. However, the solid state interaction resulted in the appearance of small impurities including $\mathrm{Bi}_{7} \mathrm{PO}_{13}$ (PDF 49-38). When the melt was cooled at rate $5^{\circ} \mathrm{C} / \mathrm{min}$ a multiphase mixture was formed whose main component was $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ with phases $\mathrm{Bi}_{3} \mathrm{PO}_{7}$ (PDF 44-645) and $\mathrm{Bi}_{4} \mathrm{~B}_{2} \mathrm{O}_{9}$ (PDF 46-420) as impurities. The impurities prevented the phase composition establishing, the crystal structure determination and investigation of physical properties.

Table 1
Crystallographic data and some experimental conditions for $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.

| Chemical formula | $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ |
| :---: | :---: |
| Molecular weight | 1037.70 |
| Crystal system | Orthorhombic |
| Space group | Pcab(61) |
| A, Å | 22.5731(3) |
| B, Å | 14.0523(2) |
| C, Å | 5.51487(8) |
| $\alpha,{ }^{\circ}$ | 90 |
| $\beta$, ${ }^{\circ}$ | 90 |
| $\gamma,{ }^{o}$ | 90 |
| $V, \AA^{3}$ | 1749.34(4) |
| Z | 8 |
| $P_{\text {calc. }}, \mathrm{g} / \mathrm{cm}^{3}$ | 7.88 |
| Colour | Colorless |
| $\mu, \mathrm{mm}^{-1}$ | 157.39 |
| T, K | 295 |
| Diffractometer | X'Pert PRO |
| Radiation | $\mathrm{Cu} \mathrm{K} \alpha$ |
| $\lambda, \AA$ Á | $\lambda_{1}=1.54056, \lambda_{2}=1.54439$ |
| Scan. area, $2 \theta\left({ }^{\circ}\right.$ ) | 3.014-110.92 |
| Number of points | 3192 |
| Number of reflections | 1108 |
| Number of refined parameters | 96 |
| $R_{p}$, \% | 8.10 |
| $R_{\text {wp }}$, \% | 10.60 |
| $\mathrm{R}_{\text {exp }}$, \% | 5.70 |
| $S=R_{w p} / R_{\text {exp }}$ | 1.88 |



Fig. 4. The crystal structure of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.


Fig. 5. Bismuth-oxygen tape with composition $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}$ and coordinating anions $\left[\mathrm{PO}_{4}\right]^{3-}$ and $\left[\mathrm{BO}_{3}\right]^{3-}$.

The synthesis approach of the pure phase was selected on basis of thermal analysis data. The thermogram of the original sample with composition $2 \mathrm{Bi}_{2} \mathrm{O}_{3}: \mathrm{BPO}_{4}$ has a number of effects caused by the interactions of the initial components (Fig. 1). The endothermic effect is associated with the solidus and solidus on the phase diagram $\mathrm{Bi}_{2} \mathrm{O}_{3}-\mathrm{B}_{2} \mathrm{O}_{3}$. The appearance of the liquid phase activates the component interactions. The exothermic effect at $692{ }^{\circ} \mathrm{C}$ is extended on temperature axis, indicating the diffusion restrictions for the chemical reaction. The exothermic effect at $792^{\circ} \mathrm{C}$ quickly transforms into deep endothermic one which corresponds to the peritectic decomposition of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$. Further heating does not induce any individual thermal effects. It means that the system is being in liquid state. Taking into account specific thermal behavior of the bismuth compound near the melting point, the experience of solid state synthesis and synthesis by annealing the quenched melt, the method of spontaneous crystallization was tested for the single phase material preparation. The melt was prepared as described


Fig. 6. Bismuth-oxygen tape with composition $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}{ }_{\mathrm{n}}$.
above. It was cold close to the peritectic temperature and then platinum wire was applied as crystallization seeding. The substance formed on the end of the wire was colorless or yellowish transparent solid with the hardness equals 5 on the Mohs scale. There is only the endothermic peak at $812{ }^{\circ} \mathrm{C}$ corresponding peritectic decomposition on the thermogram of the sample. The extended thermal effect covers the temperature associated with the liquidus (Fig. 1). Gravimetric measurements showed the constant weight of the sample during heating up to $1100^{\circ} \mathrm{C}$.

