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# Polarization, transmission, and small-angle scattering of light by a polymer film with elongated droplets of nematic liquid crystal

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## ABSTRACT

An optical-mechanical model has been developed to describe the transmittance, polarization and small-angle distribution of light scattered by an uniaxially-stretched polymer film containing the elongated ellipsoidal droplets of nematic liquid crystal. It is based on the approximations of Foldy-Tworsky, anomalous diffraction, and single scattering. The spectral dependences of transmittances and polarizing abilities of the polymer dispersed liquid crystal films have been analyzed as well as the small-angle intensity distribution and the polarization degree of scattered light depending on the film thicknesses, refractive index of polymer matrix, sizes of droplets, their anisotropy parameters, concentration, polydispersity, and optical axes orientation. The optical characteristics of films with homogeneous and inhomogeneous interfacial anchoring at the surface of liquid crystal droplets have been considered. The transmittance and polarizing ability of the films have been studied as functions of the angular aperture of the system recording scattered light.

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## 1. Introduction

At present, polymer films with anisotropy of light absorption are most widely used as the polarizers [1–3]. A dichroism in such films is caused by the special additives into polymer matrix or by the anisotropy of own absorption of polymer macromolecules. The advantages of these materials are the compactness, low cost, and simple production technology. However, these polymer films are applicable in the laser and optical devices only at low power since a light absorption can result in the strong heating and following destruction of polymer matrix.

Polymer dispersed liquid crystal (PDLC) films, consisting of non-absorbing uniaxially-elongated liquid crystal (LC) droplets within polymer matrix [4–10], used as a polarizers, allow one to increase significantly the limit power of the incident light in comparison with dichroic polarizers. PDLC films can polarize a light with the power density of incident light up to 2 kWt/cm<sup>2</sup> [10]. They effectively polarize a light in the entire transparency region (visible and near IR) of the components used, while the dichroic polarizers

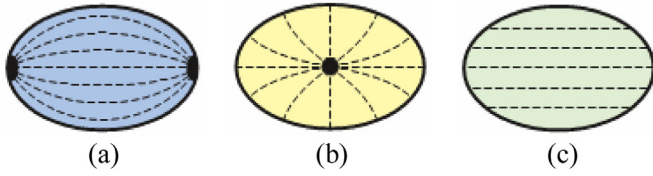
can do that only in the dichroic band of own or impurity absorption. Besides, PDLC films allow modulating the intensity, polarization and phase of light by applying the electric or magnetic field. They are particularly promising in the collimated laser devices and projection systems.

Recently, a new approach has been realized to control the optical response of PDLC film in the light-scattering mode, which is based on the surface anchoring transitions caused by ionic surfactant [11]. Unidirectional mechanical stretching of PDLC film doped with the ionic surfactants allows obtaining the LC director configuration (distribution of local optical axes) within the droplet volume close to homogeneous (monodomain) [12,13]. Thus, it gives an opportunity to achieve simultaneously the limit polarization characteristics for unpolarized incident light: the coherent transmission coefficient equal to 0.5 and the polarization degree of forward-transmitted light equal to  $\pm 1$  in the wide spectral range [14].

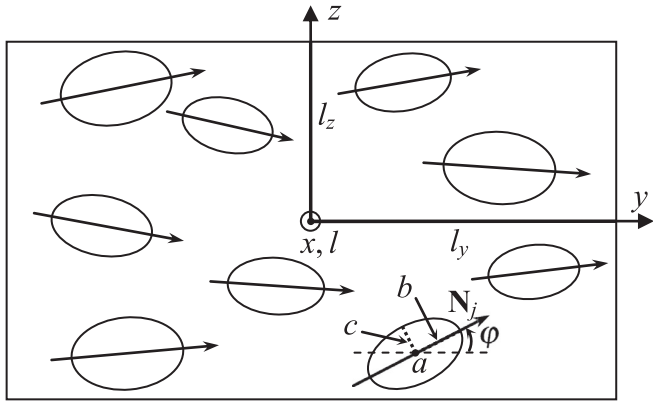
In this work we have studied the spectral dependences of the coefficients of coherent (directed) transmission and the polarization degree of forward-transmitted light, the angular distribution and polarization of light scattered in small angles by the stretched PDLC films with homogeneous (without surfactants) and inhomogeneous (with surfactants) surface anchoring. It has been considered the films consisting of ellipsoidal LC droplets with: (i) the

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**Fig. 1.** Orientational structures within ellipsoidal nematic droplets: bipolar (a), radial (b), and homogeneous monodomain (c). Director configurations are presented by dashed lines. Surface point defects (boojums) are indicated by black semicircles (a); bulk point defect (hedgehog) is shown by black circle (b).



**Fig. 2.** Scheme of the PDLC layer structure under stretching along  $y$  axis of the laboratory coordinate system  $(x, y, z)$ . The  $(y, z)$  plane coincides with the layer-front surface. The  $x$  axis is directed along the normal to PDLC layer;  $\varphi$  is the orientation angle of optical axis  $\mathbf{N}_j$  of an individual droplet;  $l$  and  $l_y, l_z$  are the thicknesses of stretched layer and its linear sizes along  $y, z$  axes;  $a, b, c$  are the semi-axes of elongated ellipsoidal droplets. The  $a$  semi-axes are oriented along  $x$  axis and  $b, c$  semi-axes are aligned in the  $(y, z)$  layer plane. The layer is normally illuminated by unpolarized light along  $x$  axis.

bipolar intrinsic structure formed under homogeneous tangential anchoring; (ii) the radial structure formed under homogeneous homeotropic (normal) anchoring; (iii) the monodomain structure raised due to inhomogeneous surface anchoring [12,13] (Fig. 1).

The transmittance, the small-angle distribution of scattered light and the polarizing ability of the film containing the ellipsoidal monodomain LC droplets have been analyzed as functions of angular aperture of the optical system.

## 2. Optical-mechanical model to describe the characteristics of scattered light. Basic equations

Let us consider a PDLC layer of thickness  $l$  placed in the  $(y, z)$  plane of laboratory coordinate system  $(xyz)$ , normally illuminated along  $x$  axis by unpolarized monochromatic light (Fig. 2).

Initially, the undeformed polymer matrix contains the polydisperse spherical (or spheroidal) LC droplets with circular section. Their optical axes are randomly oriented in  $(y, z)$  plane. The mechanical stretching of PDLC film along  $y$  axis results in the deformation of spheroidal droplets into the ellipsoidal ones with the  $a, b, c$  semi-axes and partially-oriented structure of optical axes  $\mathbf{N}_j$ ,  $j = 1, 2, \dots, N$ , where  $N$  is a number of droplets in the layer. The major semi-axes  $b$  of droplets and their optical axes  $\mathbf{N}_j$  are preferably oriented along the stretching axis  $y$ , the  $c$  semi-axes are aligned within  $(y, z)$  layer plane, the  $a$  semi-axes are directed along the  $x$  normal. The semi-axes of spherical droplets before stretching are designated by  $a_0 = b_0 = c_0$ . For spheroidal droplets  $a_0 < b_0 = c_0$ .

### 2.1. Coefficient of coherent (directed) transmission of the stretched PDLC film and the polarization degree of forward-transmitted light

Using the Foldy-Twersky approximation [14–19], we can write the expressions for the coherent (directed) transmission coefficient  $T_{np}^c$  and polarization degree  $P_c$  of the forward-transmitted light (the polarizing ability of layer for forward-transmitted light):

$$T_{np}^c = \frac{T_{||}^c + T_{\perp}^c}{2}, \quad (1)$$

$$P_c = \frac{T_{\perp}^c - T_{||}^c}{T_{||}^c + T_{\perp}^c}, \quad (2)$$

$$T_{||, \perp}^c = \exp(-\gamma_{2,1} l), \quad (3)$$

$$\gamma_{2,1} = \frac{3}{4} c_v \frac{\langle a^2 \rangle}{\langle a^3 \rangle} \left\{ \langle Q_e \rangle \frac{1 \pm S_{2f}}{2} + \langle Q_o \rangle \frac{1 \mp S_{2f}}{2} \right\}, \quad (4)$$

$$\langle a^2 \rangle = \int_0^{\infty} a^2 P(a) da, \quad (5)$$

$$\langle a^3 \rangle = \int_0^{\infty} a^3 P(a) da, \quad (6)$$

$$\langle Q_{e,o} \rangle = \frac{4 \langle \text{Re} S_{2,1}^0 \rangle}{k^2 \varepsilon_y \varepsilon_z \langle a^2 \rangle}, \quad (7)$$

$$\langle \text{Re} S_{2,1}^0 \rangle = \int_0^{\infty} \text{Re} S_{2,1}(\theta_s = 0, a, b = \varepsilon_y a, c = \varepsilon_z a) P(a) da, \quad (8)$$

$$S_{2f} = \frac{\sin(2\varphi_m)}{2\varphi_m}. \quad (9)$$

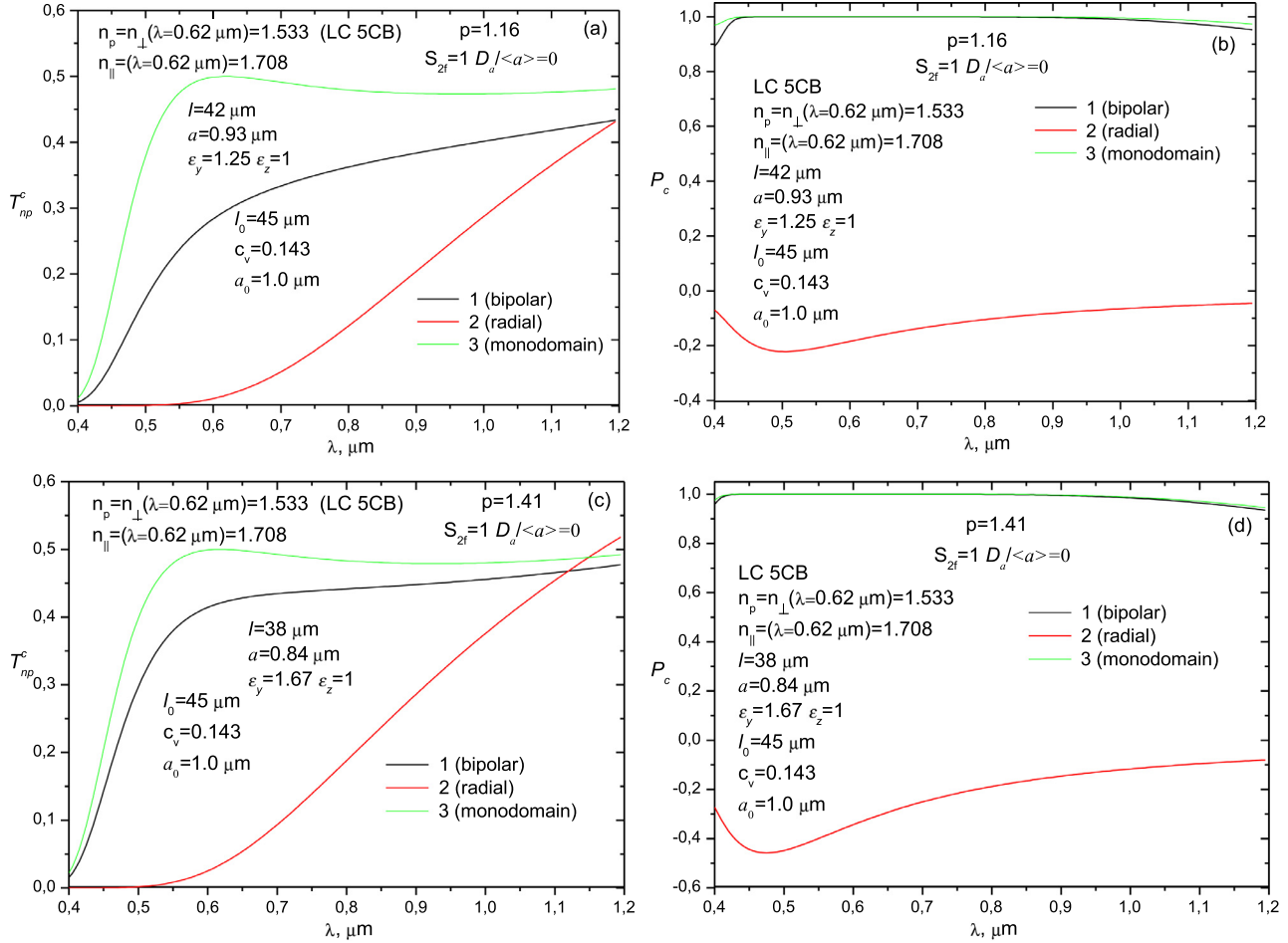
Here  $T_{||}^c$  and  $T_{\perp}^c$  are the coefficients of coherent transmission for the components of incident light polarized parallel and orthogonal to the stretching axis;  $\gamma_2$  and  $\gamma_1$  are the corresponding extinction coefficients of the layer;  $c_v$  is the volume filling factor of layer (the ratio of volume of all LC droplets to the volume of PDLC layer);  $\langle Q_e \rangle$  and  $\langle Q_o \rangle$  are the extinction efficiency factors [20] for the extraordinary and ordinary waves, averaged over the droplet sizes;  $S_{2f}$  is the two-dimensional order parameter of PDLC layer;  $k = 2\pi n_p / \lambda$ ,  $\lambda$  is the wavelength of incident light,  $n_p$  is the refractive index of polymer matrix;  $\varepsilon_y = b/a$  and  $\varepsilon_z = c/a$  are the parameters of droplet's anisotropy;  $\langle \text{Re} S_{2,1}^0 \rangle$  are the averaged real parts of the diagonal elements of amplitude scattering matrix for the strictly forward direction of scattering [14]; the angle brackets  $\langle \dots \rangle$  mean the average over the  $a$  semi-axis of droplets along the film normal;  $P(a)$  is the normalized probability density of  $a$  semi-axes distribution along the film normal;  $\varphi_m$  is the maximal angle of droplet optical axes deviation relatively to the stretching axis. At  $\varphi_m = 0$  the optical axes of droplets are entirely oriented along the stretching axis ( $S_{2f} = 1$ ). At  $\varphi_m = \pi$  they are oriented randomly ( $S_{2f} = 0$ ). The partial orientation occurs at  $0 < \varphi_m < \pi$  ( $S_{2f} < 1$ ).

