



Structure and properties of phases in the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system. The $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ phase diagram



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ABSTRACT

The phase diagram of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system is revisited to clarify ambiguity/disagreement in previously reported data. Ternary Cu_3SbSe_3 and CuSbSe_2 compounds were obtained. In order to confirm that the phases have been identified correctly, crystal structures were solved, and the energy band gaps measured. For the sample containing 75 mol% Sb_2Se_3 and 25 mol% $\text{Cu}_{1.995}\text{Se}$ the temperature range of the stability of the high-temperature CuSb_3Se_5 phase was determined for the first time. This phase is formed at 445 °C, decomposes following a peritectic reaction at 527 °C, and can be quenched. A high-temperature X-ray diffraction study of a sample containing 75 mol% Sb_2Se_3 and 25 mol% Cu_2Se allowed us to measure the thermal expansion of the CuSbSe_2 and Sb_2Se_3 phases present in the sample. The anisotropy of thermal expansion of CuSbSe_2 is similar to that of As_2S_3 (orpiment); thermal expansion of Sb_2Se_3 is similar to that of AsS (realgar). The 6 balance equations of the invariant phase transformations involving all the ternary compounds existing in the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system were suggested for the first time. The temperature and the enthalpies of all these transformations were measured. A phase diagram of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system was found for the first time in all the range of concentrations at temperatures from ambient to the complete melting. This diagram takes into consideration the phase equilibria that involve all the ternary compounds that are possible in this system. The liquidus of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system was calculated according to Redlich-Kister equation; it agrees with the experimental data within 1–17 °C.

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1. Introduction

Materials based on Sb_2Te_3 (*n*-type semiconductor) and Cu_{2-x}Se (*p*-type semiconductor) are candidates to substitute the Bi_2Te_3 and

Sb_2Te_3 , respectively, in thermoelectric converters (TEGs) [1,2] and electronic devices [3,4].

The Cu_{2-x}Se ($x = 0-0.25$) phase, as well as Cu_{2-x}S [5], is a self-doped *p*-type semiconductor with a mixed ionic-electronic conductivity: $\rho = 10^{-4}-10^{-5} \Omega \text{ m}$, and $\kappa = 1 \text{ W/(m K)}$. The Seebeck coefficient for $\alpha\text{-Cu}_2\text{Se}$ is in the range from 60 to 100 mV/K (300–350 K), and for $\beta\text{-Cu}_2\text{Se}$ (420–1000 K), from 80 to 300 mV/K (420–1000 K) [2].

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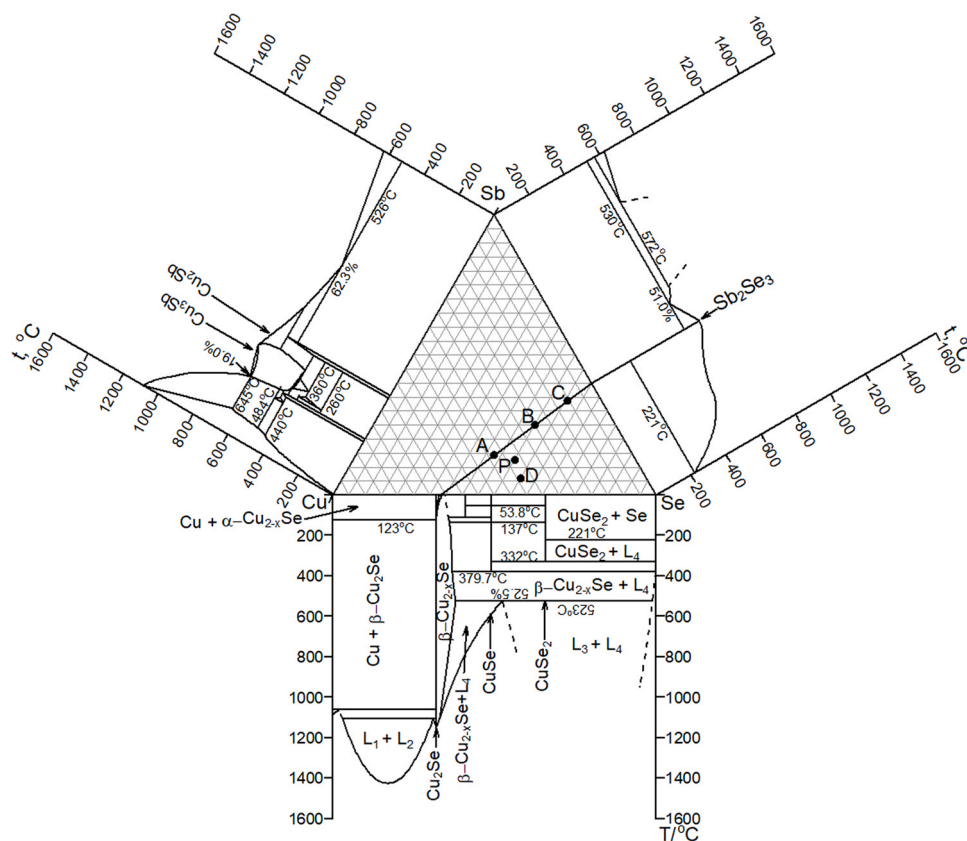


Fig. 1. The Cu-Sb-Se ternary system. Designations: A – Cu_3SbSe_3 , B – CuSbSe_2 , C – $\text{Cu}_{10.53}\text{Sb}_{33.78}\text{Se}_{55.68}$, D – $\text{Cu}_{38.8}\text{Sb}_{6.10}\text{Se}_{55.1}$, P – Cu_3SbSe_4 (permingheatite) (the phases were identified in [19]). Diagrams of binary systems Cu-Sb [20], Sb-Se [21], Cu-Se [22] are plotted on the sides of the triangle.

The Seebeck coefficient for Sb_2Se_3 at 300 K $\alpha \approx 1200$ mV/K [1] that is several times higher than the respective values for bismuth telluride or antimony telluride [6–8], as well as for their base alloys [9–11]. However, Sb_2Se_3 has low electric conductivity: $\sigma \approx 10^{-6} \Omega^{-1} \text{cm}^{-1}$ at 300 K [12]. It is promising to study Cu_{2-x}Se and Sb_2Se_3 based solid solutions in the Cu-Sb-Se ternary system (Fig. 1), since it is known that solid solutions often have improved thermoelectric parameters as compared with pure components [13–18].

The synthesis of Cu_2Se samples involves copper precipitation, so the thus-produced selenide phase has its stoichiometry shifting to Cu_{2-x}Se [22], X values being not specified in that study. The Cu_{2-x}Se polymorphs differ significantly from each other in X values (Fig. 1). The low-temperature phase $\alpha\text{-Cu}_{2-x}\text{Se}$ exists at temperatures up to 130 °C [2,23,24]; it crystallizes in the monoclinic system: $a = 14.087$ (Å), $b = 20.481$ (Å), $c = 4145$ (Å), $\beta = 90.38^\circ$ [25]; $a = 7.1379(4)$ (Å), $b = 12.3823(7)$ (Å), $c = 27.3904(9)$ (Å), $\beta = 94.308^\circ$ [26]. At 130 °C, $\alpha\text{-Cu}_{2-x}\text{Se}$ transforms to $\beta\text{-Cu}_{2-x}\text{Se}$, the cubic high-temperature phase: $a = 5.859(1)$ Å [26]; $a = 5854$ Å [27], space group $Fm\bar{3}m$ [26,27]. The congruent melting temperature was measured using differential thermal analysis to be 1117 °C [28], while use of drop calorimeter [29] resulted in the same melting temperature 1117 °C and specific heat 9055 J/mol. Glazov et al. reported the highest copper selenide melting temperature, equal to 1148 ± 1 °C, for a sample of $\text{Cu}_{1.994}\text{Se}$ [22]. Korzhuev et al. measured the highest melting temperature 1148 °C for $\text{Cu}_{1.99}\text{Se}$ [30]. Above the melting point, only liquid exists in the Cu-Se system (Fig. 2A). In [30], a stacked diagram of the Cu_{2-x}Se solid solution area is presented, the high-temperature part of which was not studied by thermal analysis methods.

Alpha and beta phases exist as independent areas of solid solutions. The $\alpha \rightarrow \beta$ transition occurs at 140 °C and is accompanied by the

formation of the β -phase and the elementary substance Cu. In the Cu-Se system, the composition of copper selenide Cu_{2-x}Se , which is in equilibrium with pure copper, is unknown. The dependence of this composition on the annealing temperature is also unknown.

Sb_2Se_3 crystallizes in the orthorhombic crystal system: structural type Sb_2S_3 , $Z = 4$; previously reported data on space groups (SG) (No 62) and unit cells parameters with e.s.d.s reported in the papers [31–35], are summarized in the Table 1.

The melting temperature of Sb_2Se_3 was measured as 611 °C in the paper [36] using differential thermal analysis; its heat of congruent melting was measured as either 50.2 ± 4.2 kJ/mol in the paper [37] or 54.4 ± 4.2 kJ/mol in the paper [38] using drop calorimeter.

The $\text{Cu}_{2-x}\text{Se}\text{-Sb}_2\text{Se}_3$ system is a section of the Cu-Sb-Se triangle (Fig. 1). Karup-Moller constructed the 350, 400, 450, 500, 600, and 700 °C isothermal sections of the Cu-Sb-Se triangle when studying 264 samples by the microprobe analysis using a JEOL Superprobe 733 [19]. From the data of [19], the results from the $\text{Cu}_2\text{Se}(\text{Cu}_{2-x}\text{Se})\text{-Sb}_2\text{Se}_3$ section are selected (Fig. 2B).

Majsztrik et al. [47] succeeded to prepare a single-phase Cu_3SbSe_3 sample by melt-quenching a 3Cu:1Sb:3Se batch followed by annealing at temperatures between 325 and 400 °C during up to 120 h. Quenching of a 3Cu:1Sb:3Se melt maintained at 500 or 900 °C without subsequent annealing yielded three-phase samples containing Cu_2Se , CuSbSe_2 , and Cu_3SbSe_3 . Annealing of the as-quenched three-phase sample at a temperature between 320 °C and 400 °C yielded Cu_3SbSe_3 due to the reaction between Cu_2Se and CuSbSe_2 controlled by diffusion rates in the solid state. The authors of [47] have measured the microhardness of the grains of Cu_2Se , Cu_3SbSe_3 and CuSbSe_2 using polished samples and a nanoindenter (Hysitron, TriboIndenter) with a diamond Berkovitch tip. According to [47], the