To confirm the chemical composition of the crystals X-ray microprobe analysis was performed. Composition of the sample: 15.23 mas.\% O, 80.73 mas.\% Bi, 1.27 mas.\% B, 2.76 mas.\% P (61.6 at.\% O, 24.9 at.\% Bi, 7.7 at.\% B, 5.7 at.\% P). Taking into account the e.s.d. of the method we can assert that the compound has a stoichiometric composition $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.

### 3.2. IR spectroscopy of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$

The band assignments in IR spectrum of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ were made basing on literature data [26-29]. There are four extended
absorption region (Fig. 2). The bands in the range $400-600 \mathrm{~cm}^{-1}$ were assigned to the valence vibrations of $v_{s}(\mathrm{Bi}-\mathrm{O})$ bonds. $\mathrm{Ab}-$ sorption bands at $705 \mathrm{~cm}^{-1}$ and $730 \mathrm{~cm}^{-1}$ in adjacent area can be interpreted as the asymmetric oscillation of bridging bonds in the polymer chains $\delta_{\mathrm{as}}(\mathrm{B}-\mathrm{O}-\mathrm{Bi})$ and $\delta_{\mathrm{as}}(\mathrm{P}-\mathrm{O}-\mathrm{Bi})$ respectively. Symmetric and asymmetric valence vibrations $v_{\mathrm{s}}, \mathrm{v}_{\mathrm{as}}(\mathrm{P}-\mathrm{O})$ give a set of split bands near $1000 \mathrm{~cm}^{-1}$ referring to vibrations in the tetrahedral anions $\mathrm{PO}_{4}^{3-}$. In the region $1150-1300 \mathrm{~cm}^{-1}$ there are absorption bands related to boron-oxygen structural units. There are no bands corresponding ( $\mathrm{B}-\mathrm{O}-\mathrm{P}$ ) vibrations detected on IR spectrum.

### 3.3. Crystal structure of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$

Because of the difficulty in obtaining perfect single crystals in conditions of peritectic reaction the crystal structure investigation was carried out by X-ray powder diffraction technique. The basic crystal data and conditions of the diffraction experiment are shown in Table 1. The experimental and calculated X-ray diffraction patterns are shown in comparison in Fig. 3. The degree of diffraction pattern fitness allows us to suppose that the level of possible impurities does not exceed $1-1.5 \%$.

The crystal structure of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ can be referred to strip polymers (Fig. 4). Considering symmetry, local structure, bond lengths allows identify the individual anionic groups $\left[\mathrm{PO}_{4}\right]^{3-}$ and $\left[\mathrm{BO}_{3}\right]^{3-}$ within the crystal framework. They can be regarded as anions compensating charge of cationic part with formal composition $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]$ and polymer structure. Anions $\left[\mathrm{PO}_{4}\right]^{3-}$ have nearly ideal tetrahedral geometry with the $\mathrm{P}-\mathrm{O}$ distances in the range $1.51-1.53 \AA$ (Tables 2 and 3 ). $\left[\mathrm{BO}_{3}\right]^{3-}$ anions are slightly distorted planar triangles with $\mathrm{B}-\mathrm{O}$ distance of about $1.42 \AA$.

The cationic part of the structure is formed by three layered endless strips $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]_{\mathrm{n}}$ oriented along the c-axis (Figs. 5 and 6). Taking into account the charge of phosphate and borate groups the specific charge of the bismuth-oxygen stripe should be regarded as $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}$. Thus, the positively charged strips are coordinated by phosphate and borate anions. The strip structure presents distorted fragment of a three-layer fluorite-grid $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]^{2+}$, well known as $\delta-\mathrm{Bi}_{2} \mathrm{O}_{3}$ structure and occurred in numerous Aurivillius phases [30]. Oxygen atoms form a slightly distorted square grid, where the bismuth atoms are coordinated above and lower checkered pattern so that each bismuth atom is in vertex of a tetragonal pyramid. $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]_{\mathrm{n}}$ plane is divided into strips with the width of four bismuth atoms in the $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ structure (Figs. 5 and 6).

The edge of oxygen "square" in the strip remains incomplete and is compensated by the oxygen atoms of $\left(\mathrm{PO}_{4}\right)^{3-}$ anions. Considering the oxygen atoms from anionic groups four types of distorted coordination polyhedrons around Bi can be selected. Bismuth coordination number changes from 5 to 8 . Short $\mathrm{Bi}-\mathrm{O}$ distances are in the range $1.86-2.65 \AA$ (Table 2).
$\left[\mathrm{BO}_{3}\right]^{3-}$ anions cross link the parallel strips. The asymmetric
coordination of $\left[\mathrm{BO}_{3}\right]^{3-}$ anions on top and bottom results in small "bend" of the strips (Figs. 4 and 5). $\left(\mathrm{PO}_{4}\right)^{3-}$ anions participate both in strips linking into the stack and in the binding adjacent stacks. These groups are responsible for the shift of adjacent stacks respectively each other.