The Eqs. (6)–(9) were obtained at the same anisotropy parameters  $\varepsilon_y$  and  $\varepsilon_z$  ( $\varepsilon_y = b/a = \text{const}$ ,  $\varepsilon_z = c/a = \text{const}$ ) for all droplets assuming the uniform distribution of the optical axes  $\mathbf{N}_j$  orientation in the  $(y, z)$  plane.

At stretching, the layer thickness  $l$  and the semi-axes  $a, b, c$  of droplets are related by the expressions [6,14]:

$$l = l_0 p^{-B}, \quad a = a_0 p^{-B}, \quad b = c_0 p, \quad c = c_0 p^{-A}, \quad (10)$$

where  $p$  is the stretching factor ( $p = l_y / l_{y0}$ ,  $l_{y0}$  is the layer length along  $y$ -axis before stretching);  $l_0$  is the layer thickness before stretching; constants  $A$  and  $B$  are determined by mechanical properties of the used polymer,  $A + B = 1$  [6]. If initially the LC droplets are spherical, then  $A = B = 0.5$ . For the initially spheroidal droplets:  $A \approx 0.4$  and  $B \approx 0.6$ .



**Fig. 3.** The spectral dependences of the coherent transmittance  $T_{np}^c(\lambda)$  (a, c) and polarization degree  $P_c(\lambda)$  of the forward-transmitted light (b, d) at the different stretching factor  $p$  of the PDLC films containing droplets with the bipolar (curves 1), radial (curves 2) and monodomain (curves 3) y-configuration of LC director.  $n_p = n_{\perp} = 1.533$  at  $\lambda = 0.62 \mu\text{m}$ .

## 2.2. Angular distribution of intensity and polarization degree of incoherently (diffusely) scattered light

Let the layer is illuminated by unpolarized light. Then the intensity  $I_{np}^{inc}$  and polarization degree  $P_{inc}$  of incoherently (diffusely) scattered light, the parallel  $I_{\parallel}^{inc}$  and orthogonal  $I_{\perp}^{inc}$  to the stretching axis components of scattered light intensity are determined as follows:

$$I_{np}^{inc} = \frac{1}{2} (I_{\parallel}^{inc} + I_{\perp}^{inc}), \quad (11)$$

$$P_{inc} = \frac{I_{\perp}^{inc} - I_{\parallel}^{inc}}{I_{\parallel}^{inc} + I_{\perp}^{inc}}, \quad (12)$$

$$I_{\parallel, \perp}^{inc} = (I_{vv}^{inc} + I_{vh}^{inc})|_{\alpha=0, \pi/2}. \quad (13)$$

Here  $I_{vv}^{inc}$  and  $I_{vh}^{inc}$  are  $vv$ - and  $vh$ -components of the intensity of scattered light with the parallel ( $vv$ -component) and orthogonal ( $vh$ -component) polarizations relatively to the polarization plane of incident wave;  $\alpha$  is the polarization angle (angle between the polarization plane of incident wave and the stretching axis  $y$ ) [21,22]. Relation (13) is obtained by averaging  $I_{vv}^{inc}$  and  $I_{vh}^{inc}$  over the polarization angle  $\alpha$  with a uniform  $\alpha$ -distribution ranging from 0 to  $2\pi$  [22].

If the filling factor  $c_v$  of the layer is low ( $c_v < 0.2$ ), then, using the single scattering approximation [23] for  $I_{vv}^{inc}$  and  $I_{vh}^{inc}$  com-

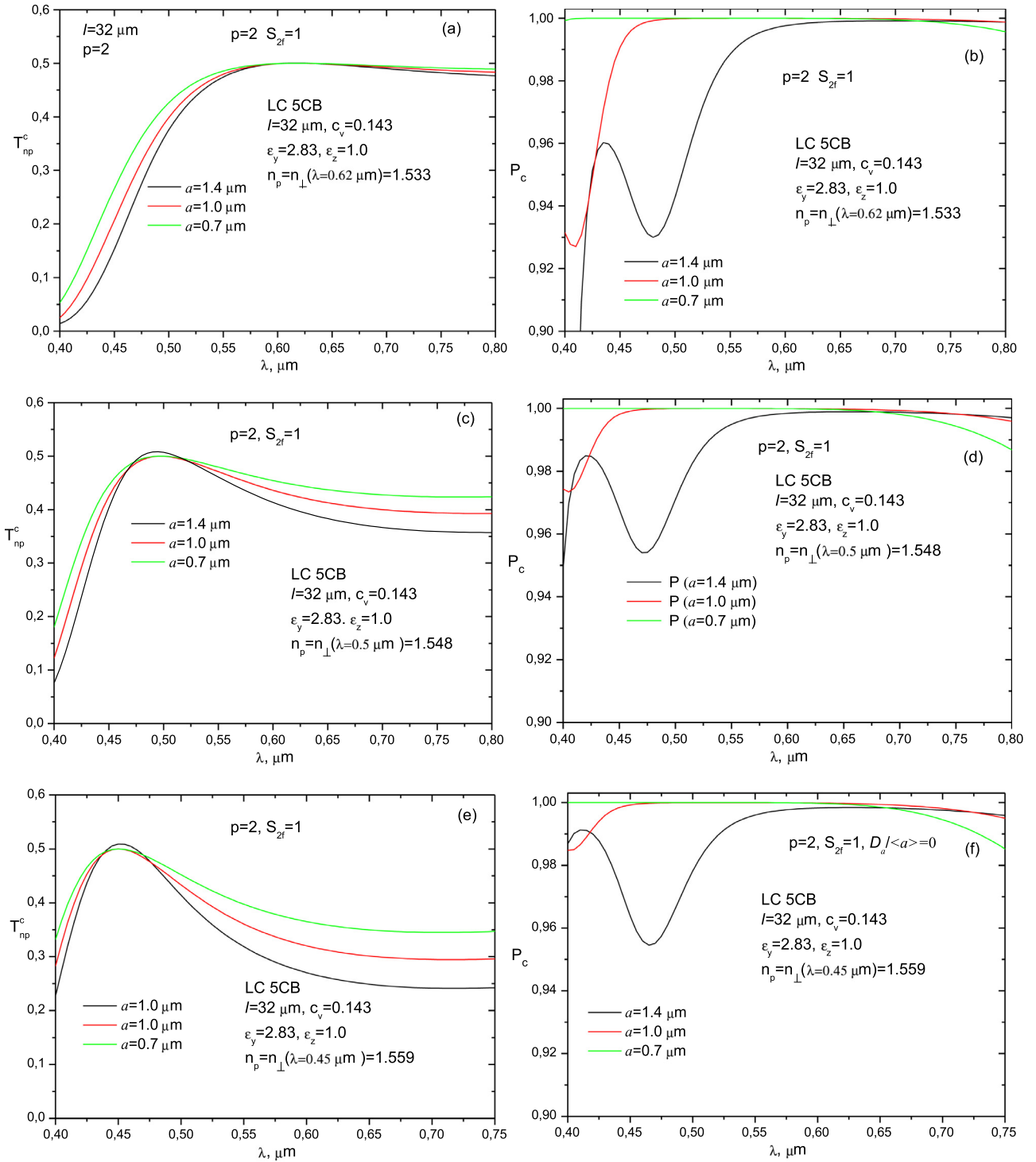
ponents of light intensity (entering in Eq. (13)), we obtain:

$$I_{vv, vh}^{inc}(\theta_s, \varphi_s) = C \frac{l \langle a^2 \rangle}{4 \epsilon_y \epsilon_z \langle a^3 \rangle} \frac{c_v}{k^2 \langle \sigma \rangle} \langle |f_{vv, vh}(\theta_s, \varphi_s)|^2 \rangle_{a, \mathbf{N}_j}, \quad (14)$$

where  $\theta_s$  and  $\varphi_s$  are the polar and azimuthal scattering angles [22,24];  $C = |E_i^2| A/R^2$ ,  $E_i$  is the amplitude of incident wave,  $A$  is the area of the illuminated part of the layer;  $R$  is the distance from layer to the observation point;  $\sigma = \pi bc$  is the section of droplet in the  $yz$  layer plane;  $f_{vv}(\theta_s, \varphi_s)$  and  $f_{vh}(\theta_s, \varphi_s)$  are  $vv$ - and  $vh$ -components of vector amplitude scattering function of the individual LC droplet [21,22,24]; the angle brackets  $\langle \dots \rangle_{a, \mathbf{N}_j}$  mean averaging over the size  $a$  and orientation of optical axes  $\mathbf{N}_j$  of droplets.