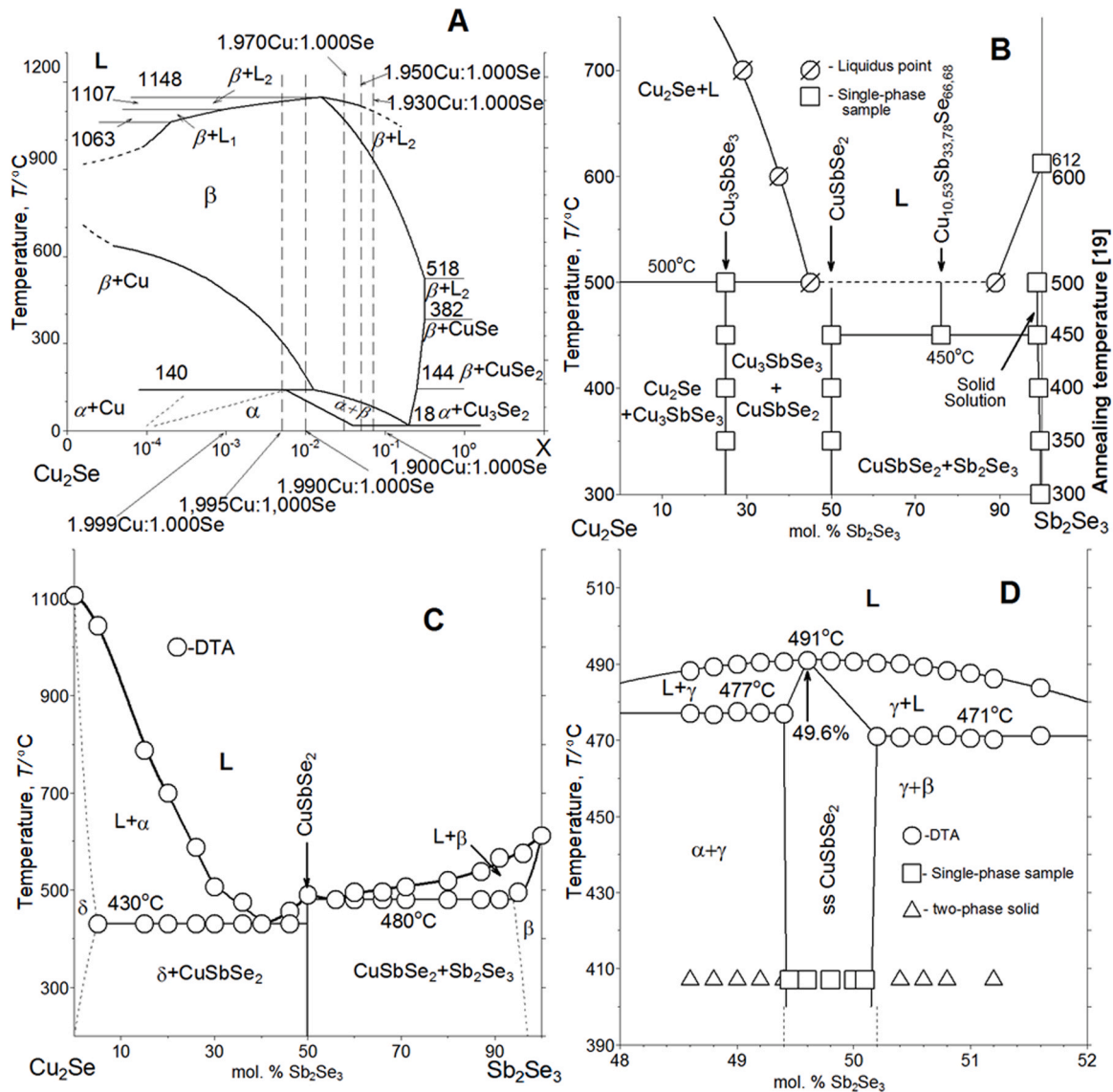


Fig. 2. Phase diagrams of systems. (A) is the area of the Cu_{2-x}Se solid solution. The x axis is the nonstoichiometry of the copper content [30]. Vertical dotted lines highlight a number of compositions. (B) – phase states of the samples in the section $\text{Cu}_2\text{Se}-\text{Sb}_2\text{Se}_3$ according to the study of the Cu-Sb-Se system in isothermal sections [19]. (C) – phase diagram of the $\text{Cu}_2\text{Se}-\text{Sb}_2\text{Se}_3$ system according to [39]. (D) – area of CuSbSe_2 phase based solid solution [40].

Table 1

Literature data on SG (No 62) and unit cell parameters for Sb_2Se_3 (Space group is the same in all 4 papers, two different settings were used for structure refinement), $Z = 4$.

Ref.	Setting	Unit cell parameters			
		a , (Å)	b , (Å)	c , (Å)	V , (Å ³)
[31]	$Pnma$	11.794(1)	3.986(1)	11.648(1)	547.583
[32]	$Pnma$	11.7938(9)	3.9858(6)	11.6478(7)	547.54
[33]	$Pnma$	11.744(4)	3.955(2)	11.588(5)	538.23
	$(Pbnm)$	(11.588(5))	(11.744(4))	(3.955(2))	
[34]	$Pnma$	11.77(1)	3.962(7)	11.62(1)	541.872
	$(Pbnm)$	(11.62(1))	(11.77(1))	(3.962(7))	
[35]	$Pnma$	11.780	3.985	11.633	546.09
	$(Pbnm)$	(11.633)	(11.780)	(3.985)	

values of the microhardness of the samples Cu_3SbSe_3 and CuSbSe_2 with different thermal history were very close (about 35000 MPa). The microhardness of the Cu_2Se phase was smaller (8000 MPa).

Glazov et al. in the paper [39] described phase equilibria in the $\text{Cu}_2\text{Se}-\text{Sb}_2\text{Se}_3$ system by a phase diagram with one congruently

melting compound, namely CuSbSe_2 , which divided the diagram into two simple eutectic diagrams with limited solid solubility (Fig. 2C).

Golovei et al. in the paper [40] determined the extension of CuSbSe_2 -based solid solution as 49.5–50.1 mol% Sb_2Se_3 . The maximum melting temperature ($491 \pm 3^\circ\text{C}$) corresponds to the Sb_2Se_3 content 49.6 mol% (Fig. 2D). The melting temperature of the stoichiometric CuSbSe_2 is $481 \pm 3^\circ\text{C}$. Temperature values were measured using differential thermal analysis.

According to [19], Cu_3SbSe_3 , CuSbSe_2 , and $\text{Cu}_{10.53}\text{Sb}_{33.78}\text{Se}_{55.68}$ ternary compounds are formed in the $\text{Cu}_{2-x}\text{Se}-\text{Sb}_2\text{Se}_3$ system. Their cell parameters and space groups (SG), reported in the papers [41–46], are summarized in the Table 2.

For the high-temperature phase $\text{Cu}_{10.53}\text{Sb}_{33.78}\text{Se}_{55.68}$, no structural data were documented. Its existence range was tentatively defined from 450 to 500°C [19].

Documenting the results of the studies of the Cu_2Se and Sb_2Se_3 -based solid solution, Karup-Moller did not report either direct experimental data on the variations in unit cell parameters, or the data

Table 2
Unit cell parameters and symmetry of the ternary compounds in the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system.

Ref.	SG, crystal system	Z	ST	Unit cell parameters			
				a, (Å)	b, (Å)	c, (Å)	V, (Å ³)
CuSbSe ₂ [41] [42] [43] [44]	Pnma, orthorhombic	4	CuBiS ₂	6.40	3.95	15.33	387.54
				6.299(2)	3.9734(12)	15.005(5)	375.5(2)
				6.302	3.988	14.957	375.9
				6.2988(8)	3.981(5)	15.003(2)	376.21(8)
Cu ₃ SbSe ₃ [45] [46]	Pnma, orthorhombic	4	Cu ₃ SbSe ₃	7.959(1)	10.583(1)	6.824(1)	574.79
				7.9865(8)	10.6138(9)	6.8372(7)	579.6(1)

from the thermoanalytical experiments, and microstructure studying [19].

There was no information on the enthalpies of phase transformations in the $\text{Cu}_2\text{Se-Sb}_2\text{Se}_3$ system, and no relevant thermodynamic calculations [19,39,40,47].

It is not explained in [47] why compounds Cu_3SbSe_3 and CuSbSe_2 with different chemical compositions and structures have coinciding microhardness values. The phase composition of the sample containing 75 mol% Sb_2Se_3 at elevated temperatures, features of thermal expansion of equilibrium phases, which can qualitatively explain the reasons for their interaction, have not been determined. Papers [39,40] do not present the data of thermal analysis, the results of studying the microstructure and phase composition of the samples.

It is an efficient strategy to combine differential scanning calorimetry with liquidus calculations by the Redlich-Kister equation [48]; along with other models [49–51]; this method has been actively developed in recent years [52–55].

In this work, we sought to determine the structure and properties of ternary phases formed in the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system, to obtain the phase diagram of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system, to find balance equations for phase transformations, and to calculate the liquidus using the Redlich-Kister equation.

2. Experimental details

2.1. Synthesis

The samples of Cu_{2-x}Se and Sb_2Se_3 binary compounds and $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ samples (from 3 to 7 g) were prepared from elements: antimony (99.9999 wt%), selenium (> 99.997 wt%), and electrolytic copper (99.99 wt%, purchased from Khimreaktiv, Russia). The weight of the synthesized samples ranged from 3 to 7 g. The accuracy of weighting the starting reactants is ± 0.00005 g (via a Mettler Toledo ME204 analytical balance). The reactants were placed into the optical silica glass ampoules (with volumes up to 5 cm³). The ampoules were degassed to 0.1 Pa and then sealed off [56]. Heat treatment mode for the reactants placed in degassed and sealed silica glass ampoules has been developed according to the data reported in the papers [19,39,40,47,57]. The ampoules with the samples were heated at 50–100 °C/day until the entire sample melted (depending on the sample, the melting temperature varied from 500 to 1150 °C, i.e. the whole heating procedure took from 120 to 300 h). The molten samples were kept at these temperatures for 1 h with the ampoules intermittently manually vibrated using a special home-made device [57–60]. Then the melts were either cooled at 50–100 °C/h or quenched in water at 20 °C. Samples containing 25 and 50 mol% Sb_2Se_3 were also prepared by the ceramic method. Preliminary synthesized binary compounds copper selenide and Sb_2Se_3 were weighted and then pressed into cylinders at 196 MPa. The ampoules with samples were annealed at 350 °C 750 h, at 350 °C 1100 h, at 470 °C 1950 h, and at 450 °C for 4300 h, at 480 °C for 4300 h. The temperature in the muffle furnaces was maintained with

an accuracy of ± 5 °C and automatically restored in case of power supply failures.

2.2. The ratio of elementary substances Cu, Sb, Se for the studied samples, the phase composition of the samples after synthesis and annealing

Due to the fact that the Cu_{2-x}Se phase acquires a copper-deficient nonstoichiometry during synthesis, we studied the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ and $\text{Cu}_{2-x}\text{Se-Cu}_3\text{SbSe}_3$ systems for various ratios of copper and selenium. In the present paper, the samples of copper semiselenide, which were synthesized and studied, are indicated not by lower case indices, but by the atomic ratio of the elements of copper and selenium, placed in a quartz ampoule. The weighted portions of elementary substances, which were placed in quartz ampoules, were calculated for the following sample compositions: section I: $(1-X) \times (2.000 \text{ Cu}: 1.000 \text{ Se}) + X \text{ Sb}_2\text{Se}_3$ ($X = 0-1.0$); section II: $(1-X) \times (1.995 \text{ Cu}: 1.000 \text{ Se}) + X \text{ Cu}_3\text{SbSe}_3$; section III: $(1-X) \times (1.990 \text{ Cu}: 1.000 \text{ Se}) + X \text{ Cu}_3\text{SbSe}_3$ ($X = 0-1.0$); section IV: $(1-X) \times (1.970 \text{ Cu}: 1.000 \text{ Se}) + X \text{ Cu}_3\text{SbSe}_3$ ($X = 0-1.0$); section V: $(1-X) \times (1.950 \text{ Cu}: 1.000 \text{ Se}) + X \text{ Cu}_3\text{SbSe}_3$ ($X = 0-1.0$); section VI: $(1-X) \times (1.930 \text{ Cu}: 1.000 \text{ Se}) + X \text{ Cu}_3\text{SbSe}_3$ ($X = 0-1.0$).

When studying the section $\text{Cu}_2\text{Se-Sb}_2\text{Se}_3$, in the range of compositions 25–100 mol% Sb_2Se_3 , conforming results of physicochemical studies were obtained for several series of samples. Impurity phases were present only in single synthesized and annealed samples. The results of the physicochemical study of samples from the $\text{Cu}_2\text{Se-Sb}_2\text{Se}_3$ section for the concentration range 25–100 mol% Sb_2Se_3 are plotted on the diagram of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system.

In the concentration range 0–25 mol% Sb_2Se_3 system $\text{Cu}_{2-x}\text{Se-Cu}_3\text{SbSe}_3$ was studied in six sections (I–VI). In each section, from 2 to 15 samples were synthesized. We tried to determine the composition of copper selenide, which is in equilibrium with the Cu_3SbSe_3 phase, in order to present the phase diagram of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system without phase equilibrium lines from the ternary system Cu-Sb-Se [61–63].

3. Methods of physicochemical analysis

Microstructural analysis (MSA) was carried out on AxioVert.A1MAT metallurgical microscope (0.5 μm resolution). The AxioVision SE64 program suite was used to calculate the amount of grains of different phases [61]. In order to get clear photographs, thin polished sections of the samples were etched with chromosulfuric acid. The chemical and grain compositions of the samples as well as particle morphology were determined at three sites on the surface of the sample by scanning electron microscopy (SEM) using a Tescan Mira 3 LMU scanning electron microscope (SEM) equipped with an energy dispersive X-ray spectroscopy (EDS) Oxford instruments unit (with references) and INCA analyzer software [64]. EDS data were used to map the surface distributions of elements in Aztec software.

Microhardness [65] was measured using an HMV-G21DT microhardness tester using HMV-G data processing software [60]. The result represented an average value over 15 clear-cut indents.

Samples for metallographic studies and microhardness measurements were embedded into the epoxy resin, ground with alumina abrasive papers (P180-P1000), polished with chromium(III) oxide (0.3 μm) paste and diamond (0.1/0 μm) paste, cleaned with ethanol, and then cotton swab dried. For SEM characterization, samples were prepared in a similar way but without embedding in epoxy resin [60,66–69].

Standard calculation software was used in calculations with using Redlich-Kister equation [70].

The phase diagrams for this paper were plotted using software edstate23D developed in Tyumen state university, including computer programs edstate2D (to calculate the binary phase diagrams) and edstate3D (to plot flat isothermal sections of the ternary phase diagrams) [71].

The DSC data for each group of the experimental points of the phase diagram of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system were approximated by a third-order polynomial using the edstate2D program, entering the invariant points as compulsory. The same edstate2D program was used to reproduce the documented binary phase diagrams in the ternary Cu-Sb-Se system. The program edstate3D was used to plot the isothermal section of the ternary Cu-Sb-Se system at 20 °C.