The reason leading to the fragmentation of infinite plane $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]_{\mathrm{n}}$ into the separated strips apparently relates with the chemical composition of the compound. It is well known that highly charged metal ions have no strong polarization feature due to charge compensation mechanism by forming oxygenated cations, e.g., $\mathrm{VO}_{2}^{+}, \mathrm{UO}_{2}^{2+}[31]$. The chemical stability of $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]_{\mathrm{n}}^{2+}$ plane is supported using similar procedure. In the case of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ the compensation of bismuth charge is completed by the formation of $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}$-charged infinite cationic framework. Apparently $\left[\mathrm{PO}_{4}\right]^{3-}$ anion influence on stoichiometry of $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}$ by attracting oxygens from bismuth oxide. Finally bismuth oxide with a nominal composition of $\mathrm{Bi}_{4} \mathrm{O}_{6}$ loses 3 oxygen atoms, becoming a cation $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}$. Lack of oxygen atoms causes the fragmentation of the plane $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]_{n}^{2+}$ into the strips. As a result the structure $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ is constructed from stacks of endless $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]$ strips separated by $\left(\mathrm{BO}_{3}\right)^{3-}$ and $\left(\mathrm{PO}_{4}\right)^{3-}$ anions.

Among the known bismuth borates and phosphates there are no analogues containing layers of $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]$. The phase $\mathrm{Bi}_{4} \mathrm{~B}_{2} \mathrm{O}_{9}$ is much close in composition to the discussed compound [32]. Borons have similar triangular coordination. However there are no layers of [ $\mathrm{Bi}_{2} \mathrm{O}_{2}$ ] or fragments thereof in the structure. Layered structures known among dioxo-dibismuth hydroborates $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]\left[\mathrm{B}_{3} \mathrm{O}_{5}(\mathrm{OH})\right]$ and $\left[\mathrm{Bi}_{2} \mathrm{O}_{2}\right]\left(\mathrm{BO}_{2}(\mathrm{OH})\right)[31]$.

## 3.4. $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ electronic band structure modeling

Fig. 7 presents the band electronic structure of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ obtained by DFT approach. The calculated and experimental absorption spectra are shown in Fig. 8a, b. The obtained forbidden band gap is 3.56 eV . It is rather close to the experimental value of 3.46 eV . The results show that the compound is a direct-gap semiconductor with a band gap minimum in the "gamma" point. Absorption spectrum calculated for different directions of the crystal (Fig. 8) indicates the presence of optical anisotropy, which is the most pronounced along the $b$ axis.

In particular, the difference is in the presence on the calculated spectrum the long-wavelength peak at $\sim 350 \mathrm{~nm}(3.55 \mathrm{eV})$ near the absorption edge. This spectral feature can be explained by the orientation of the nonbonding orbitals. An indirect confirmation of their presence in the system is weak dispersion of the top filled band which is absent along other directions. To identify the localization of nonbonding atomic orbitals the state densities were calculated (Fig. 7). The largest contribution to the partial state densities near the Fermi level was made by oxygen and bismuth atoms. The localized $6 \mathrm{~s}^{2}$ electron pairs and polyhedra type as $\mathrm{EBiO}_{3}$ and $\mathrm{EBiO}_{4}$ (where $\mathrm{E}-6 s^{2}$ pair) are often taken into account in

Table 2
The interatomic distances in $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.

| Atom A | Atom B | $\mathrm{d}(\mathrm{A}-\mathrm{B}), \AA$ | Atom A | Atom B | d(A-B), $\AA$ | Atom A | Atom B | d(A-B), $\AA$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bi1 | 03 | 2.032(17) | Bi2 | 09 | 2.519(15) | Bi4 | 01 | 2.616(16) |
| Bi1 | 03 | 2.537(18) | Bi3 | 06 | 2.574(4) | Bi4 | 010 | 2.705(16) |
| Bi1 | 09 | 2.653(4) | Bi3 | 02 | 2.228(12) | P1 | 05 | 1.52(2) |
| Bi1 | 05 | 2.617(15) | Bi3 | 01 | 1.858(3) | P1 | 07 | 1.53(4) |
| Bi1 | 01 | 2.402(17) | Bi3 | 04 | 2.395(16) | P1 | 06 | 1.518(19) |
| Bi2 | 01 | 2.504(15) | Bi3 | 010 | 2.305(15) | P1 | 04 | 1.51(4) |
| Bi2 | 02 | 1.897(12) | Bi4 | 08 | 1.859(3) | B1 | 08 | 1.42(2) |
| Bi2 | 07 | 2.628(15) | Bi4 | 03 | 2.623(4) | B1 | 09 | 1.418(16) |
| Bi2 | 05 | 2.379(12) | Bi4 | 03 | 2.163(4) | B1 | 010 | 1.42(2) |