Assuming independence of the distributions of droplets over the size and orientation of their optical axes, we have:

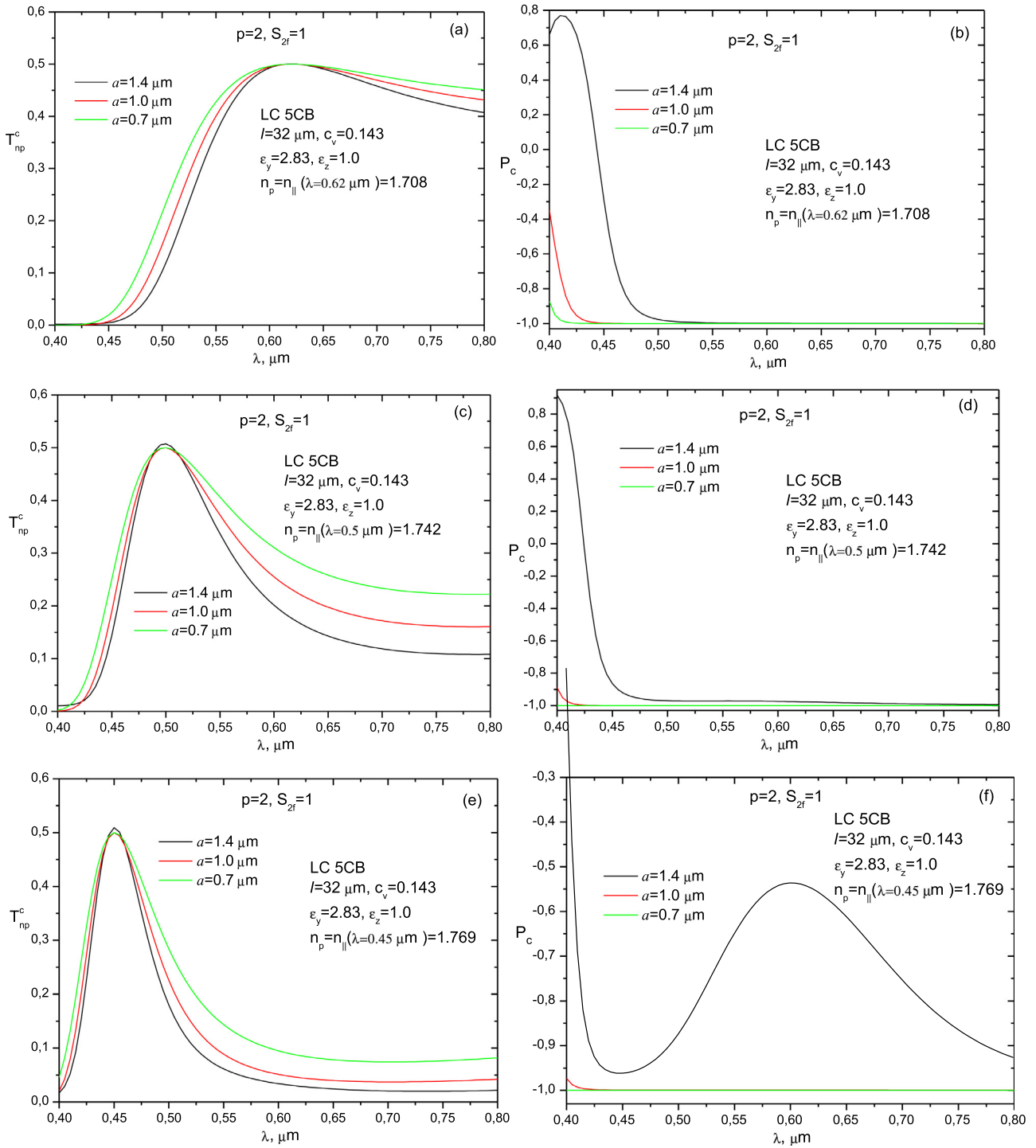
$$\begin{aligned} \langle |f_{vv}|^2 \rangle_{a, \mathbf{N}_j} &= \langle |S_2|^2 \overline{\cos^4(\alpha - \varphi_s - \varphi_d)} + |S_1|^2 \overline{\sin^4(\alpha - \varphi_s - \varphi)} \rangle \\ &+ \frac{1}{4} \langle \{S_1 S_2^* + S_2 S_1^* + (S_3 + S_4)(S_3^* + S_4^*)\} \overline{\sin^2 2(\alpha - \varphi_s - \varphi)} \rangle \\ &+ \frac{1}{8} \langle \{ (S_3 + S_4) S_2^* + S_2 (S_3^* + S_4^*) \} \overline{[2 \sin 2(\alpha - \varphi_s - \varphi)]} \rangle \\ &+ \overline{\sin 4(\alpha - \varphi_s - \varphi)} + \frac{1}{8} \langle \{ (S_3 + S_4) S_1^* + S_1 (S_3^* + S_4^*) \} \rangle \\ &\overline{[2 \sin 2(\alpha - \varphi_s - \varphi) - \sin 4(\alpha - \varphi_s - \varphi)]}, \end{aligned} \quad (15)$$



**Fig. 4.** The spectral dependences of coherent transmittance  $T_{np}^c$  (a, c, e) and polarization degree  $P_c$  (b, d, f) of the forward-transmitted light at the different sizes of lateral droplet semiaxis  $a$  for the polymer refractive index  $n_p$  equaled to the ordinary refractive index  $n_{\perp}$  of 5CB at  $\lambda = 0.62$  (a, b);  $0.5$  (c, d) and  $0.45$   $\mu\text{m}$  (e, f). Monodisperse droplets with the monodomain LC structure and oriented optical axes (the film order parameter  $S_{2f} = 1$ ). The stretching ratio of film is  $p = 2$ , the droplet lateral semiaxis is  $a = 0.7$   $\mu\text{m}$ , the film thickness is  $l = 32$   $\mu\text{m}$ , the volume filling factor of PDLC film is  $c_v = 0.143$ , the anisotropy parameters of LC droplets are  $\epsilon_y = 2.83$ ,  $\epsilon_z = 1.0$ .

$$\begin{aligned}
 \langle |f_{vh}|^2 \rangle_{a, N_j} = & \langle |S_3|^2 \rangle \overline{\sin^4(\alpha - \varphi_s - \varphi_d)} + \langle |S_4|^2 \rangle \overline{\cos^4(\alpha - \varphi_s - \varphi)} \\
 & + \frac{1}{4} \langle \{ (S_2 - S_1)(S_2^* - S_1^*) - S_4 S_3^* - S_3 S_4^* \} \rangle \overline{\sin^2(\alpha - \varphi_s - \varphi)} \\
 & - \frac{1}{8} \langle \{ (S_2 - S_1)S_4^* + S_4(S_2^* - S_1^*) \} \rangle \overline{[2\sin 2(\alpha - \varphi_s - \varphi) + \sin 4(\alpha - \varphi_s - \varphi)]} + \frac{1}{8} \langle \{ (S_2 - S_1)S_3^* + S_3(S_2^* - S_1^*) \} \rangle \\
 & \overline{[2\sin 2(\alpha - \varphi_s - \varphi) - \sin 4(\alpha - \varphi_s - \varphi)]}, \quad (16)
 \end{aligned}$$

where  $S_j = S_j(\theta_s, \varphi_s)$  are the elements of the amplitude scattering matrix of the individual LC droplet ( $j = 1, 2, 3, 4$ ) [22,24–26].



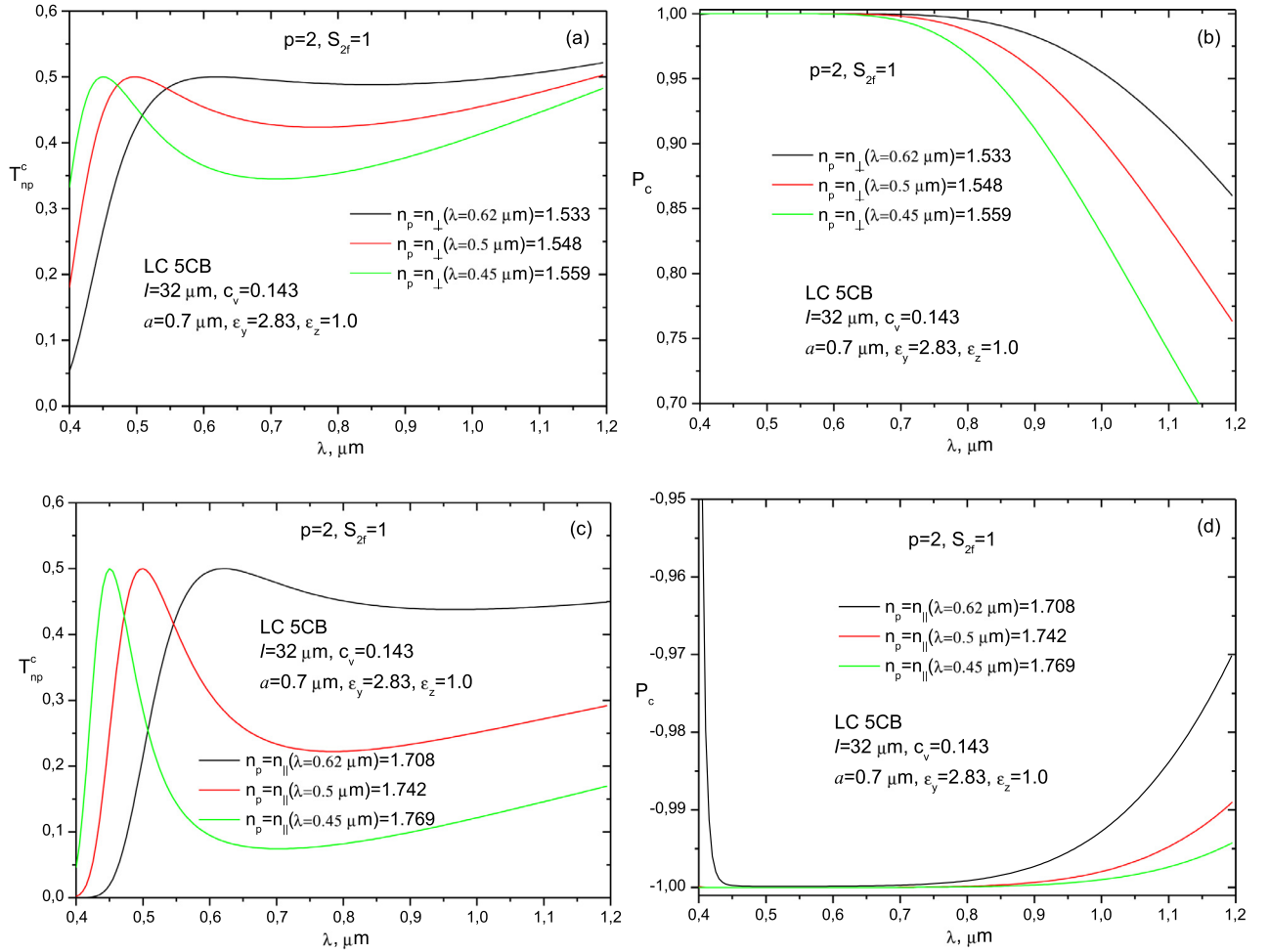
**Fig. 5.** The spectral dependences of coherent transmittance  $T_{np}^c$  (a, c, e) and polarization degree  $P_c$  (b, d, f) of the forward-transmitted light at the different sizes of lateral droplet semiaxis  $a$  for the polymer refractive index  $n_p$  equaled to the extraordinary refractive index  $n_{||}$  of 5CB at  $\lambda = 0.62$  (a, b);  $0.5$  (c, d) and  $0.45$   $\mu\text{m}$  (e, f). Monodisperse droplets with the monodomain LC structure and oriented optical axes.  $S_{2f} = 1$ ,  $p = 2$ ,  $a = 0.7$   $\mu\text{m}$ ,  $l = 32$   $\mu\text{m}$ ,  $c_v = 0.143$ ,  $\varepsilon_y = 2.83$ ,  $\varepsilon_z = 1.0$ .