Differential scanning calorimetry (DSC) experiments [66] were carried out on a Setsys Evolution 1750 (TGA–DSC 1600) thermal analyzer with a Pt/PtRh (10%) thermocouple using SETSOFT 2000 data processing software, and on a STA 449 F3 Jupiter simultaneous thermal analyzer with a W3%Re-W25% thermocouple using NETZSCH Proteus 6.1 software. The heating rate was 3 or 5 °C/min [67]. Samples for DSC (100–110 mg) were placed into quartz ampoules (about 100 μL), which were then sealed off. A sealed-off empty ampoule served as a reference [72]. For calibration, pure metal standards: In (99.9995%), Sn (99.9995%), Bi (99.9995%), Al (99.995%), Zn (99.995%), Ag (99.999%), Au (99.9995%), Pb (99.9995%), Cu (99.999%), Pd (99.999%) were used. The Setsys Evolution 1750 (TGA–DSC 1600) has a measurement error of ± 1.8 °C in determining the temperature and 11.6% in determining the enthalpies of phase transitions. The STA 449 F3 Jupiter has a measurement error of ± 1.50 °C in determining the temperature and 6.9% in determining the enthalpies of phase transitions [66].

X-ray powder diffraction (XRD) patterns were recorded on DRON-7 [66–68] (Ni-filtered CuK_α radiation ($\lambda = 1.5406$ Å)), on Bruker D2 Phaser [73] (Ni-filtered CuK_α radiation ($\lambda = 1.5406$ Å)), and on Rigaku Ultima IV (CuK_α radiation ($\lambda = 1.5406$ Å)), Graphite monochromator Cu (Flexible) [74] diffractometers. The following software was used: PDWin 4.0 [66–68], Topas 6 [75], Bruker Diffrac.EVA [73], and HighScore version 3.0 (2012) with reference to the PDF-2 File and Crystallography Open Database (COD) [76]. The samples were further studied at a D8 Advance Bruker X-ray diffractometer equipped with an HTK-1200N Anton Paar high-temperature chamber in the temperature range 20–480 °C using CuK_α radiation [75]. High-temperature powder X-ray diffraction (HTXRD) experiments were carried out at 100, 200, 300, 400, 410, 420, 430, 440, 450, 460, 470, and 480 °C. The sample was put into a high-temperature chamber with Pt heating filament. If the sample amount was small, X-ray radiation penetrated Pt heating filament. The intensity of the platinum line served to assess the degree of sublimation of sample during experiment. The platinum percentage at 20 °C was 4.3 mol% Pt. Unit cell parameters of the phases for each temperature were calculated using the FULLProf software package [77]. The X-ray diffraction patterns were processed by the Rietveld method [78] in the Topas 6 program [79,80]. Thermal expansion was determined for CuSbSe_2 and Sb_2Se_3 selenides from powder HTXRD data. Eigenvalues of thermal expansion tensor were determined using the polynomial approximation of temperature dependencies

of the unit-cell parameters by the Theta To Tensor & Rietveld To Tensor software [81,82].

Single-crystal X-ray diffraction data for CuSbSe_2 and Cu_3SbSe_3 were collected at an Oxford Diffraction Gemini R Ultra X-ray diffractometer equipped with a CCD area detector using $\text{MoK}\alpha$ radiation [83]. For these studies we used the fragments of the broken polycrystalline blocks that were solidified by slow cooling of melt, and then annealed. They contained several differently oriented single-crystalline domains. CrysAlisPro software [84] was used for data collection, unit cell determination, and primary data processing. The structures were solved using the dual-space algorithm implemented in SHELXT software [85]. Refinement was done using SHELXL-2018 [86] with ShelXle [87] as the GUI. IUCr Checkcif/PLATON service [88] was used to validate the structural model. VESTA [89] was used for graphical representation of the crystal structures. The complete structural data set was deposited with the CSD [90] (refcodes CCDC 2080025–2080026).

Diffuse reflectance spectra were taken from thin layers of powders in the range 200–1400 nm using a UV-2600 Shimadzu (Japan) spectrophotometer equipped with an ISR-2600Plus integrating sphere attachment [91]. BaSO_4 standard supplied by Shimadzu with the spectrophotometer was used in the measurement of diffuse reflection spectra. Upon building the linear fit for the fundamental absorption region, we chose the regions of linearity in the way that enabled Pearson correlation coefficient to be 0.999 just like, e.g., in the paper by Rampino [92].

4. Results and discussion

4.1. The samples of ternary compounds Cu_3SbSe_3 and CuSbSe_2 of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system

The polycrystalline samples of ternary compounds (Cu_3SbSe_3 and CuSbSe_2) of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system that were prepared from elements and annealed at 450 °C for 4300 h, were analyzed by several instrumental techniques. The part of the sample used for analyzing by X-ray powder diffraction and for particle morphology characterization by scanning electron microscopy was preliminary fine-ground manually in a mortar. The part of the sample used for elemental analysis using the same scanning electron microscope (see Experimental details) was studied after surface polishing.

X-ray powder diffraction patterns of the samples of Cu_3SbSe_3 and CuSbSe_2 ternary compounds of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system that were prepared from elements and annealed at 450 °C for 4300 h are shown in Fig. 3.

According to the X-ray powder diffraction analysis, the samples of the ternary compounds contained a single phase each. Therefore, we decided to study the samples by several instrumental techniques.

The crystallites of Cu_3SbSe_3 in the thin polished sections of the cooled molten polycrystalline samples were of light gray color with a faint greenish tint. The crystallites of CuSbSe_2 in the polished thin sections were light-colored with a grayish tint. In the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system, the microhardness of the phases changes completely regularly: Cu_{2-x}Se $H = 99 \pm 7$ HV, Cu_3SbSe_3 $H = 235 \pm 5$ HV, CuSbSe_2 $H = 179 \pm 9$ HV, Sb_2Se_3 $H = 45 \pm 3$ HV.

The SEM images of the particles and the element distribution of the samples of Cu_3SbSe_3 and CuSbSe_2 ternary compounds are shown in Fig. 4.

The crystallites in Cu_3SbSe_3 had the sizes of about 5–30 μm and a dense grain structure. Most CuSbSe_2 grains had a layered structure. The layer thickness was 0.1–0.3 μm . The crystallites of the compounds had polyhedral shapes with the angles of 60° and 120° (Fig. 4).

The distribution of copper, antimony, and selenium in the thin polished sections of the solid samples, as probed by SEM, was uniform in full agreement with XRD data (Fig. 4). EDS elemental

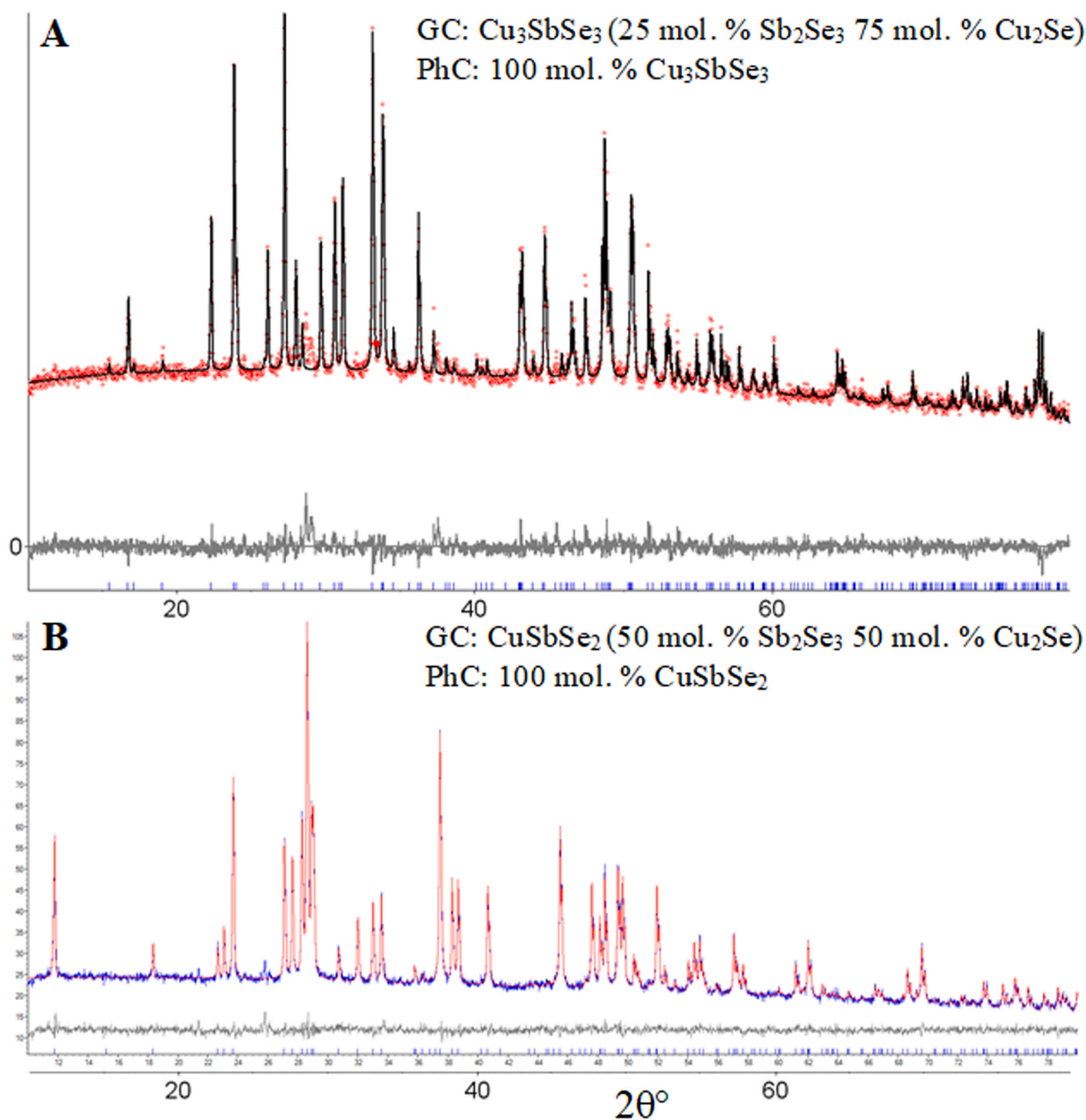


Fig. 3. X-ray diffraction patterns of the samples of ternary compounds of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system annealed at 450 °C for 4300 h: (A) Cu_3SbSe_3 and (B) CuSbSe_2 . Experimental patterns, calculated diffraction patterns, difference plot and the positions of diffraction patterns in the calculated patterns.

mapping made it possible to identify also the traces of minor phases. Thus, in the Cu_3SbSe_3 sample, there were a few selenium-enriched grains. In the CuSbSe_2 sample, there was one antimony grain smaller than 10 μm .

The fragments of sub-millimeter sizes were separated from the polycrystalline Cu_3SbSe_3 and CuSbSe_2 samples and studied by single-crystal X-ray diffraction. For the first time, the crystal structure of Cu_3SbSe_3 and CuSbSe_2 compounds on single-crystal blocks was studied. Unfortunately, we failed to break blocks so that to get

true single-crystal samples. The blocks contained several single-crystalline fragments. However, most reflections from a multi-crystalline sample did not overlap, so that the crystal structure refinement provided acceptable and reliable results. The data collection and refinement details as well as crystal data are summarized in Electronic [supplementary information](#) (ESI) (Table S1).