Table 3
The bond angles in $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.

| Atom A | Atom B | Atom C | Angle (ABC) | Atom A | Atom B | Atom C | Angle (ABC) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bi1 | 03 | Bi1 | 110.09(14) | Bi2 | 09 | B1 | 114.3(12) |
| Bi1 | 02 | Bi2 | 115.27(12) | Bi4 | 08 | B1 | 110.66(11) |
| Bi1 | 01 | Bi2 | 100.45(10) | Bi3 | 010 | B1 | 115.6(12) |
| Bi1 | 03 | Bi4 | 116.28(12) | Bi3 | 04 | P1 | 162.23(7) |
| Bi1 | 09 | B1 | 106.72(6) | Bi2 | 05 | P1 | 105.0(17) |
| Bi4 | 03 | Bi4 | 106.46(13) | Bi4 | 06 | P1 | 121.9(11) |
| Bi4 | 01 | Bi3 | 102.98(12) | Bi2 | 07 | P1 | 110.03(6) |
| Bi4 | 02 | Bi3 | 98.8(4) |  |  |  |  |



Fig. 7. The electronic band structure, total (TDOS) and partial (pDOS) state density for a single crystal $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.
describing the bismuth coordination sphere in its oxide phases. Therefore the partial state densities for $s$ - and $p$-electrons were constructed separately for nonequivalent bismuth atoms (Fig. 9). Analysis of the state densities shows a significant mixing of the contributions from $s$ and p-orbitals of bismuth atoms, indicating their joint hybridization. The exception is the peak of state for the fourth Bi atom near the Fermi level corresponding to the nonbonding level of $6 s^{2}$ electron pair. In order to clarify the possible


Fig. 9. The partial state densities ( pDOS ) for s (black lines) and p electrons (red lines) of different bismuth atoms in a single crystal of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ near the Fermi level. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
orientation of $6 s^{2}$ electron pair the modeling the electron density distribution of the filled band top inside crystal cell of $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ was carried out (Fig. 10). Calculations showed the displacement of the electron density in the localized $6 s^{2}$ pair $\mathrm{Bi}_{4}$ atom with the formation of polyhedron $\mathrm{EBiO}_{4}$.

## 4. Conclusion

New bismuth borophosphate $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$ was obtained from the stoichiometric melt by spontaneous crystallization approach. At heating the compound is stable up to $812{ }^{\circ} \mathrm{C}$ then melts peritectically with decomposition. The crystal structure was determined by


Fig. 8. (a) - Calculated absorption spectra in the directions of the crystallographic axes; (b) - the experimental absorption coefficient of the powder sample for $\mathrm{Bi}_{4} \mathrm{BPO}_{10}$.


Fig. 10. The electron density distribution for the highest occupied zone in the unit cell (a) and $\mathrm{Bi}_{4}$ atom in the polyhedron(b).

X-ray powder diffraction technique. The peculiarity of the crystal structure of the compound is in the possibility of separating the anion and cation parts. Bismuth-oxygen cation part with specific composition $\left[\mathrm{Bi}_{4} \mathrm{O}_{3}\right]^{6+}$ forms endless strips with 4 bismuth atoms width. The parallel strips are gathered into the stacks and separated in stacks by planar triangular isolated anions $\left[\mathrm{BO}_{3}\right]^{3-}$. Tetrahedral anions $\left[\mathrm{PO}_{4}\right]^{3-}$ are located between adjacent stacks. The compound is the direct-gap semiconductor. The band gap is defined on the absorption edge in visible spectra equals to 3.46 eV . The band structure modeling by DFT method allowed the calculation of band gap ( 3.56 eV ) rather close to the experimental value. The direction of $6 \mathrm{~s}^{2}$ electron pair $\mathrm{Bi}_{4}$ was also calculated.

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