For uniform distribution of droplet axes orientation over the angle  $\varphi$ , we can write:

$$\overline{\cos^4(\alpha - \varphi_s - \varphi_d)} = \frac{3}{8} + \frac{1}{2} \cos(2(\alpha - \varphi_s)) \text{sinc}(2\varphi_m) + \frac{1}{8} \cos(4(\alpha - \varphi_s)) \text{sinc}(4\varphi_m), \quad (17)$$

$$\overline{\sin^4(\alpha - \varphi_s - \varphi_d)} = \frac{3}{8} - \frac{1}{2} \cos(2(\alpha - \varphi_s)) \text{sinc}(2\varphi_m) + \frac{1}{8} \cos(4(\alpha - \varphi_s)) \text{sinc}(4\varphi_m), \quad (18)$$

$$\overline{\sin^2(2(\alpha - \varphi_s - \varphi_d))} = \frac{1}{2} (1 - \cos(4(\alpha - \varphi_s)) \text{sinc}(4\varphi_m)), \quad (19)$$



**Fig. 6.** The dependences of coherent transmittance  $T_{np}^c$  of PDLC film (a, c) and polarization degree  $P_c$  (b, d) of the forward-transmitted light on the wavelength  $\lambda$  of incident unpolarized light for the polymer refractive indices  $n_p$  equaled to the ordinary  $n_{\perp}$  (a, b) and extraordinary  $n_{\parallel}$  (c, d) refractive indices of 5CB at  $\lambda = 0.62, 0.5$  and  $0.45 \mu\text{m}$ . Monodisperse droplets with the monodomain LC structure and oriented optical axes (the film order parameter  $S_{2f} = 1$ ). The stretching ratio of film is  $p=2$ , the droplet lateral semiaxis is  $a=0.7 \mu\text{m}$ , the film thickness is  $l=32 \mu\text{m}$ , the volume filling factor of PDLC film is  $c_v = 0.143$ , the anisotropy parameters of LC droplets are  $\epsilon_y = b/a = 2.83$ ,  $\epsilon_z = c/a = 1.0$  (where  $b$  is the droplet semiaxis along the stretching direction,  $a$  is the droplet semiaxis along the normal to the film,  $c$  is the lateral semiaxis in the film plane).

$$\overline{\sin 2(\alpha - \varphi_s - \varphi_d)} = \sin(2(\alpha - \varphi_s)) \text{sinc}(2\varphi_m), \quad (20)$$

$$\overline{\sin(4(\alpha - \varphi_s - \varphi_d))} = \sin(4(\alpha - \varphi_s)) \text{sinc}(4\varphi_m), \quad (21)$$

where  $\varphi_m$  is the maximal deviation angle of the droplet axes from the stretching axis,  $\text{sinc}(x) = \sin(x)/x$ .

### 2.3. Transmittance and polarization ability as functions of the angular aperture of the optical system

To analyze the transmittance and polarizing ability of the PDLC layer taking into account the field of view  $\theta_{fov}$  (FOV) angle, it is necessary to integrate the intensity of scattered light over the polar  $\theta_s$  and azimuthal  $\varphi_s$  scattering angles from  $0$  to  $\theta_{fov}/2$  and from  $0$  to  $2\pi$ , respectively.

Under normal illumination by unpolarized light, the coefficient of incoherent (diffuse) transmission  $T_{np}^{inc}(\theta_{fov})$  and the integral polarizing ability  $P_{inc}(\theta_{fov})$  of layer for the incoherently scattered light can be determined by:

$$T_{np}^{inc}(\theta_{fov}) = \frac{1}{2} (T_{\parallel}^{inc}(\theta_{fov}) + T_{\perp}^{inc}(\theta_{fov})), \quad (22)$$

$$P_{inc}(\theta_{fov}) = \frac{T_{\perp}^{inc}(\theta_{fov}) - T_{\parallel}^{inc}(\theta_{fov})}{T_{\parallel}^{inc}(\theta_{fov}) + T_{\perp}^{inc}(\theta_{fov})}, \quad (23)$$

$$\begin{aligned} T_{\parallel, \perp}^{inc}(\theta_{fov}) &= \frac{1}{C_{np}} \int_0^{2\pi} d\varphi_s \int_0^{\theta_{fov}/2} (I_{vv}^{inc}(\theta_s, \varphi_s) + I_{vh}^{inc}(\theta_s, \varphi_s)) \Big|_{\alpha=0, \pi/2} \sin \theta_s d\theta_s, \end{aligned} \quad (24)$$

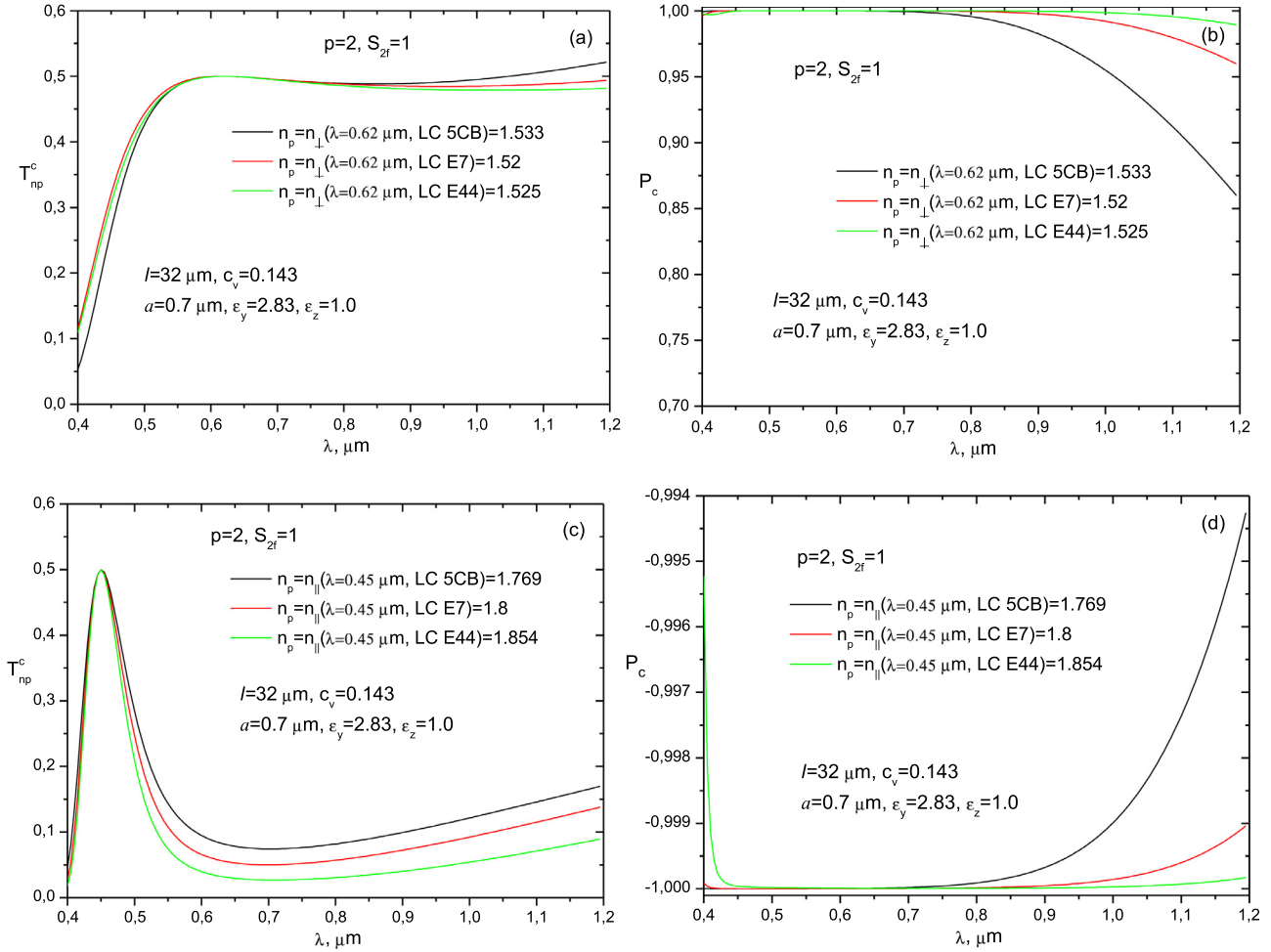
$$\begin{aligned} C_{np} &= \int_0^{2\pi} d\varphi_s \int_0^{\pi} \{ (I_{vv}^{inc}(\theta_s, \varphi_s) + I_{vh}^{inc}(\theta_s, \varphi_s)) \Big|_{\alpha=0} + (I_{vv}^{inc}(\theta_s, \varphi_s) \\ &\quad + I_{vh}^{inc}(\theta_s, \varphi_s)) \Big|_{\alpha=\pi/2} \} \sin \theta_s d\theta_s, \end{aligned} \quad (25)$$

where  $T_{\parallel}^{inc}(\theta_{fov})$  and  $T_{\perp}^{inc}(\theta_{fov})$  are the parallel and orthogonal components of the incoherent transmittance of the layer.

Taking into account the coherent component, the total transmittance  $T_{np}$  of the layer and the polarization degree  $P_{fov}$  are follows:

$$T_{np}(\theta_{fov}) = T_{np}^c + T_{np}^{inc}(\theta_{fov}) = T_{\parallel}(\theta_{fov}) + T_{\perp}(\theta_{fov}), \quad (26)$$

$$P_{fov}(\theta_{fov}) = \frac{T_{\perp}(\theta_{fov}) - T_{\parallel}(\theta_{fov})}{T_{\parallel}(\theta_{fov}) + T_{\perp}(\theta_{fov})}, \quad (27)$$



**Fig. 7.** The dependences of coherent transmittance  $T_{np}^c$  of PDLC film (a, c) and polarization degree  $P_c$  (b, d) of the forward-transmitted light on the wavelength  $\lambda$  of incident unpolarized light for the polymer refractive indices  $n_p$  equaled to the ordinary  $n_{\perp}$  (a, b) and extraordinary  $n_{\parallel}$  (c, d) refractive indices of different LC (5CB, E7, E44) at  $\lambda = 0.62 \mu\text{m}$  (a, b) and  $\lambda = 0.45 \mu\text{m}$  (c, d). Monodisperse droplets with the monodomain LC structure and oriented optical axes ( $S_{2f} = 1$ ).  $p=2$ ,  $a=0.7 \mu\text{m}$ ,  $l=32 \mu\text{m}$ ,  $c_v = 0.143$ ,  $\varepsilon_y = 2.83$ ,  $\varepsilon_z = 1.0$ .

$$T_{\parallel,\perp}(\theta_{fov}) = \frac{1}{2} (T_{\parallel,\perp}^c + T_{\parallel,\perp}^{inc}(\theta_{fov})). \quad (28)$$

The normalizing factor  $C_{np}$  is determined as:

$$C_{np} = C \frac{3}{4} \frac{c_v l (a^2)}{\varepsilon_y \varepsilon_z (a^3)} (\langle Q_{\parallel} \rangle + \langle Q_{\perp} \rangle), \quad (29)$$

$$\langle Q_{\parallel,\perp} \rangle = \left( \langle Q_e \rangle \frac{1 \pm S_{2f}}{2} + \langle Q_o \rangle \frac{1 \mp S_{2f}}{2} \right), \quad (30)$$

$$\langle Q_{\parallel} \rangle + \langle Q_{\perp} \rangle \equiv \langle Q_e \rangle + \langle Q_o \rangle, \quad (31)$$

where  $\langle Q_{\parallel} \rangle$  and  $\langle Q_{\perp} \rangle$  are the average values of extinction efficiency factor of LC droplets for the incident light polarizations parallel and orthogonal to the stretching axis;  $\langle Q_e \rangle$  and  $\langle Q_o \rangle$  are determined by Eq. (7).

### 3. Simulation results

Here the results of numerical simulation of the polarization degree and the transmittance are presented. They have been obtained by the formulas from the previous section.

The relaxation method of minimizing the free energy volume density was applied to simulate the LC director configuration (a distribution of local optical axes) inside droplets. The anomalous

diffraction approximation was used to determine the elements of the amplitude scattering matrix  $S_j(\theta_s, \varphi_s)$  ( $j=1,2,3,4$ ) [14,19,22,26–28]. The calculations were carried out for the monodisperse LC droplets in a polymer film (matrix).