The fragments of the Cu_3SbSe_3 and CuSbSe_2 crystal structures were obtained (refcodes CCDC 2080025–2080026). The CuSbSe_2 structure is built of SbSe_5 square pyramids and CuSe_4 tetrahedra

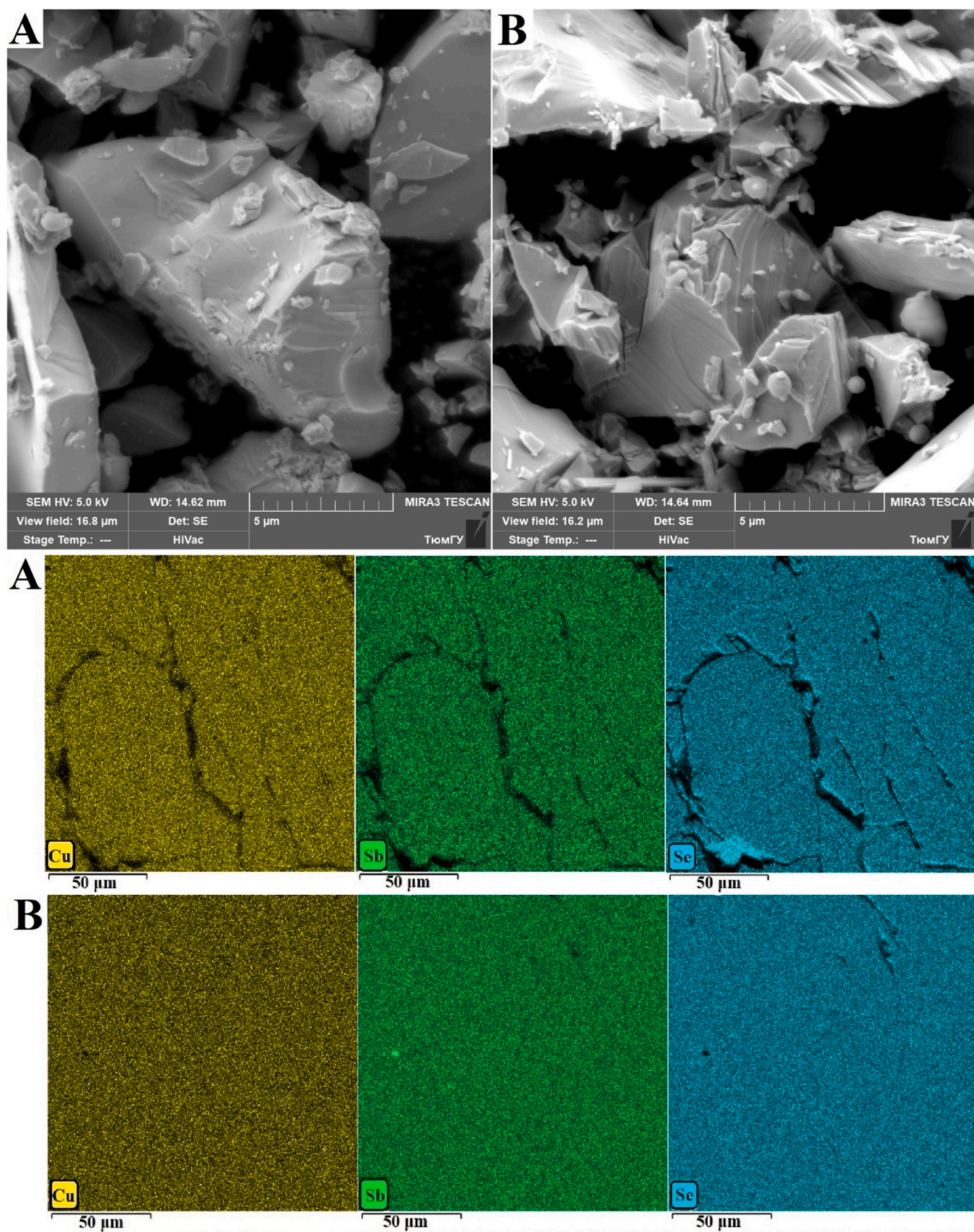


Fig. 4. SEM images of particles of powders and EDS elemental mapping showing the distribution of chemical elements Cu, Sb, Se in thin polished sections for samples of ternary compounds: A – Cu_3SbSe_3 , B – CuSbSe_2 .

Table 3
Balance equations of invariant equilibria in the $\text{Cu}_2\text{-xSe-Sb}_2\text{Se}_3$ system.

No.	Phase transformation	Invariant point coordinates		Phase transformation equation, mol%	ΔH , J/g	ΔH , kJ/mol
		composition, mol% Sb_2Se_3	T/°C			
1	Incongruent melting of Cu_3SbSe_3	25	530	$\text{Cu}_3\text{SbSe}_3 (0.25 \text{ Sb}_2\text{Se}_3; 0.75 \text{ Cu}_{1,995}\text{Se}) \leftrightarrow 0.226 \beta\text{-Cu}_{1,995}\text{Se ss} (0.01 \text{ Sb}_2\text{Se}_3; 0.99 \text{ Cu}_{1,995}\text{Se}) + 0.774 \text{L} (0.32 \text{ Sb}_2\text{Se}_3; 0.68 \text{ Cu}_{1,995}\text{Se})$	67.6	37.1
2	Eutectic ($1\text{Cu}_3\text{SbSe}_3 + 8\text{CuSbSe}_2$) melting	45	477	$0.889 \text{CuSbSe}_2 (0.5 \text{ Sb}_2\text{Se}_3; 0.5 \text{ Cu}_{1,995}\text{Se}) + 0.111 \text{Cu}_3\text{SbSe}_3 (0.25 \text{ Sb}_2\text{Se}_3; 0.75 \text{ Cu}_{1,995}\text{Se}) \leftrightarrow \text{L} (0.45 \text{ Sb}_2\text{Se}_3; 0.55 \text{ Cu}_{1,995}\text{Se})$	73.3	-
3	Incongruent melting of CuSbSe_2	50	479	$\text{CuSbSe}_2 (0.5 \text{ Sb}_2\text{Se}_3; 0.5 \text{ Cu}_{1,995}\text{Se}) \leftrightarrow 0.862 \text{L} (0.46 \text{ Sb}_2\text{Se}_3; 0.54 \text{ Cu}_{1,995}\text{Se}) + 0.138 \text{CuSb}_3\text{Se}_5 (0.75 \text{ Sb}_2\text{Se}_3; 0.25 \text{ Cu}_{1,995}\text{Se})$	85.1	29.2
4	Formation of high-temperature compound CuSb_3Se_5	75	445	$0.500 \text{Sb}_2\text{Se}_3 + 0.500 \text{CuSbSe}_2 (0.5 \text{ Sb}_2\text{Se}_3; 0.5 \text{ Cu}_{1,995}\text{Se}) \leftrightarrow \text{CuSb}_3\text{Se}_5 (0.75 \text{ Sb}_2\text{Se}_3; 0.25 \text{ Cu}_{1,995}\text{Se})$	21.5	17.7
5	Incongruent melting of CuSb_3Se_5	75	527	$\text{CuSb}_3\text{Se}_5 (0.75 \text{ Sb}_2\text{Se}_3; 0.25 \text{ Cu}_{1,995}\text{Se}) \leftrightarrow 0.138 \text{Sb}_2\text{Se}_3 + 0.862 \text{L} (0.71 \text{ Sb}_2\text{Se}_3; 0.29 \text{ Cu}_{1,995}\text{Se})$	36.7	30.2
6	Eutectoid phase transformation in $\text{Cu}_2\text{-xSe ss}$	1	125	$0.020 \text{Cu}_3\text{SbSe}_3 (0.25 \text{ Sb}_2\text{Se}_3; 0.75 \text{ Cu}_{1,995}\text{Se}) + 0.980 \alpha\text{-Cu}_{1,995}\text{Se ss} (0.005 \text{ Sb}_2\text{Se}_3; 0.995 \text{ Cu}_{1,995}\text{Se}) \leftrightarrow \beta\text{-Cu}_{1,995}\text{Se ss} (0.01 \text{ Sb}_2\text{Se}_3; 0.99 \text{ Cu}_{1,995}\text{Se})$	11	2.3

seems appropriate to write the eutectic composition as $(1\text{Cu}_3\text{SbSe}_3 + 8\text{CuSbSe}_2)$.

Eutectic mixtures consisted of extended oval grains of Cu_3SbSe_3 and CuSbSe_2 phases, 1.5–4 μm wide and an average length of 5–9 μm , located in the volume of CuSbSe_2 phase crystals of almost the same dimensions, a width of 2–5 μm , and a length of 4–11 μm (Fig. 8, sample B).

The Cu_3SbSe_3 and CuSbSe_2 primary crystals as crystallized from the melt had different shapes. The Cu_3SbSe_3 primary crystals were typically oval with linear sizes of 25–250 μm and angles of 120°. The CuSbSe_2 primary crystals were oblong, 10–50 μm wide and 100–350 μm long. In some areas of the sample, crystals formed layered structures. Eutectic crystals were located in the interlayers in-between the layered oblong primary crystals of CuSbSe_2 (Fig. 8).

In the concentration range 50–100 mol.% Sb_2Se_3 , a high-temperature compound of provisional composition CuSb_3Se_5 was formed. The endotherm due to the formation of this compound appeared at 445 °C in all the samples that contained more than 50 mol.% Sb_2Se_3 .

Several methods were used to prepare 75 mol% Sb_2Se_3 samples, in particular, by careful co-grinding of the powder samples of the annealed CuSbSe_2 and Sb_2Se_3 compounds. The formation of phases in particles during grinding of layers, a decrease in particle size to 0.5–2 μm , form a high specific surface of phase contact. Such an approach is known to be efficient in the solid-state inorganic synthesis. The authors of papers [96–101] used mechanochemistry methods to increase the chemical activity of reagents. The mechanical treatment of CuSbSe_2 and Sb_2Se_3 phases yields the high-temperature phase CuSb_3Se_5 already on the first heating of the sample to 450 °C [38].

The DSC curve of the sample 6 in Fig. 6 features a peak due to CuSb_3Se_5 phase formation at 445 °C ($\Delta H = 21.5 \text{ J/g}$) and then a weak peak at 479 °C due to the incongruent melting of CuSbSe_2 ($\Delta H = 1.92 \text{ J/g}$). The enthalpy of CuSbSe_2 melting in a 75 mol% Sb_2Se_3 sample calculated on the assumption of the absence of the CuSb_3Se_5 phase in the system $\Delta H = 0.5 \times 145 = 72.5 \text{ J/g}$. The DSC data were used to calculate the yield of reaction (4) in a sample heated to 500 °C as $100\% - (1.92 \text{ J/g} : 72.5 \text{ J/g}) \times 100\% = 97.35\%$. The yields of the reaction (4) for several independently prepared samples ranged within 90–97.5%. The values of the enthalpies for reactions (4) and (5) are given in Table 3. According to the DSC data, the transformation completeness for the reaction (4) was equal to 97%.

The average temperature of CuSb_3Se_5 incongruent melting is 527 °C for the samples whose compositions lie in the range 72–99 mol% Sb_2Se_3 . In the paper [102] proposed a technique for separating the areas of overlapping peaks originating from various thermal effects. The overlapping peaks due to the melting of CuSb_3Se_5 (36.7 J/g) and the melting of Sb_2Se_3 primary crystals (29.6 J/g) (Fig. 6: samples (6), (7)) were resolved as described in the paper [102]. The temperatures and enthalpies of CuSb_3Se_5 decomposition were reproduced in parallel experiments. Tammann triangle plotting shows that the thermal events have the highest values at 75 mol% Sb_2Se_3 . When the samples were heated further after the CuSb_3Se_5 decomposition, the DSC curves featured the melting of the Sb_2Se_3 crystals. The end temperatures of these thermal events were identified as liquidus temperatures (Fig. 6: samples (6) and (7)).

During the cooling of the sample 75 mol% Sb_2Se_3 two sets of undercooling thermal events were recorded. As a rule, Sb_2Se_3 and CuSb_3Se_5 grains crystallize simultaneously following the reaction (4). The decomposition of CuSb_3Se_5 and the formation of CuSbSe_2 by reaction (5) also occurred in close temperature ranges, or simultaneously (Table 3).