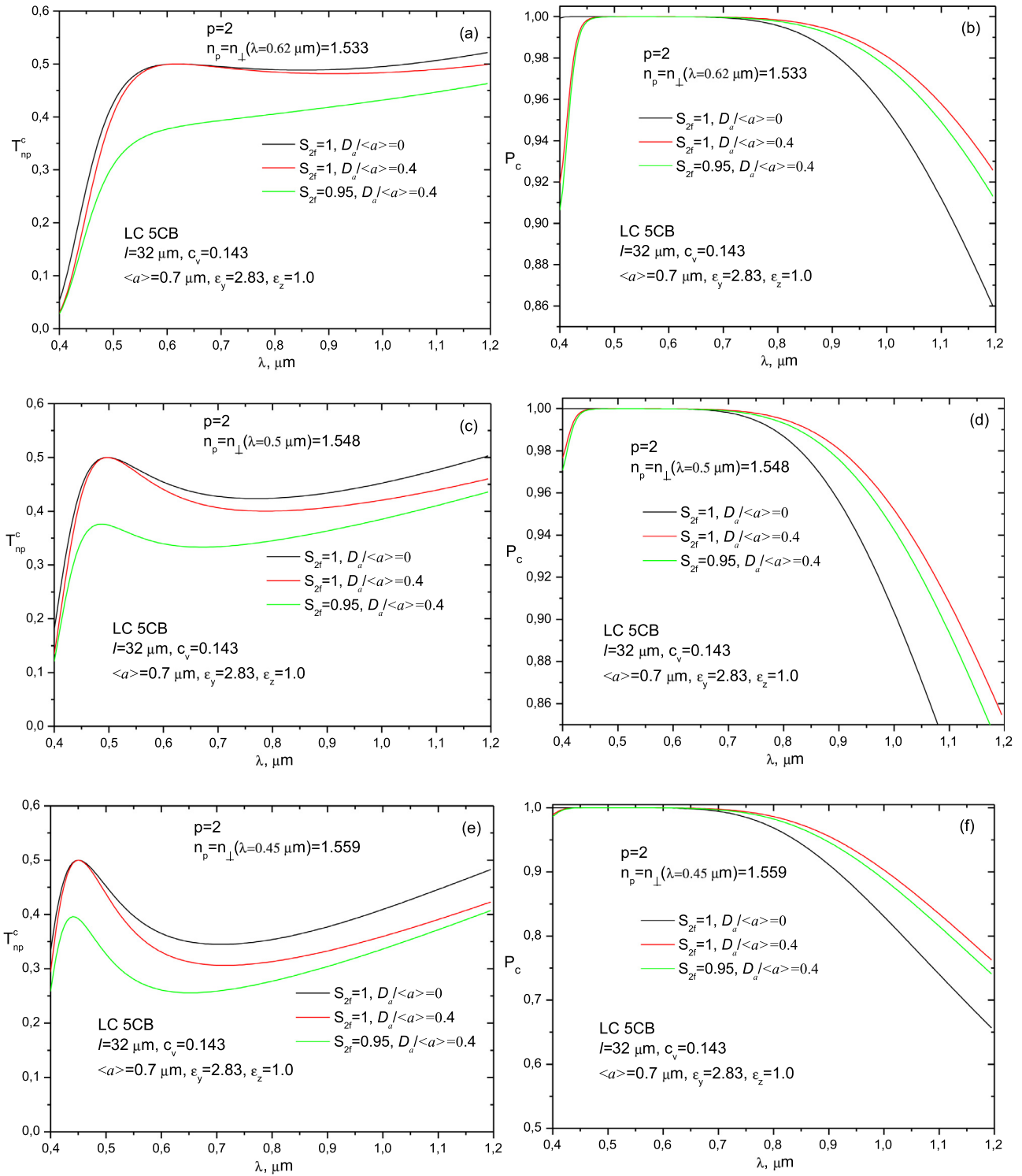
The dependences of the ordinary  $n_{\perp}$  and extraordinary  $n_{\parallel}$  refractive indices of LC on the wavelength  $\lambda$  of incident light were described by Cauchy formulas:

$$n_{\perp,\parallel} = A_{\perp,\parallel} + \frac{B_{\perp,\parallel}}{\lambda^2} + \frac{C_{\perp,\parallel}}{\lambda^4}, \quad (32)$$

where  $A_{\perp,\parallel}$ ,  $B_{\perp,\parallel}$ ,  $C_{\perp,\parallel}$  are the coefficients determined by the kind of LC used [29].

#### 3.1. Spectral dependences of the coherent transmittance and the polarization degree of the forward-transmitted light for the stretched PDLC film

Fig. 3 illustrates the simulation data of spectral dependences of the coherent transmittance  $T_{np}^c(\lambda)$  and the polarizing ability  $P_c(\lambda)$  of PDLC film for the forward-transmitted light at two stretching factors of the film ( $p=1.16, 1.41$ ). PDLC films with bipolar, radial and monodomain  $y$ -configurations of LC inside the droplets are considered. The refractive index  $n_p$  of polymer matrix was chosen equaled to the ordinary refractive index  $n_{\perp}$  of LC at  $\lambda=0.62 \mu\text{m}$  ( $n_p = n_{\perp} = 1.533$ ); the extraordinary refractive index is  $n_{\parallel} = 1.708$ ;



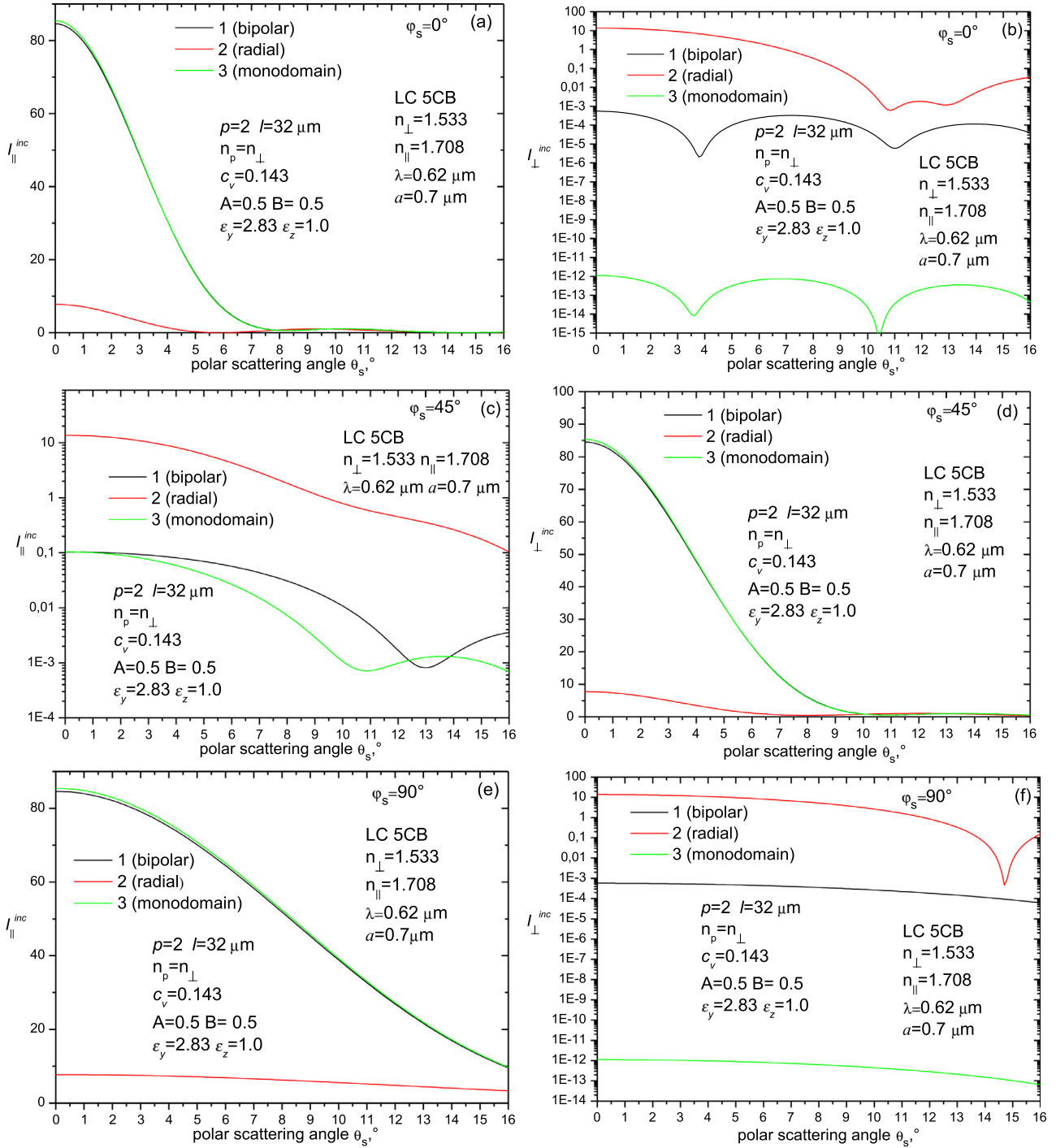
**Fig. 8.** The spectral dependences of coherent transmittance  $T_{np}^c$  of PDLC film (a, c, e) illuminated by unpolarized incident light and the polarization degree  $P_c$  (b, d, f) of the forward-transmitted light in condition of equality of the polymer refractive index  $n_p$  and the ordinary refractive index  $n_{\perp}$  of 5CB at  $\lambda = 0.62, 0.5$  and  $0.45 \mu\text{m}$ . The LC structure inside the droplets is monodomain. The stretching ratio of film is  $p=2$ . The average size of droplet lateral semiaxis  $a$  is  $\langle a \rangle = 0.7 \mu\text{m}$ . The anisotropy parameters of droplets are  $\epsilon_y = 2.83$ , and  $\epsilon_z = 1.0$ . The order parameters of film are  $S_{2f} = 1$  and  $0.95$ . Gamma-distribution of droplet sizes. The variation coefficients are  $D_a/\langle a \rangle = 0$  and  $0.4$ .

the layer thickness before stretching was  $l_0 = 45 \mu\text{m}$ . The calculations were carried out for the monodisperse droplets totally oriented in the stretching direction: the variation coefficient [22] of droplet semiaxes  $a$  is  $D_a/\langle a \rangle = 0$ ; the order parameter of film is  $S_{2f} = 1$ . The rest parameters are shown in the legends of figures. The selected sizes of droplets semiaxis  $a = 0.93, 0.84, 0.71 \mu\text{m}$  cor-

respond to the values at which the  $T_{np}^c$  and  $P_c$  are close to the limiting ones:  $T_{np}^c(\lambda) \rightarrow 0.5, P_c(\lambda) \rightarrow \pm 1.0$ , in the wide wavelength range.

The stretching of PDLC films containing the droplets with monodomain and bipolar configurations allows one to polarize effectively the light in the wavelength range from  $0.55$  to  $0.8 \mu\text{m}$





**Fig. 9.** The dependences of parallel (to the stretching axis)  $I_{||}^{inc}(\theta_s)$  (a, c, e) and orthogonal  $I_{\perp}^{inc}(\theta_s)$  (b, d, f) components of scattered light intensity on the polar scattering angle  $\theta_s$  at different azimuthal scattering angles  $\varphi_s$ . PDLC film was double-stretched ( $p=2$ ) at homogeneous (1, 2) and inhomogeneous (3) surface anchoring.  $n_p = n_{\perp} = 1.533$  at  $\lambda = 0.62 \mu\text{m}$ .