The high-temperature phase CuSb_3Se_5 was not detected upon cooling or quenching. CuSbSe_2 and Sb_2Se_3 were the equilibrium phases at temperatures below 445 °C in the range 50–100 mol%

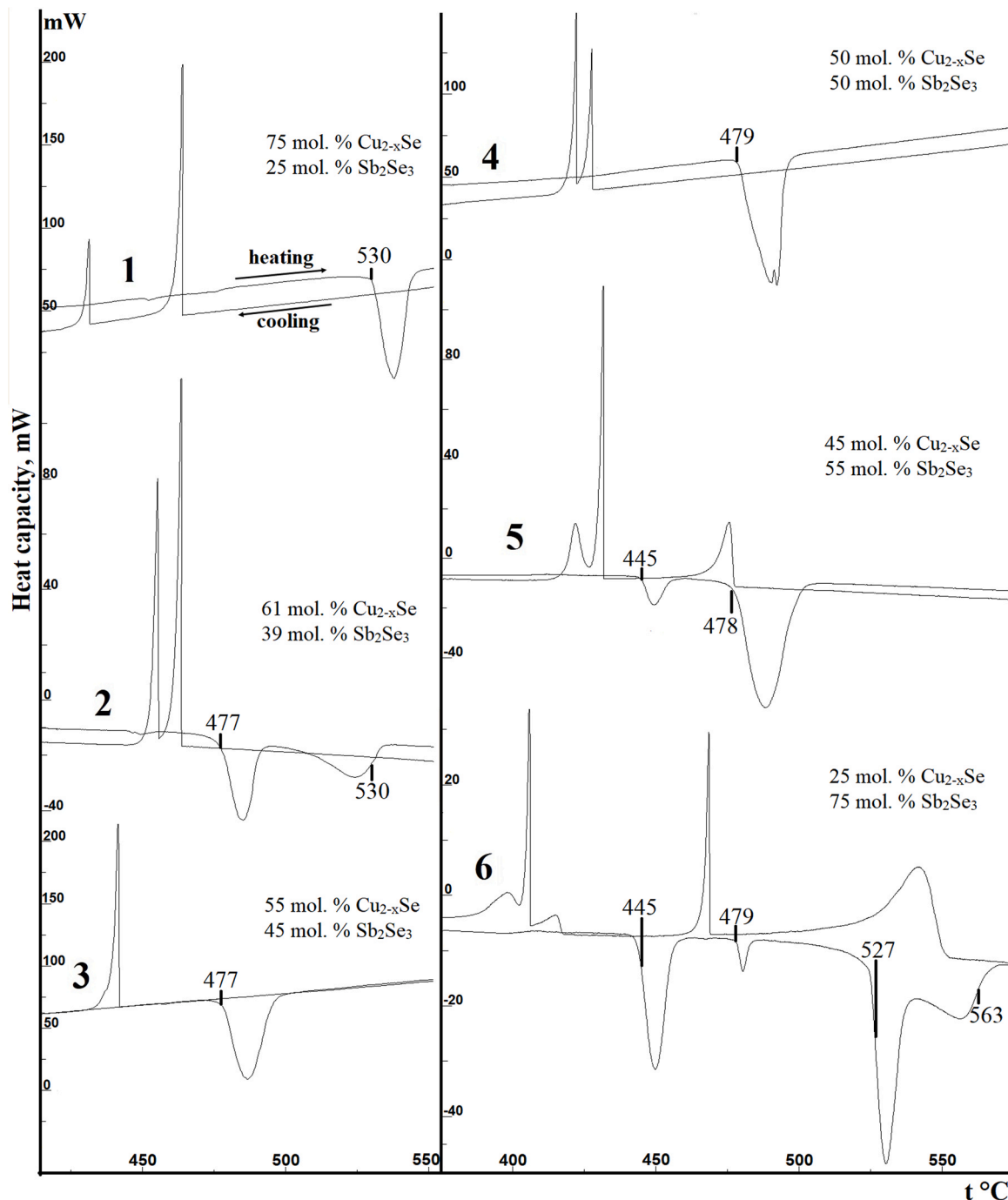


Fig. 6. DSC traces for $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ samples containing: (1) 25.0, (2) 39.0, (3) 45.0, (4) 50.0, (5) 55.0, and (6) 75.0 mol% Sb_2Se_3 .

Sb_2Se_3 . The compositions of the samples in this range did not change during annealing for 750 and 1100 h at 350 °C (Fig. 8: sample D). Sample 75 mol% Sb_2Se_3 was studied by high-temperature powder X-ray diffraction (Fig. 9). Weak reflections from the platinum heating filament were detected at 20 °C (Fig. 9A).

The intensity of the platinum lines was used to estimate the degree of sublimation of the sample during experiment. The systematic increase in the intensity of platinum reflections in the diffraction patterns collected on heating was indicative of sublimation of the selenides. At 20 °C, the sample consists of the CuSbSe_2 and Sb_2Se_3 phases, the reflection of platinum is also fixed. The platinum percentage at 20 °C was 4.3 mol% Pt (Fig. 9A).

Sublimation of the selenides in the diffractometer chamber became visually observable at 450 °C. At 480 °C, the percentage of the platinum in the sample including the substrate and the selenides was as high as 25.54 mol% Pt (Fig. 9B).

5. Thermal expansion of CuSbSe_2 and Sb_2Se_3

As temperature rises, the unit cell parameters of CuSbSe_2 and Sb_2Se_3 phases increase continuously up to 460 °C (Fig. 10). The temperature dependencies of the unit-cell parameters were approximated by quadratic polynomial functions $p_T = p_0 + p_1T + p_2T^2$ where p_T denotes a , b , c and V parameters for both selenides within

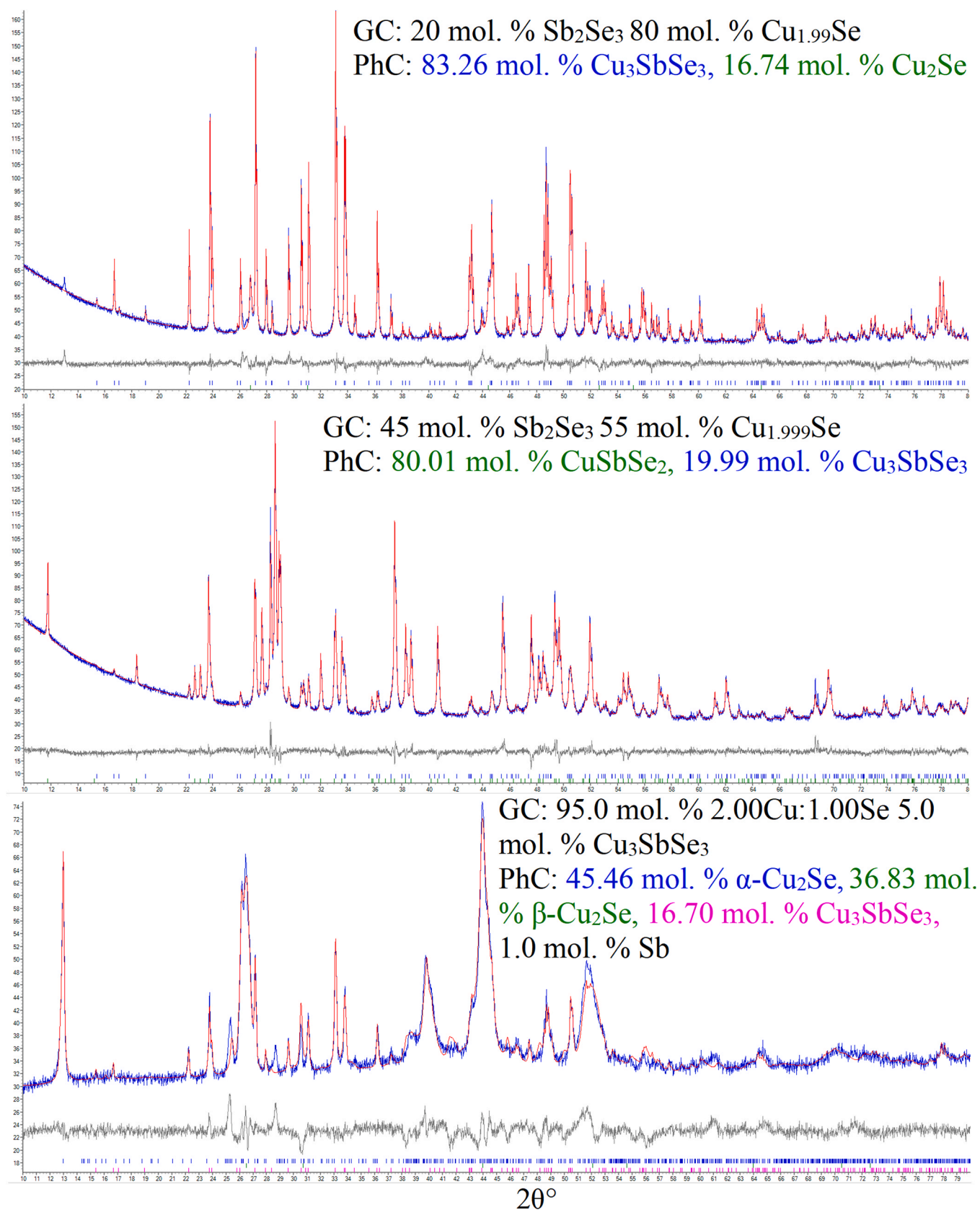


Fig. 7. X-ray diffraction patterns of annealed at 350 °C during 750 h samples. Notations: GC – as-batch (global) composition; PhC – phase composition of the sample.

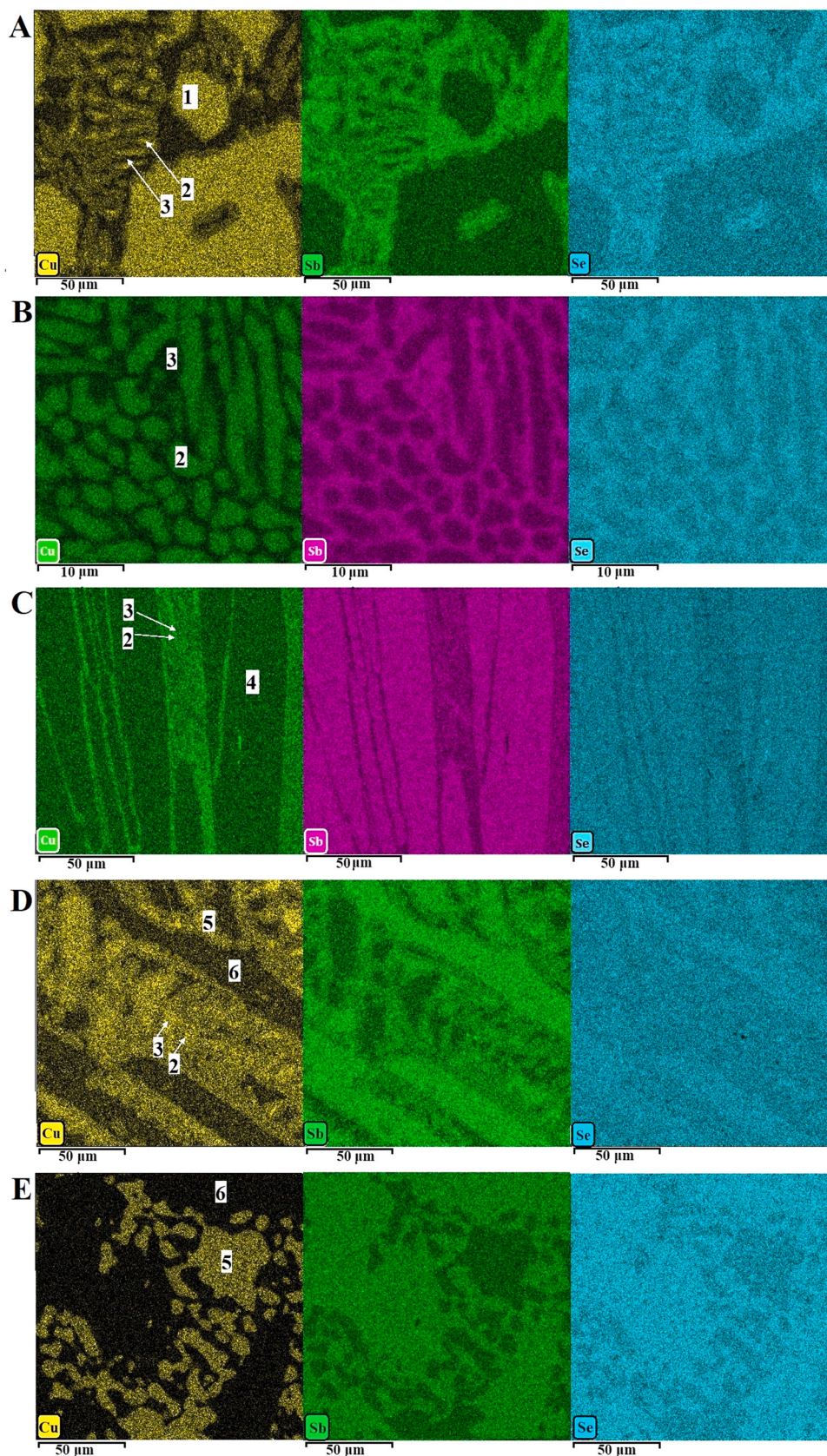


Fig. 8. SEM images illustrating the Cu, Sb, and Se concentrations in polished thin sections of heat-treated samples of as-batch composition (mol% Sb_2Se_3): (A) 39.0, (B) 45.0, (C) 48.0, (D) 55.0, and (E) 75.0. (1, 2) Cu_3SbSe_3 grains: (1) primary grains crystallized from the melt and (2) eutectic grains. (3, 4, 5) CuSbSe_2 grains: (3) eutectic, (4) primary, and (5) having compositions in the range 50–100 mol% Sb_2Se_3 . (6) Sb_2Se_3 grains.