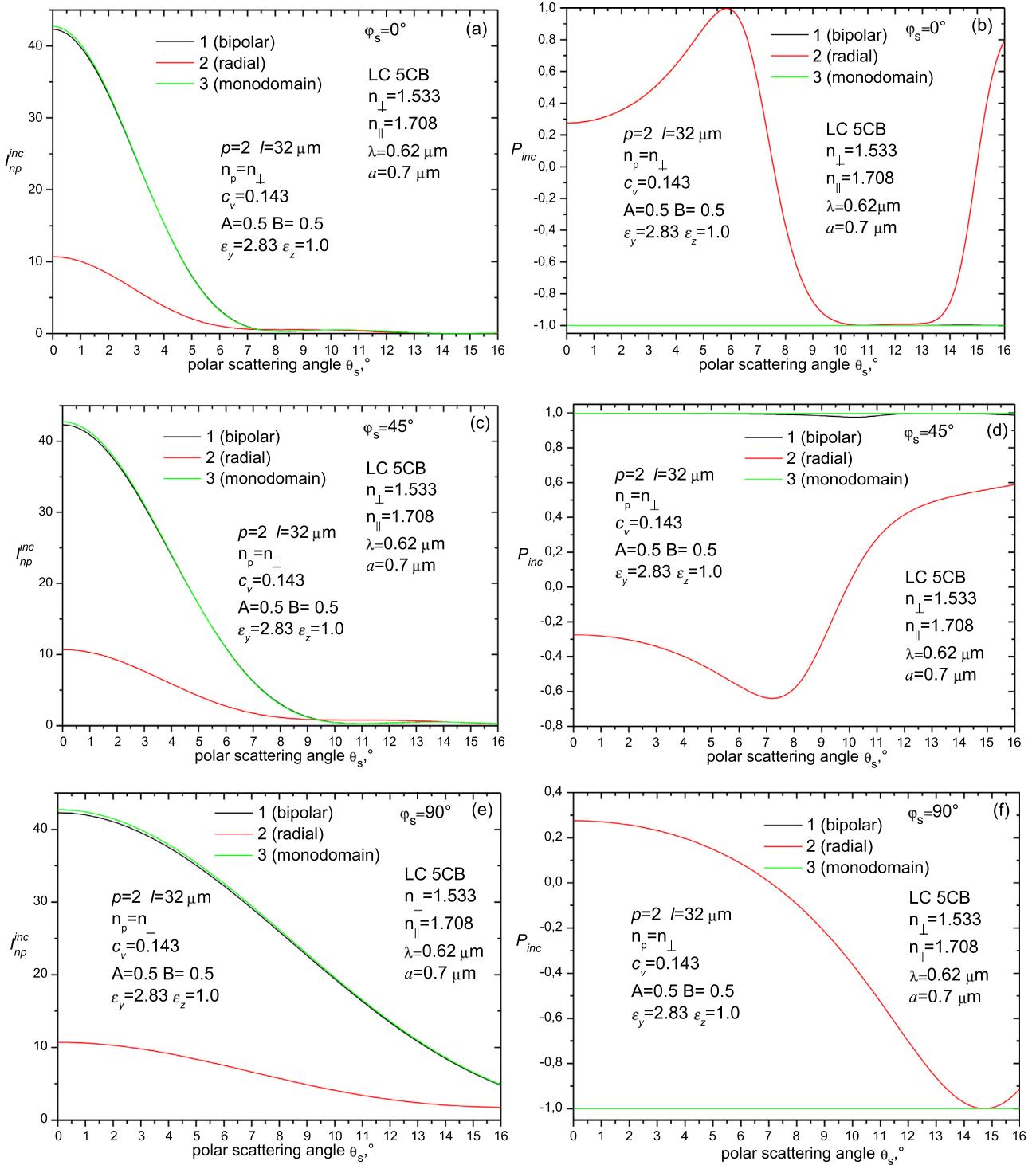
(polarization degree  $P_c > 0.99$  and transmittance  $T_{np}^c > 0.47$ ). As calculations show, varying the refractive index of polymer  $n_p$  (upward at the condition  $n_p = n_{\perp}(\lambda)$  or  $n_p = n_{||}(\lambda)$ ) and the  $a$  droplet size, it is possible to shift into the range of smaller wavelength  $\lambda < 0.55 \mu\text{m}$  with  $T_{np}^c(\lambda) \approx 0.5$  and  $P_c(\lambda) \approx \pm 1.0$ .

The high polarization degree of forward-transmitted light ( $P_c > 0.97$ ) in the spectral range from 0.45 to 0.7  $\mu\text{m}$  (Fig. 3 (b,d)) can be achieved in the PDLC films containing LC droplets with the monodomain and bipolar configurations at  $n_p = n_{\perp}$ . The

$T_{np}^c$  transmittances of films with bipolar configuration are smaller than that of films with the monodomain internal structure.

The films with the radial droplet structure and the homogeneous surface anchoring do not allow effectively polarize the forward-transmitted light.

Note, the positive and negative values of  $P_c$  mean that the forward-transmitted light is polarized orthogonally and parallel to the direction of film stretching, respectively. A polarization sign is determined by which component (polarized orthogonally or



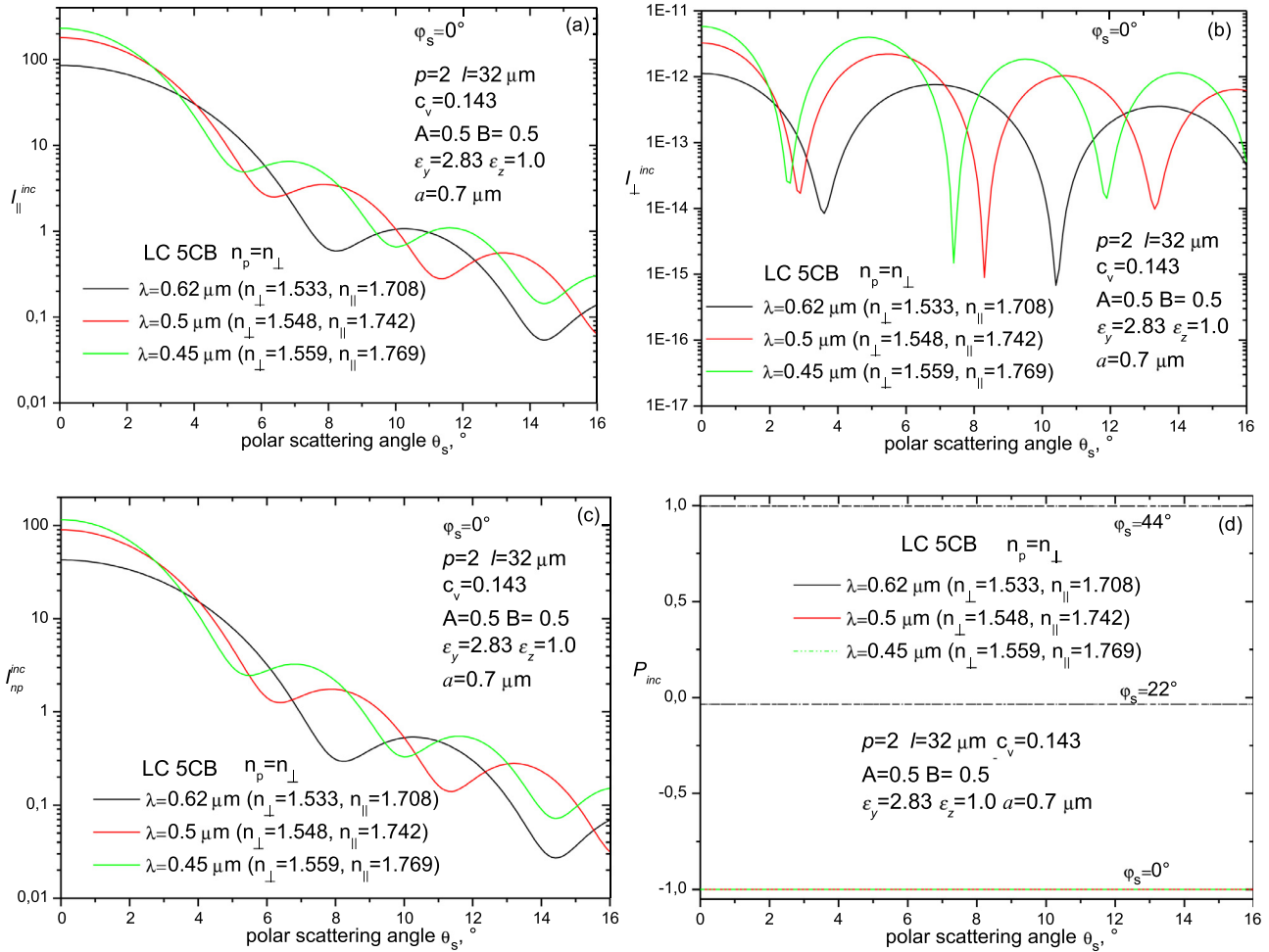
**Fig. 10.** The dependences of intensity  $I_{np}^{inc}(\theta_s)$  (a, c, e) and polarization degree  $P_{inc}(\theta_s)$  (b, d, f) of scattered light on the polar scattering angle  $\theta_s$  at different values of azimuthal scattering angle  $\varphi_s$ . PDLC film was double-stretched ( $p=2$ ) at homogeneous (1, 2) and inhomogeneous (3) surface anchoring.  $n_p = n_\perp = 1.533$  at  $\lambda = 0.62 \mu\text{m}$ .

parallel to the stretching axis) is less scattered. For the monodomain LC structure the orthogonal component of transmittance is not scattered at wavelength  $\lambda$ , if  $n_p = n_\perp(\lambda)$ . At that, if the parallel component is strongly scattered, the polarization degree of the forward-transmitted light  $P_c \rightarrow +1$  (forward-transmitted light is linearly polarized orthogonally to the stretching axis). For  $n_p = n_\parallel(\lambda)$  the parallel component is not scattered. And  $P_c \rightarrow -1$  (forward-transmitted light is linearly polarized parallel to the stretching axis) if the orthogonal component is strongly scattered.

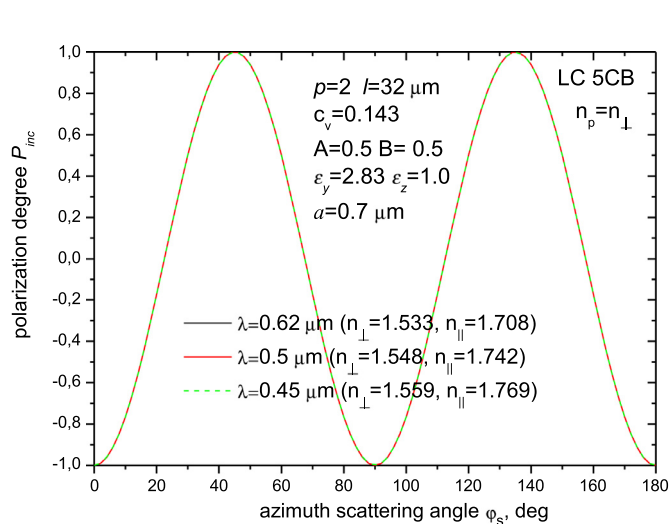
### 3.2. Monodomain structure

It is convenient to consider the transmittance and polarization by varying the  $a$ -values in the conditions of: (i) the equality of the refractive index  $n_p$  of polymer to the ordinary refractive index  $n_\perp$  of LC at the selected wavelength  $\lambda$  ( $n_p = n_\perp(\lambda)$ ) or (ii) the equality of  $n_p$  to the extraordinary refractive index  $n_\parallel$  of LC ( $n_p = n_\parallel(\lambda)$ ).