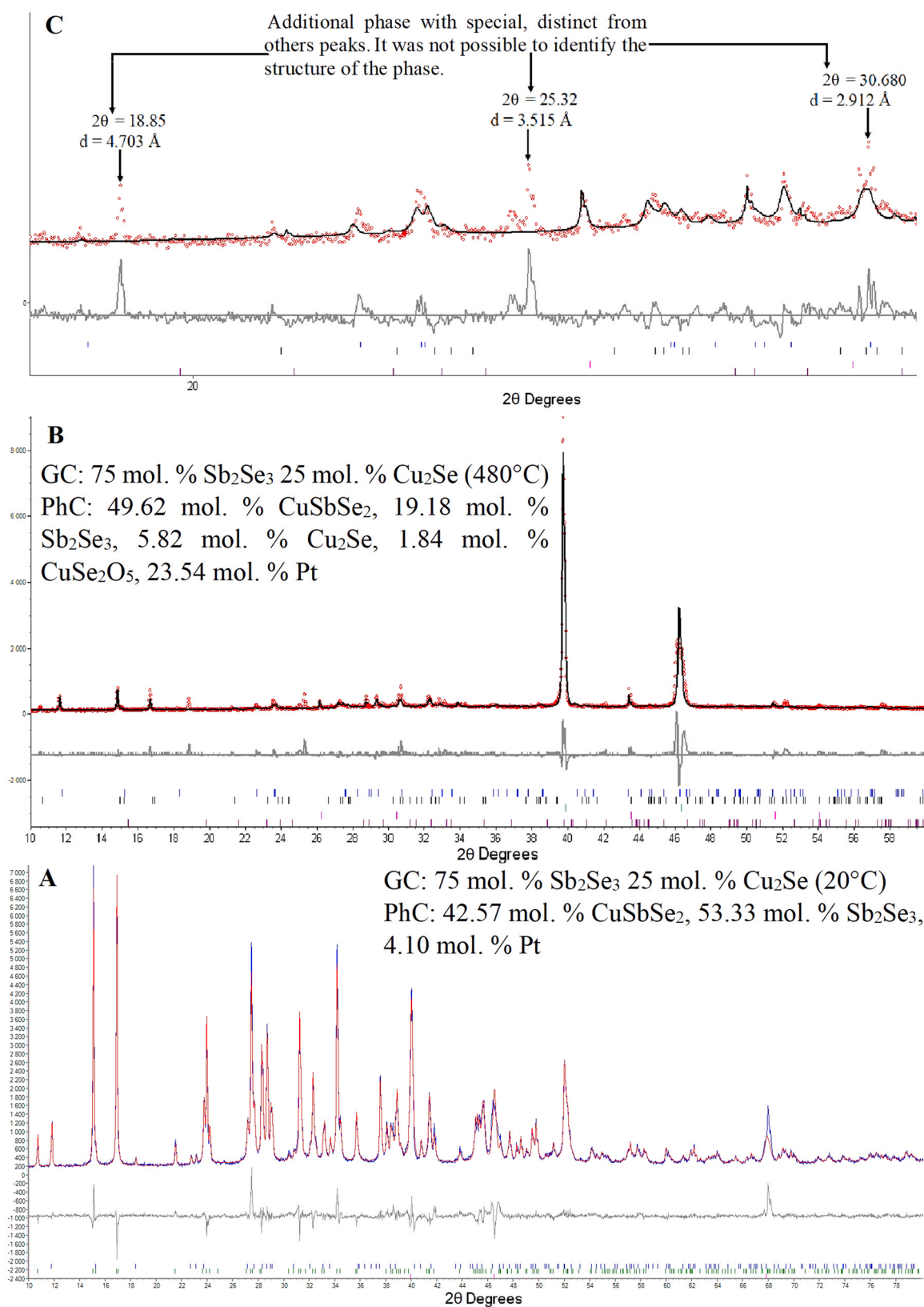


Fig. 9. X-ray diffraction patterns of a 75 mol% Sb_2Se_3 + 25 mol% Cu_2Se sample at (A) 20°C and (B) 480°C; and (C) a fragment of the 480°C X-ray diffraction pattern where the peaks of the newly formed CuSb_3Se_5 phase are indicated.

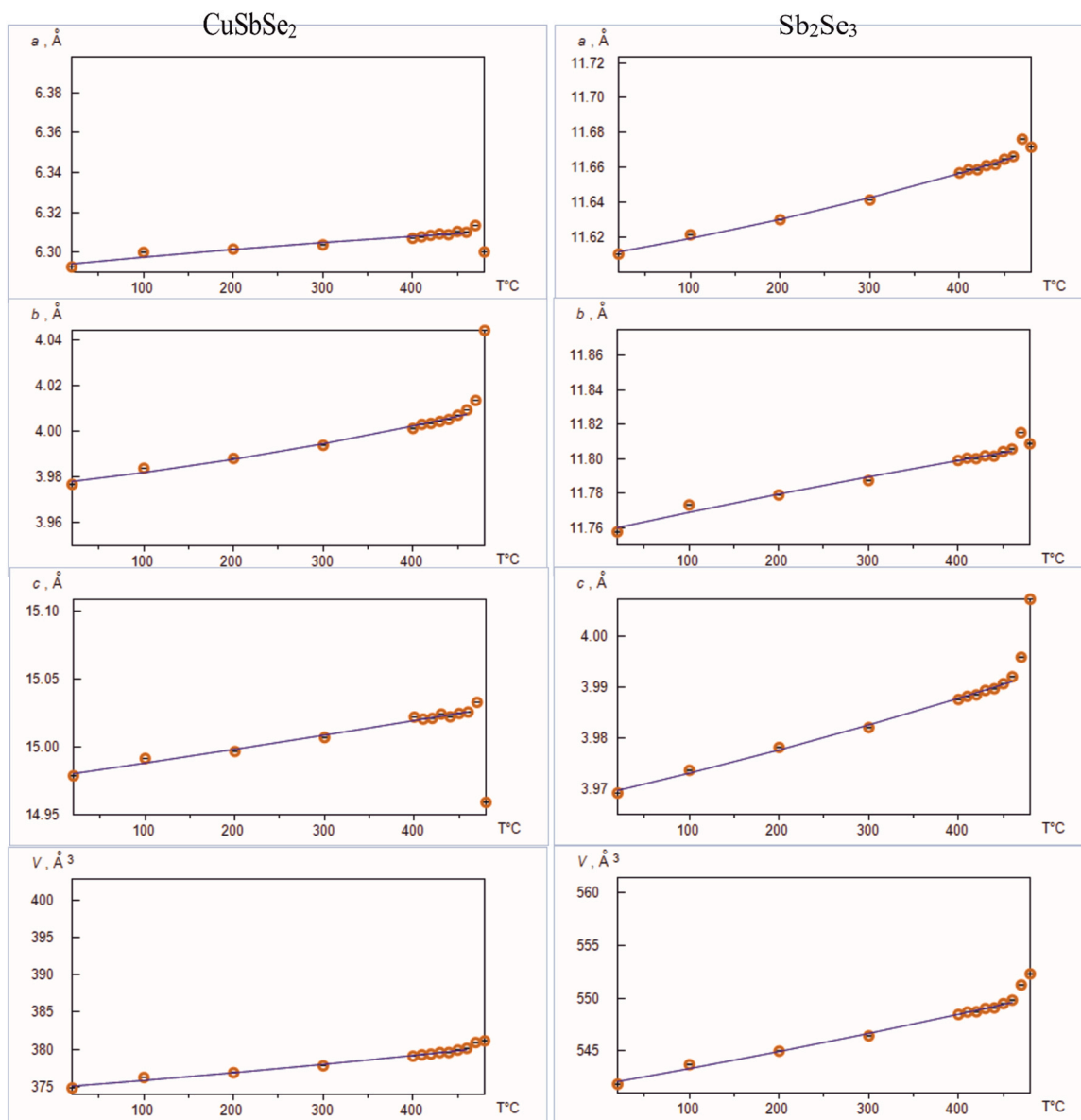


Fig. 10. Unit cell parameters of CuSbSe₂ and Sb₂Se₃ phases versus temperature in a 75 mol% Sb₂Se₃ + 25 mol% Cu₂Se sample.

the 20–460 °C temperature range (Table 4). Using the coefficients of approximation, the components of tensor (Table 5) were determined, and the drawing of the figures of α were performed using the Theta To Tensor & Rietveld to Tensor software [81,82].

Volume thermal expansion, α_v , gradually increases for both selenides within the temperature range under study; also, the anisotropy of thermal expansion defined as ratio $\alpha_{max}/\alpha_{min}$ rises for both phases when temperature increases (Table 5). Anisotropy for CuSbSe₂ is about 1.7 at 20 °C and it becomes about 5 at 450 °C, that

for Sb₂Se₃ is about 1.4 at 20 °C and 1.9 at 450 °C. Volume expansion increase is caused by rising thermal vibrations.

The crystal structure of CuSbSe₂ expands dramatically within the area close to *b* direction and minimally within the area close to *a* direction (Table 5). The framework is formed by alternating layers of CuSe₄ tetrahedra and SbSe₅ square pyramids, the layers are arranged perpendicular to the *c* axis (Fig. 11). The covalent Sb–Se bonds in pyramids are stronger than the more ionic Cu–Se bond. The apical bond is the shortest (Sb–Se1 is 2.569 Å) in comparison with others

Table 4

Polynomial coefficients ($p_T = p_0 + p_1T + p_2T^2$) for approximation of the unit-cell parameters and V for CuSbSe₂ and Sb₂Se₃ within 20–460 °C.

Parameter	CuSbSe ₂			Sb ₂ Se ₃		
	p_0	$p_1 \times 10^3$	$p_2 \times 10^6$	p_0	$p_1 \times 10^3$	$p_2 \times 10^6$
<i>a</i>	6.2933(13)	0.044(13)	−0.019(25)	11.6100(13)	0.087(12)	0.076(23)
<i>b</i>	3.9773(13)	0.043(12)	0.050(24)	11.7578(21)	0.114(21)	−0.028(41)
<i>c</i>	14.9784(21)	0.097(20)	0.015(39)	3.96888(57)	0.0406(56)	0.017(10)
<i>V</i>	374.92(21)	9.1(2.1)	4.0(4.1)	541.78(22)	14.8(2.1)	4.7(4.1)

Table 5
Eigenvalues of thermal expansion tensor for CuSbSe_2 and Sb_2Se_3 phases at selected temperatures.

α (10^6 °C $^{-1}$)	Temperature, T / °C					
	20	100	200	300	400	450
CuSbSe_2						
$\alpha_a = \alpha_{11}$	7.1(2)	6.4(1.2)	5.8(6)	5.2(6)	4.6(1.2)	4.3(1.6)
$\alpha_b = \alpha_{22}$	10.8(3.1)	13.3(1.9)	15.8(9)	18.2(8)	20.7(1.8)	21.9(2.4)
$\alpha_c = \alpha_{33}$	6.5(1.3)	6.67(87)	6.9(4)	7.1(4)	7.24(82)	7.3(1)
α_V	24.4(5.6)	26.4(3.5)	28.5(1.6)	30.5(1.4)	32.5(3.3)	33.5(4.3)
$\alpha_{\max}/\alpha_{\min}$	1.66	2.1	2.72	3.5	4.5	5.09
Sb_2Se_3						
$\alpha_a = \alpha_{11}$	7.5(1)	8.8(7)	10.0(3)	11.3(3)	12.6(6)	13.3(8)
$\alpha_b = \alpha_{22}$	9.7(1.8)	9.2(1.1)	8.8(5)	8.3(5)	7.8(1)	7.5(1.4)
$\alpha_c = \alpha_{33}$	10.2(1.4)	11.1(9)	11.9(4)	12.7(4)	13.5(8)	14.0(1.1)
α_V	27.4(4)	29.1(2.5)	30.7(1.1)	32.3(1)	33.9(2.3)	34.7(3)
$\alpha_{\max}/\alpha_{\min}$	1.36	1.26	1.35	1.53	1.73	1.87

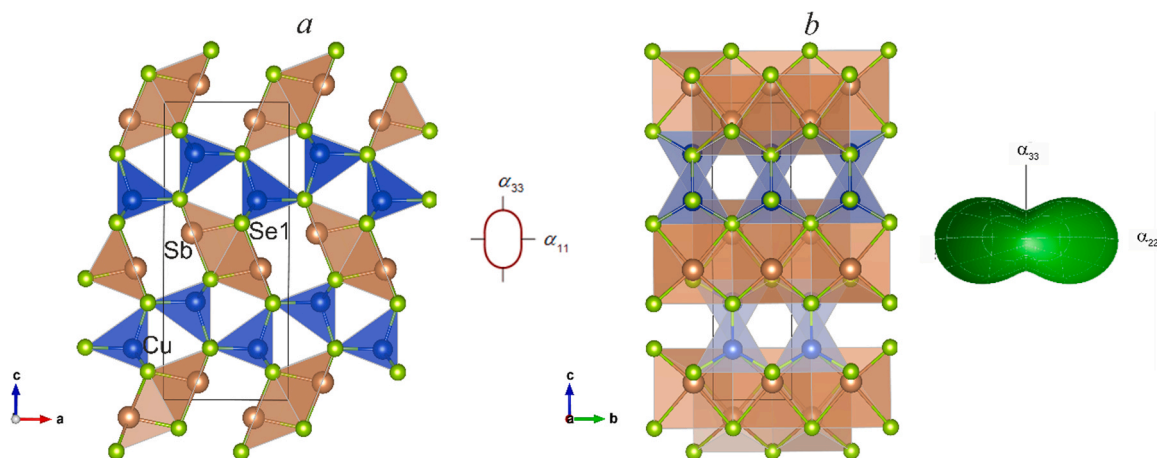


Fig. 11. The anisotropy of thermal expansion of CuSbSe_2 at 450 °C in the ac (a) and cb (b) planes in comparison to crystal structure.

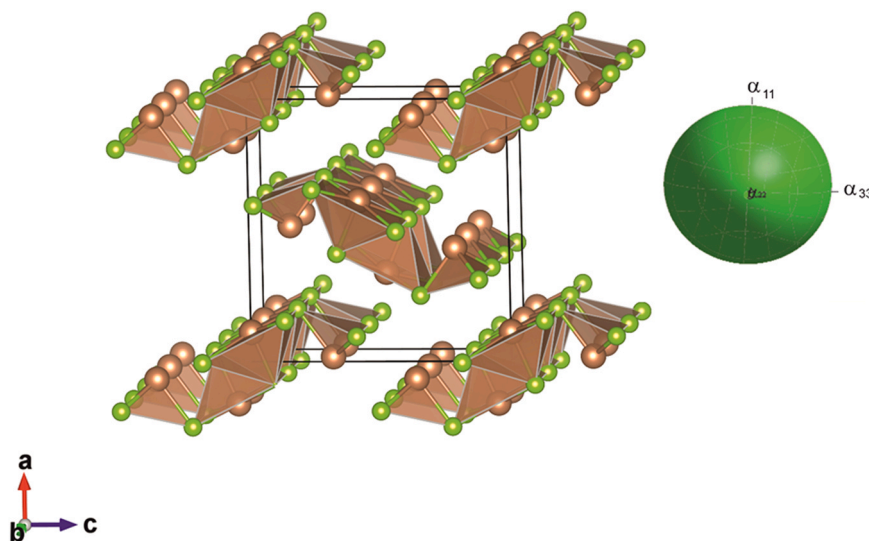


Fig. 12. General view of the Sb_2Se_3 crystal structure formed by the ribbons extending along the b axis (left) in comparison to thermal expansion tensor at 450 °C (right).

(2.702 Å and 3.202 Å) and therefore, this bond is the strongest. With an increase in temperature, the Cu–Se bonds in the CuSe_4 tetrahedra seem to elongate more than Sb–Se bonds in SbSe_5 pyramids, and the framework becomes distorted.

The thermal expansion is minimal in the ac plane especially along a axis due to the shortest and strongest Sb–Se1 bond (Fig. 11a) which is located about along this direction. The layers of CuSe_4

tetrahedra expand along the b axis direction and in this direction the thermal expansion is maximal (Fig. 11b).

Expansion between the layers is medium in the c direction. The nature of the strong anisotropy of thermal expansion up to negative within any area is described in detail in [103–106]. As a rule, a strong expansion along one direction causes a minimum up to a negative one in the perpendicular direction, and structure of CuSbSe_2

demonstrates similar anisotropy. The anisotropy of thermal expansion in the *ac* and *cb* planes at 450 °C in comparison to the crystal structure is shown in Fig. 11a and b, respectively. The anisotropy of thermal expansion of this selenide is similar to that of As₂S₃ (orpiment) [107].

The crystal structure of Sb₂Se₃ [31] consists of ribbons, containing two chains of SbSe₅ pyramids connected along the edges and chains of vertex-connected SbSe₃ distorted triangles in the projection on the *ac* plane (Fig. 12). The ribbons are elongated along the *b* axis (Fig. 12), and these ribbons are weakly bonded to each other. Therefore, with an increase in temperature, the expansion increases almost isotropically in the *ac* plane, while the expansion along the *b* axis slightly decreases because bonds along ribbons are very strong. It is notable that thermal expansion character of this selenide is similar to that of AsS realgar built up from isolated As₄S₄ molecules bonded by weak van der Waals interactions [107]. The average volume thermal expansion coefficient for both selenides ($\langle \alpha_V \rangle_2 = 30 \times 10^{-6} \text{ } ^\circ\text{C}^{-1}$) is smaller than average volume thermal expansion coefficient for both sulfides ($\langle \alpha_V \rangle_2 = 108 \times 10^{-6} \text{ } ^\circ\text{C}^{-1}$).

On heating, the anisotropy of thermal expansion (defined as ratio $\alpha_{\text{max}}/\alpha_{\text{min}}$ in Table 5) practically does not change for Sb₂Se₃ phase due to strong covalent bonds while it increases for CuSbSe₂ phase that may be caused by the presence of both covalent and ionic bonds.

The anisotropy of thermal expansion of the phase CuSbSe₂, distortion of the frame structure, and significant distortion of the CuSe₄ tetrahedra along the *b* axis determine the thermal instability of the CuSbSe₂ compound and increase its chemical activity. The interaction between the CuSbSe₂ and Sb₂Se₃ phases at 445 °C forms the ternary phase CuSb₃Se₅.

Three new diffraction peaks were recorded by HTXRD at temperatures of 470–480 °C. The values of *d* and 2θ for these peaks are shown in Fig. 9C. The main peaks of CuSbSe₂ and Sb₂Se₃ were also present on the diffraction pattern, but their unit cell parameters changed abruptly and in different directions (Fig. 10, isolated points). The diffraction patterns (Fig. 9) also contain several weak reflections with a lower intensity. Probably, weak peaks are caused by the appearance of impurity phases in the sample. Weak peaks could not be identified due to the small number and lack of information in diffractometric databases on suitable *d* values for phases from the Cu-Sb-Se-O system. The estimated content of these phases is no more than 0.5 mol%.

6. Properties of the CuSb₃Se₅ phase

An appreciable sublimation of the sample and an insufficient yield of the CuSb₃Se₅ did not allow us to obtain a complete X-ray diffraction pattern of this phase at 480 °C. Probably, in the CuSb₃Se₅ structure, the smaller number of CuSe₄ tetrahedra (the fourth part) prone to distortion determines the thermal stability of the phase.

The high-temperature phase CuSb₃Se₅ is stable over time. A sample containing 75 mol% Sb₂Se₃ was annealed at $t = 480 \pm 10 \text{ } ^\circ\text{C}$ during 4300 h in an evacuated and sealed quartz ampoule, which was at an angle to the horizontal line during annealing. Annealing resulted in the formation of a compact solid sample. If the CuSb₃Se₅ phase would decompose during annealing, then the Sb₂Se₃ crystalline phase and liquid should have been formed. In this case, the sample would have to spread over the ampoule. The sample did not separate into its component parts and remained compact during annealing. After cooling, the sample had the following phase composition: 47 mol% Sb₂Se₃, 41 mol% CuSbSe₂, 12 mol% Cu₃SbSe₃. The grain structure of the sample after cooling was similar to the grain structure of the sample after DSC (Fig. 8E).

Thus, HTXRD and annealing results for a sample containing 75 mol% Sb₂Se₃ at $480 \pm 10 \text{ } ^\circ\text{C}$ confirm the formation of the high-temperature phase CuSb₃Se₅.

The CuSbSe₂ and CuSb₃Se₅ phases do not form eutectic mixtures. The DSC curves for the samples containing from 50 to 71 mol% Sb₂Se₃ feature the following thermal events: CuSb₃Se₅ formation at 445 °C, incongruent melting of CuSbSe₂ at 478 °C, and melting of the crystals produced during incongruent melting of CuSbSe₂ (Fig. 5: sample (5)). The DSC curves contain exotherms of the following phase transformations: formation of CuSb₃Se₅ primary crystals at 480 °C, CuSbSe₂ formation at 430 °C, and superposition of peaks due to CuSb₃Se₅ decomposition and eutectic (1 Cu₃SbSe₃ + 8 CuSbSe₂) solidification at 424 °C. The liquidus temperature systematically and monotonically increases in the concentration range 50–71 mol% Sb₂Se₃.

7. Peculiarities of phase equilibria in the Cu_{2-x}Se-Sb₂Se₃ system in the concentration range 0–25 mol% Sb₂Se₃

The 2.00Cu:1.00Se-Sb₂Se₃ section in the concentration range 0–25 mol% Sb₂Se₃ crosses several subordinate systems of the Cu-Sb-Se triangle. In the sample containing 0.5 mol% Sb₂Se₃ (Fig. 13a) the Cu_{2-x}Se and Sb phases are present. Antimony Sb grains are located in the form of strips between the Cu_{2-x}Se grains. With an increase in the content of Sb₂Se₃, the samples become three-phase. The Cu_{2-x}Se phase binds an increased content of selenium, which is thus included in its composition. Selenium content is not sufficient to form the Cu₃SbSe₃ phase with stoichiometric composition. The elementary substance Sb is concentrated in the form of grains inside the Cu₃SbSe₃ phase (Fig. 13b). Samples from the 1.990Cu:1.000Se - Cu₃SbSe₃ and 1.970Cu:1.000Se - Cu₃SbSe₃ sections contain single antimony grains (Fig. 13c). Only in the 1.930Cu:1.000Se - Cu₃SbSe₃ section the presence of antimony as an elementary substance was not detected (Fig. 13d).

The presence of both low-temperature and high-temperature modifications of the Cu_{2-x}Se phase is observable on the diffraction patterns of the cooled samples, which confirms the formation of the Cu_{2-x}Se-based solid solution in the Cu-Sb-Se system (Fig. 7). The Cu₃SbSe₃ phase is most likely in equilibrium with a Cu_{2-x}Se-based solid solution of variable composition for X values: $1.97 \pm 0.01 < X \leq 1.93 \pm 0.01$. The content of copper and selenium in the Cu_{2-x}Se phase in each of the samples was determined by the SEM method for five to seven points on the sample surface. Average values are shown in Table 6. For two samples, the X values in the Cu_{2-x}Se phase composition were obtained, which are included in the mentioned above interval (Table 6).

The Cu_{2-x}Se-Sb₂Se₃ system phase diagram represents data for samples from 1.99Cu:1.00Se-Cu₃SbSe₃ section for two reasons.

Sample with stoichiometry 1.99Cu:1.00Se in the Cu_{2-x}Se-based solid solution area has a maximum melting point 1145 °C. The DSC-curves of samples from this section show a slight decrease (up to 5 °C) in the temperature of incongruent melting of the Cu₃SbSe₃ phase.

For samples from the 1.950Cu:1.000Se-Cu₃SbSe₃ and 1.930Cu:1.000Se-Cu₃SbSe₃ sections the peak of Cu₃SbSe₃ phase incongruent melting becomes blurred, its temperature drops by 10–20 °C.

8. Thermodynamic modeling using the Redlich-Kister polynomial

The liquidus consists of five segments. In each of the four segments, from 8 to 11 data points were obtained, and these segments were approximated by second-order or third-order polynomials. Since the eutectic lies in the area of more high concentrations of the refractory component, it was necessary to compare the results of thermal studies with the results of calculations.