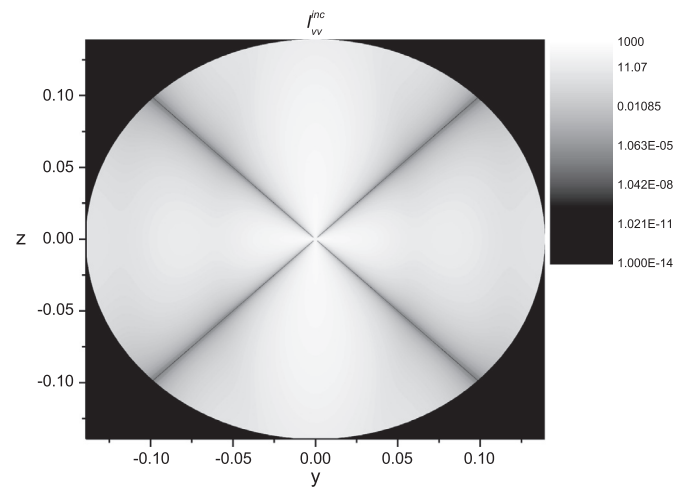
Figs. 4 and 5 show the calculation data for 5CB liquid crystal in the red, green and blue spectral ranges ( $\lambda = 0.62, 0.5$  and



**Fig. 11.** Angular distribution of the parallel  $I_{\parallel}^{inc}(\theta_s)$  (a) and orthogonal  $I_{\perp}^{inc}(\theta_s)$  (b) to the stretching axis intensity components, the intensity  $I_{np}^{inc}(\theta_s)$  (c), and the polarization degree  $P_{inc}(\theta_s)$  (d) of scattered light for the refractive index  $n_p$  of polymer matrix equal to the ordinary refractive index  $n_{\perp}$  of 5CB at  $\lambda = 0.62, 0.5, 0.45 \mu\text{m}$ . The stretching ratio of film is  $p=2$ . The structure within LC droplets is monodomain.  $a=0.7 \mu\text{m}$ .



**Fig. 12.** Dependences of the polarization degree  $P_{inc}$  of scattered light on the azimuthal scattering angle  $\varphi_s$  in the condition of the equality of the refractive index  $n_p$  of polymer matrix and ordinary refractive index  $n_{\perp}$  of 5CB at  $\lambda = 0.62, 0.5, 0.45 \mu\text{m}$ . The stretching ratio of film is  $p=2$ . The structure within LC droplets is monodomain.  $a=0.7 \mu\text{m}$ .



**Fig. 13.** Distribution of the  $I_{vv}^{inc}$ -component of incoherently scattered light.

0.45  $\mu\text{m}$ ). As can be seen, if  $n_p = n_{\perp}(\lambda)$  or  $n_p = n_{\parallel}(\lambda)$ , the maximum  $T_{np}^c \approx 0.5$  is realized at these  $\lambda$  for all considered sizes of a semiaxis (Fig. 4(a,c,e) and Fig. 5(a,c,e)). The values of the refractive index  $n_p$  of polymer and a semiaxis determine the wavelength

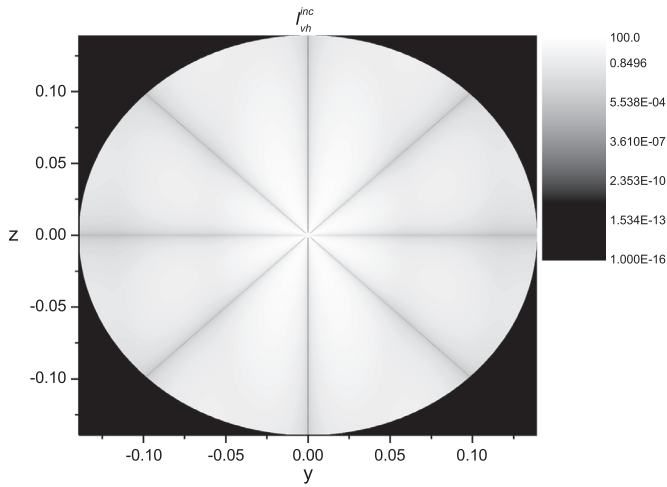


Fig. 14. Distribution of the  $I_{vh}^{inc}$ -component of incoherently scattered light.

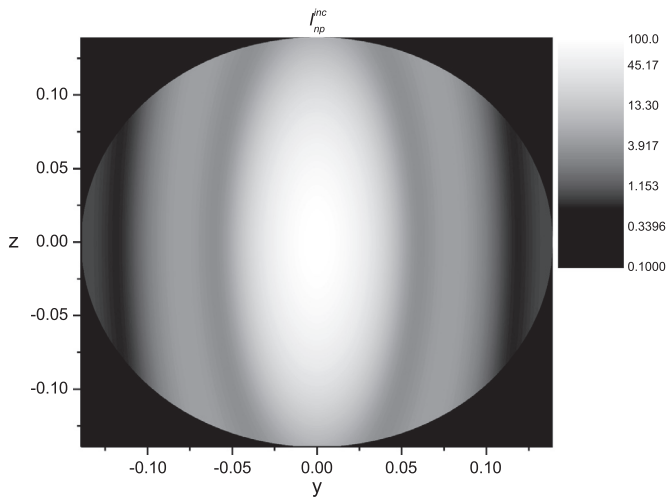


Fig. 15. Distribution of the  $I_{np}^{inc}$  intensity of incoherently scattered light.

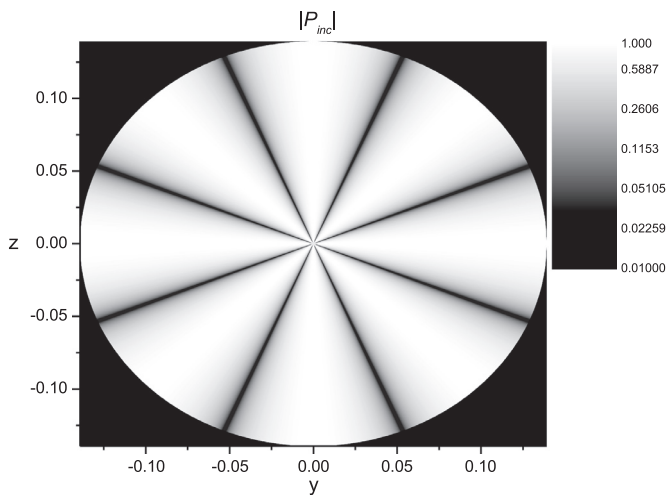


Fig. 16. Distribution of the  $|P_{inc}|$  for incoherently scattered light.

range where the transmittance  $T_{np}^c$  of the film and polarization degree  $P_c$  of light reach simultaneously the values close to the limiting ones (0.5 and  $\pm 1.0$ ), respectively. For  $a = 0.7 \mu\text{m}$  the polarization degree of forward-transmitted light has the values close to the maximal one ( $P_c \approx \pm 1$ ) in the wide enough spectral range (Fig. 4(b,d,f) and Fig. 5(b,d,f)). For the film with the parameters  $l = 32 \mu\text{m}$ ,  $c_v = 0.143$ ,  $\varepsilon_y = 2.83$ ,  $\varepsilon_z = 1.0$  containing the monodisperse oriented droplets, the value  $a = 0.7 \mu\text{m}$  allows realizing the spectral characteristics close to the limiting ones.

Fig. 6 illustrates the  $T_{np}^c(\lambda)$  and  $P_c(\lambda)$  dependences for the film with 5CB LC droplets at  $n_p = n_{\perp\parallel}$  ( $\lambda = 0.62, 0.5, 0.45 \mu\text{m}$ ). As can see, an effective polarization of visible light in the wavelength range from blue to red with significant coherent transmission coefficient can be achieved by changing the refractive index  $n_p$  of polymer from  $n_p = n_{\perp}$  to  $n_p = n_{\parallel}$ .

The  $T_{np}^c(\lambda)$  and  $P_c(\lambda)$  dependences for PDLC films based on the different liquid crystals (5CB, E7, E44) are shown in Fig. 7. An increasing of the optical anisotropy of LC allows widening the wavelength range in which the polarizing ability of the film will be  $P \approx \pm 1.0$  (Fig. 7(b), 7(d)).

The results shown in Figs. 6 and 7 imply that the mechanically stretched PDLC films in which the droplet-polymer interface is modified by surfactants can be used as: (i) the wide-band polarizers of forward-transmitted light with the high transmittance ( $T_{np}^c \approx 0.5$ ) and the polarizing ability ( $P_c(\lambda) \approx \pm 1$ ) in the wavelength range  $0.6 \mu\text{m} < \lambda < 0.7 \mu\text{m}$ ; (ii) the polarizers with the transmittance  $T_{np}^c \approx 0.5$  and the polarization degree  $P_c \approx -1.0$  at  $\lambda \approx 0.5 \mu\text{m}$  (Fig. 7(c), 7(d)), the polarizers at  $\lambda \approx 0.45 \mu\text{m}$  and at others wavelengths of visible light. The values  $P_c = 1$  and  $P_c = -1$  in the Figs. 4–7 mean that the forward-transmitted light is linearly polarized orthogonally and parallel to the film stretching direction, respectively. As was mentioned above, this is determined by which of the transmittance components is not scattered.

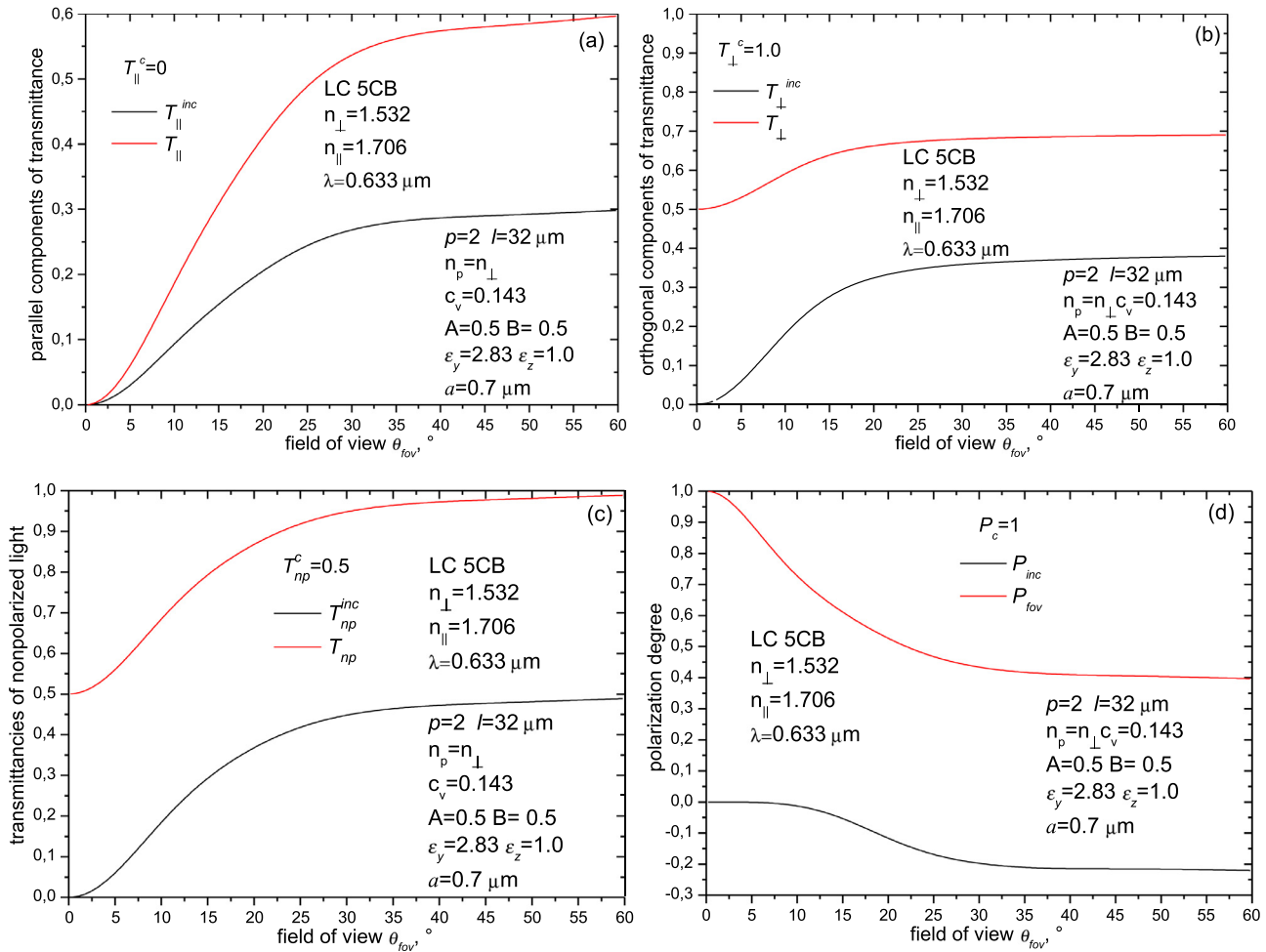
The near to limiting values  $T_{np}^c \approx 0.5$  and  $P_c \approx 1.0$  (or  $P_c \approx -1$ ) depend on a droplet polydispersity as well as orientation of their optical axes under film stretching (Fig. 8). Increasing the droplet polydispersity (described by the variation coefficient  $Da/\langle a \rangle$ ) and decreasing the order parameter  $S_{2f}$  of film result in reduce of its coherent transmittance  $T_{np}^c$  (Fig. 8(a, c, e)) and change of the spectral dependence of the polarization degree  $P_c$  of forward-transmitted light (Fig. 8(b, d, f)).

The numerical analysis showed that the narrowing of spectral range in which the film transmittance is close to the limiting values ( $T_{np}^c \approx 0.5$ ) is most sensitive to a variation of film order parameter  $S_{2f}$  (i.e. to the difference of  $S_{2f}$  values from 1 corresponding to a perfect orientation of droplet optical axes under mechanical stretching). The polarization degree  $P_c$  of the forward-transmitted light is most sensitive to a polydispersity of LC droplets.

### 3.3. Small-angle distribution of the intensity and polarization degree of the scattered light. Droplets with homogeneous and inhomogeneous surface anchoring

Figs. 9 and 10 illustrate the dependences of the  $I_{\parallel}^{inc-}$ ,  $I_{\perp}^{inc-}$  components of scattered light, and the polarization degree  $P_{inc}$  of scattered light on the polar  $\theta_s$  and azimuthal  $\varphi_s$  scattering angles. The simulation was carried out at double stretching of PDLC films ( $p = 2$ ) with the homogeneous surface anchoring for the bipolar and radial LC configurations inside the droplets and with the inhomogeneous anchoring for the monodomain structure. The refractive index of polymer  $n_p = n_{\perp} = 1.533$  at  $\lambda = 0.62 \mu\text{m}$ . Other parameters of the simulations are indicated in the legends of figures.

As can see in Figs. 9 (a, b) and 9 (e, f), at  $\varphi_s = 0^\circ, 90^\circ$  a high anisotropy of light scattering is observed for both the bipolar and monodomain droplet structures: the ratios  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) \approx 10^3$



**Fig. 17.** The dependences of the transmittance for parallel (a) and orthogonal (b) components of scattered light, the transmittance for unpolarized incident light (c), and the polarizing degree (d) on the field of view angle  $\theta_{fov}$ . The structure within LC droplets is monodomain. The stretching ratio of the film is  $p=2$ .  $n_p = n_{\perp} = 1.532$ . The wavelength of incident light  $\lambda = 0.633 \mu\text{m}$ .  $a = 0.7 \mu\text{m}$ .

for bipolar structure and  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) \approx 10^{12}$  for monodomain configuration. At  $\varphi_s = 45^\circ$  (Fig. 9 (c, d)),  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) \approx 10^{-4}$  both for the bipolar and monodomain droplet structures. For the PDLC films containing the droplets with radial structure, the ratios  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) \approx 1/2$  at  $\varphi_s = 0^\circ$ ;  $90^\circ$  and  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) \approx 2$  at  $\varphi_s = 45^\circ$ .

The intensity  $I_{np}^{inc}(\theta_s, \varphi_s)$  (Fig. 10 (a, c, e)) and the polarization degree  $P_{inc}$  of incoherently scattered light (Fig. 10 (b, d, f)) practically coincide with  $I_{np}^{inc}(\theta_s, \varphi_s)$  and  $P_{inc}$ , respectively, for the double-stretched PDLC films with bipolar and monodomain structures.

The polarization degree  $P_{inc}$  of incoherently scattered light does not practically depend on the polar scattering angle  $\theta_s$  (Fig. 10 (b, d, f)) for bipolar and monodomain structures. It is caused by the equality  $n_p = n_{\perp}$  when one of the components (parallel,  $I_{\parallel}^{inc}(\theta_s)$ , or orthogonal,  $I_{\perp}^{inc}(\theta_s)$ ) exceeds significantly another one (by 4–12 orders and more, Fig. 9). At  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) \rightarrow \infty$ , the value  $P_{inc}(\theta_s) \rightarrow -1$ . At  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) \rightarrow 0$ , the value  $P_{inc}(\theta_s) \rightarrow +1$ . Fig. 10 (b, d, f) shows the polarization degree  $P_{inc} = -1$  at  $\varphi_s = 0^\circ$ ,  $90^\circ$  and  $P_{inc} = +1$  for  $\varphi_s = 45^\circ$  – for bipolar and monodomain structures. It should be emphasized that the polarization degree  $P_{inc}(\theta_s)$  of diffusely scattered light for stretched PDLC film containing radial droplets (Fig. 10 (b, f)) can reach the limiting values ( $\pm 1$ ) at the azimuthal  $\varphi_s = 0^\circ$ ;  $90^\circ$  and polar  $\theta_s \approx 6^\circ$ ;  $12^\circ$ ;  $15^\circ$  etc. scattering angles.

### 3.4. Small-angle distribution of the intensity and polarization degree of the scattered light. Droplets with monodomain structure: refractive index of polymer is equal to the ordinary refractive index of liquid crystal

Figs. 11 and 12 display the parallel  $I_{\parallel}^{inc}$  and orthogonal  $I_{\perp}^{inc}$  (to the stretching axis) components of scattered light intensity, the intensity  $I_{np}^{inc}$  of scattered light for unpolarized incident light and the polarization degree  $P_{inc}$  of incoherently scattered light. The calculations were performed for a double-stretched PDLC film with monodomain droplet structure forming under modification of surface anchoring for initially (before stretching) spherical droplets with bipolar and radial configurations. The refractive index  $n_p$  of polymer matrix is equal to the ordinary refractive index  $n_{\perp}$  of 5CB at  $\lambda = 0.62, 0.5, 0.45 \mu\text{m}$ . The following parameters were used in the simulation: the film thickness is  $l = 32 \mu\text{m}$ ; the stretching ratio is  $p = 2$  (the film thickness before stretching was  $l_0 = 45 \mu\text{m}$ ); the volume filling factor of film is  $c_v = 0.143$ ; the anisotropy parameters of droplets are  $\epsilon_y = 2.83$ ,  $\epsilon_z = 1.0$  ( $p = 2$ ); the droplet semiaxis  $a = 0.7 \mu\text{m}$ .

Fig. 11 shows that a high asymmetry of scattered light reveals for all considered wavelengths. The ratio  $I_{\parallel}^{inc}(\theta_s)/I_{\perp}^{inc}(\theta_s) > 10^{12}$  at  $\varphi_s = 0^\circ$  (Fig. 11 (a, b)).

It is worth noting, that at the considered conditions ( $n_p = n_{\perp}$ ), the polarization degree  $P_{inc}$  is the same at different wavelengths

and does not depend on the polar scattering angle  $\theta_s$ . At that  $P_{inc}$  depends on the azimuthal angle (Fig. 11(d), Fig. 12).

Figs. 13–16 demonstrate the angular distributions of intensity components and the polarization degree of incoherently scattered light for the stretched PDLC film containing monodisperse droplets with monodomain director configuration and with totally oriented structure of their  $N_j$  optical axes. The dependences of  $I_{vv,vh}^{inc}(\theta_s, \varphi_s)$ ,  $I_{np}^{inc}(\theta_s, \varphi_s)$  and  $P_{inc}(\theta_s, \varphi_s)$  were calculated for LC 5CB according to the formulas of Section 2.2 at the following parameters:  $\theta_{fov} = 16^\circ$ ,  $p=2$ ,  $l=32 \mu\text{m}$ ,  $c_v = 0.143$ ,  $a = 1.4 \mu\text{m}$ ,  $\varepsilon_y = 2.83$ ,  $\varepsilon_z = 1.0$ ,  $A=B=0.5$ ,  $C = 1$ . The horizontal and vertical axes show the values of  $y = \sin\theta_s \cos\varphi_s$  and  $z = \sin\theta_s \sin\varphi_s$  within  $-8^\circ \leq \theta_s \leq 8^\circ$ ,  $0^\circ \leq \varphi_s \leq 360^\circ$ .

### 3.5. Dependence of the transmittance and polarizing ability of the film with the monodomain droplet structure on the field of view

The dependences of the  $T_{\parallel,\perp}^{inc}$ ,  $T_{\parallel,\perp}^{inc}$ ,  $T_{np}^{inc}$  transmittances and polarizing abilities  $P_{fov}^{inc}$ ,  $P_{fov}$  of PDLC film on the field of view  $\theta_{fov}$  (angular aperture of the optical system recording the intensity of light scattered by the film) are shown in Fig. 17.

The simulations were carried out for the film containing a monodisperse oriented LC droplets with monodomain internal structure. The film parameters are indicated in the legends. At such parameters, the forward-transmitted light is entirely polarized ( $P_{fov} = 1$  at  $\theta_{fov} = 0$ ), and the coherent transmittance of film is  $T_{np}^c = 0.5$ .

The obtained data show that almost all incoherently scattered light is recorded at  $\theta_{fov} = 60^\circ$ ; the total transmittance is  $T_{np}(\theta_{fov} = 60^\circ) \approx 1$ . The incoherent transmission coefficient for unpolarized incident light is  $T_{np}^{inc} \approx 0.5$  Fig. 17(c)). The forward-transmitted light or light transmitted in forward hemisphere, i.e.  $T^c + T^{inc}$  (see Eqs. (26)–(28)) is partially polarized with the polarization degree  $P_{fov} \approx 0.4$  (Fig. 17(d)). The polarization degree of diffusely scattered light is about  $\sim 0.22$  that corresponds to the more stronger scattering of parallel intensity component as compared with the orthogonal one.

The polarization degree of transmitted light has the values exceeding 0.95 (Fig. 17(d)) at  $\theta_{fov} < 3$ . Under such conditions the stretched PDLC film with monodomain and bipolar droplet director configuration effectively polarizes light and has the transmittance  $\sim 0.5$ .

## 4. Conclusion

A high polarization degree (more than 0.97) can be achieved for the forward-transmitted light in the wide wavelength range (from 0.45 to 0.7  $\mu\text{m}$ ) both for PDLC films with monodomain and bipolar LC droplet structures and for films with inhomogeneous surface anchoring of “tangential-normal” type. A coherent transmittance of the films with bipolar droplet configuration and inhomogeneous “tangential-normal” anchoring is smaller than that of the films with monodomain internal structure. The films with homogeneous surface anchoring and radial LC droplet structure do not allow polarizing effectively the forward-transmitted light.

The angular distributions of intensity of light scattered by the PDLC films with bipolar and monodomain internal droplet structures at the stretching ratio equaled to 2 are practically coincided. At that, the polarization degrees are the same at the different wavelengths and do not depend on the polar scattering angle when the refractive index of polymer matrix is equal to the ordinary refractive index of LC.

The stretched PDLC films with monodomain and bipolar droplet structures polarize effectively light for the small FOVs ( $< 3^\circ$ ). The

polarization degree can exceed 0.95 at the transmittance close to 0.5.

The developed optical-mechanical model to analyze the coherent transmittance, angular and spectral characteristics of light scattered by the stretched PDLC film allows solving the inverse problem: to determine the structural parameters of the film (the filling factor and thickness, sizes and anisometry parameters of the droplets, refractive indices of the polymer matrix and LC) at which its transmittance and polarizing ability simultaneously reach the values close to the limit ones (0.5 and 1.0, respectively).

The obtained results can be used to develop the polarizers of transmitted light based on the stretched PDLC films with the surfactant-induced modification of surface anchoring, operating in the light-scattering mode and possessing by a high transmittance and polarizing ability.

## Acknowledgments

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