From the Redlich-Kister polynomial for subsequent calculations of the liquidus line position, the expressions for the activity coefficients and chemical potentials of the components in the melt

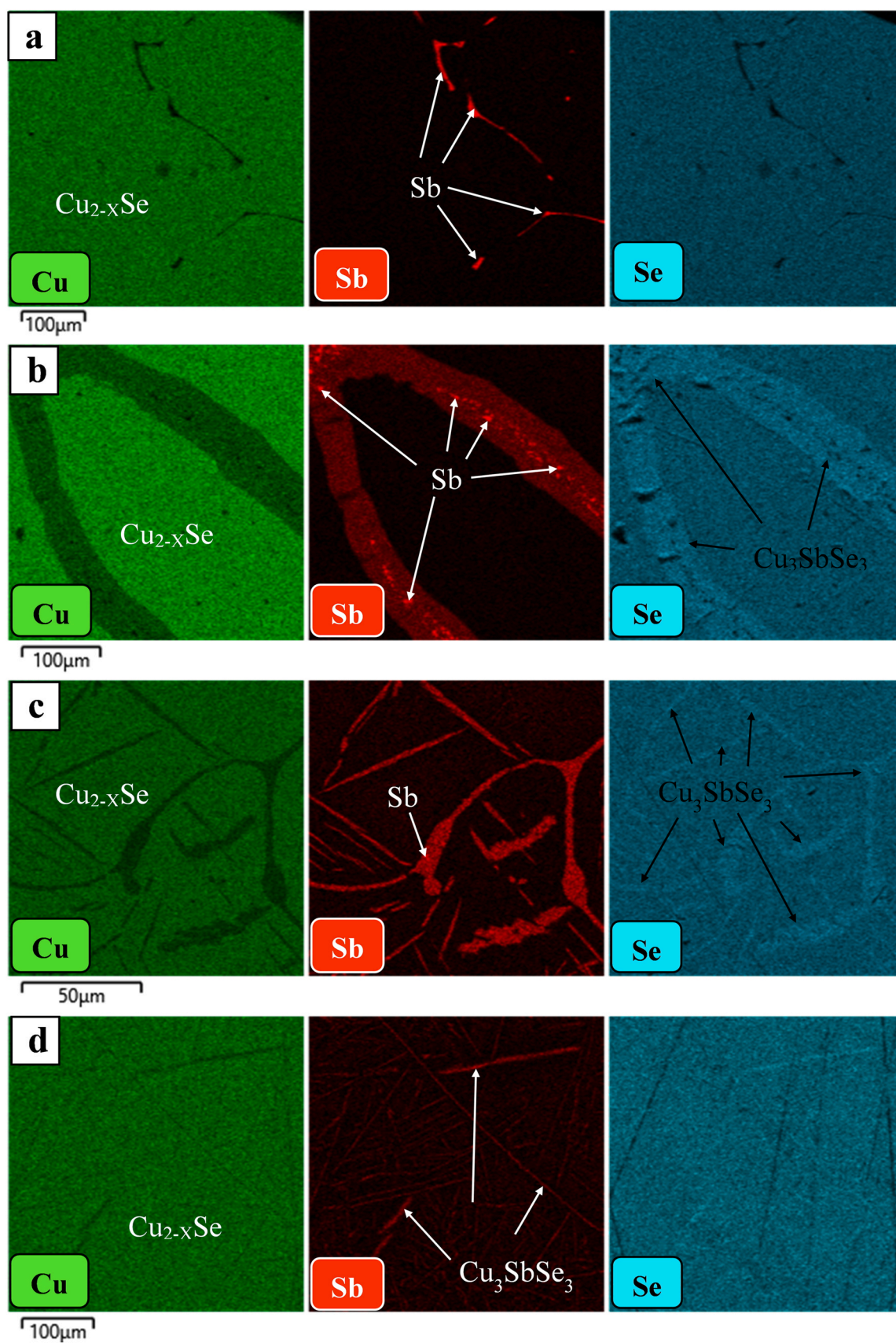


Fig. 13. SEM images illustrating the Cu, Sb, and Se concentrations in polished thin sections of annealed samples. Notations: as-batch (global) composition – phase composition. a – 99.5 mol% 2.00Cu:1.00Se 0.5 mol% Sb_2Se_3 – Cu_{2-x}Se , Sb; b – 95.0 mol% 2.00Cu:1.00Se 5.0 mol% Cu_3SbSe_3 – Cu_{2-x}Se , Cu_3SbSe_3 , Sb; c – 95.0 mol% 1.97Cu:1.00Se 5.0 mol% Cu_3SbSe_3 – Cu_{2-x}Se , Cu_3SbSe_3 , Sb (single grains); d – 95.0 mol% 1.93Cu:1.00Se 5.0 mol% Cu_3SbSe_3 – Cu_{2-x}Se , Cu_3SbSe_3 .

Table 6

Mass percentage of Cu and Se in the Cu_{2-x}Se phase according to weighted portion calculation data and SEM data.

	2.00 Cu: 1.00 Se	1.97 Cu: 1.00 Se	1.93 Cu: 1.00 Se
	Weighted portion calculation data		
Cu	61.56%	61.32%	60.83%
Se	38.44%	38.68%	39.17%
	SEM data		
Cu	61.3	60.3%	60.7%
Se	38.7	39.7%	39.3%
Cu _{2-x} Se phase composition according to SEM data	Cu _{1.97} Se	Cu _{1.89} Se	Cu _{1.92} Se

(solution) were obtained. This liquidus calculation model was successfully used to plot phase diagrams for similar systems [108–110].

The Redlich-Kister polynomial describes the variation of the excess Gibbs free energy and the activity coefficients of the components depending on the composition and temperature in the system. Molar excess Gibbs energy for a binary solution is expressed by the following Eq. (1):

$$\Delta G = x_1 x_2 \left[L_0 + L_1(x_1 - x_2) + L_2(x_1 - x_2)^2 + \dots \right] = x_1 x_2 \sum_{j=0}^k L_j (x_1 - x_2)^j \quad (1)$$

where x_1 and x_2 are the molar fractions of components in the melt and L_j are numerical factors (the interaction parameters).

The temperature effect on the excess thermodynamic functions of the liquid is taken into account in the equation for the excess Gibbs energy $RT \ln \gamma = \Delta G_m^E$ and is expressed by the equations for activity coefficients of the components while retaining the first three terms. The equations for activity coefficients of the binary solution components were obtained [70] (2), (3):

$$RT \ln \gamma_1 = (1 - x_1)^2 \left[L_0 + L_1(4x_1 - 1) + L_2(12x_1^2 - 8x_1 + 1) \right] \quad (2)$$

$$RT \ln \gamma_2 = x_1^2 \left[L_0 + L_1(4x_1 - 3) + L_2(12x_1^2 - 16x_1 + 5) \right] \quad (3)$$

where γ_1 and γ_2 are activity coefficients of the 1st and 2nd component, respectively; and L_0 , L_1 , and L_2 are numerical factors.

This is enough to write down expressions for chemical potentials and subsequently calculate the liquidus line of the system.

The chemical potentials of components may be expressed by the following equations:

$$\mu_1 = \mu_1^0 + RT \ln x_1 + (1 - x_1)^2 \left[L_0 + L_1(4x_1 - 1) + L_2(12x_1^2 - 8x_1 + 1) \right] \quad (4)$$

$$\mu_2 = \mu_2^0 + RT \ln x_2 + x_1^2 \left[L_0 + L_1(4x_1 - 3) + L_2(12x_1^2 - 16x_1 + 5) \right] \quad (4)$$

where μ_1^0 , μ_2^0 are standard chemical potentials of component 1 and component 2, respectively. Subscript "1" refers to Cu₂Se, and subscript "2" refers to Sb₂Se₃.

The temperature effect on the coefficients L for the melt is taken into account. The coefficients are found for a specific equilibrium temperature taken from the experimental data, thus taking into account its effect.

The entropy contribution to the stability of solid phases, of course, is present. But since the solid phases are stable and are being in equilibrium with the melt, this contribution for the equilibrium "solid component-melt" was not determined separately. The activity of the pure solid component is 1. The melting entropy contribution to the equilibrium is partially taken into account in Eq. (6) and subsequent transformations.

$$-RT \ln a_i = \frac{\Delta H_{m,i}(T_{m,i} - T)}{T_{m,i}}, \quad (6)$$

where a_i is activity of the i^{th} component in the melt, $\Delta H_{m,i}$ is enthalpy of melting of the pure i^{th} component, $T_{m,i}$ is melting temperature of the i^{th} component, and T is temperature of the equilibrium melt. Then, taking into account the generally accepted formula:

$$\mu = \mu^0 + RT \ln a, \quad (7)$$

for the first component we have

$$RT \ln a_1 = RT \ln x_1 + (1 - x_1)^2 \left[L_0 + L_1(4x_1 - 1) + L_2(12x_1^2 - 8x_1 + 1) \right] \quad (8)$$

and the expression for equilibrium becomes

$$\frac{\Delta H_{m,1}(T_{m,1} - T)}{T_{m,1}} = - \left[RT \ln x_1 + (1 - x_1)^2 \left[L_0 + L_1(4x_1 - 1) + L_2(12x_1^2 - 8x_1 + 1) \right] \right] \quad (9)$$

For example, the calculation equation for the equilibrium "melt-component Sb₂Se₃" at a temperature of 529 °C will look like:

$$\frac{\Delta H_{m,2}(T_{m,2} - T)}{T_{m,2}} = - \left[RT \ln x_2 + x_1^2 \left[L_0 + L_1(4x_1 - 3) + L_2(12x_1^2 - 16x_1 + 5) \right] \right] \quad (10)$$

where $\Delta H_{m,2}$ is the enthalpy of melting of the Sb₂Se₃ component, and $x_2 = 0.71$ and $x_1 = 0.29$ are, respectively, Sb₂Se₃ and Cu₂Se mole fractions at the equilibrium temperature $T = 527$ °C (800 K). Similar equations for phase equilibria in the other invariant points can be written (Table 3, Eqs. (1)–(5)) [108].

The melting enthalpies for the components of the system were obtained by DSC. The approaches described in the paper [111], where the thermal characteristics of complex chalcogenides were determined, were used. The temperature and enthalpy of melting for Sb₂Se₃ were found to be: $T_m = 612$ °C and $\Delta H_m = 50.2 \pm 5.8$ kJ/mol. These values nearly coincided with previously reported values: $T_m = 611$ °C [36], and $\Delta H_m = 50.2 \pm 4.2$ kJ/mol [37].

Samples of the copper semiselenide Cu_{2-x}Se based solid solution area were synthesized with the next ratios for elementary substances placed in ampoules: 2.000 Cu: 1.000 Se (1), 1.990 Cu: 1.000 Se (2), 1.970 Cu: 1.000 Se (3), 1.930 Cu: 1.000 Se (4). For samples (1) and (2), the melting peaks have a pronounced linear section, indicating the transition of the sample into a melt at a constant temperature. The rest of the samples melted within a certain temperature range. The melting enthalpies and melting temperatures, respectively, are: $\Delta H_m(1) = 9.7 \pm 1.1$ kJ/mol, $T_m(1) = 1143$ °C; $\Delta H_m(2) = 8.7 \pm 1.0$ kJ/mol, $T_m(2) = 1145$ °C; $\Delta H_m(3) = 5.2 \pm 1.0$ kJ/mol, $T_m(3) = 1108$ –1135 °C; $\Delta H_m(4) = 4.7 \pm 1.0$ kJ/mol, $T_m(4) = 1087$ –1132 °C.

The values determined for the enthalpies of melting agree, within the determination error, with the values reported for Cu₂Se $T_m = 1117$ °C, and $\Delta H_m = 9.055$ kJ/mol [25]. To calculate the liquidus line according to the obtained equations, we used the data for the sample (2).

The solution of the equations system gave the following numerical values: $L_0 = -15,390$, $L_1 = 24,400$, and $L_2 = -27,740$. The liquidus line was calculated for each range as a temperature versus composition function. The calculated liquidus is shown by the dashed line in Fig. 5.

The discrepancy between the liquidus curve plotted by fitting DSC data and the curve calculated by the Redlich-Kister method is 1–13 °C in the range 0–32 mol% Sb₂Se₃, 1–7 °C in the range 32–45 mol% Sb₂Se₃, and 1–3 °C in the range 71–100 mol% Sb₂Se₃. The largest discrepancy (1–17 °C) was observed in the range 46–71 mol% Sb₂Se₃. The calculated liquidus is a convex curve, that is the most frequent type of liquidus. The experimental liquidus shows

an insignificant concavity. The trend of the liquidus in that range correlates with the existence of the unstable high-temperature phase CuSb_3Se_5 , whose primary crystals are formed upon cooling precisely in the range 46–71 mol% Sb_2Se_3 . In general, the results of the calculation of the liquidus line using the Redlich-Kister polynomial obtained from the data for phase equilibria at invariant points of the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system agrees with the DSC data, supporting the correctness of the phase diagram.

Comparison of the obtained $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system phase diagram with literature data (Figs. 2 and 5).

In the present work, like in [39] and [40], the existence of the CuSbSe_2 compound, which forms a eutectic towards the Cu_{2-x}Se component, is confirmed. Like the author of [19], we confirmed the existence of three ternary compounds in the system, including the high-temperature phase CuSb_3Se_5 . In this paper, for the first time, the thermal characteristics of phases, a number of their properties, and the position of phase equilibrium lines in $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ systems are presented.

9. Conclusions

The re-determination of the phase diagram in this system combined with a careful characterization of all the phases in the system by a complex of instrumental techniques helped to resolve the discrepancy in the earlier published results [19,30,39,40,47].

We have confirmed unambiguously that the three ternary compounds Cu_3SbSe_3 , CuSbSe_2 , CuSb_3Se_5 – can exist in the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system. The formation of CuSb_3Se_5 was proved by high-temperature X-ray diffraction of a sample containing 75 mol% Sb_2Se_3 and 25 mol% Cu_2Se . During the experiment the sample sublimed, and the completeness of the reaction was not high enough, therefore the diffraction data from the small amount of the CuSb_3Se_5 phase were not sufficient to solve its structure. A high-temperature X-ray diffraction study of the sample containing 75 mol% Sb_2Se_3 and 25 mol% Cu_2Se allowed us to follow the anisotropy of thermal expansion of the CuSbSe_2 and Sb_2Se_3 phases. Volume thermal expansion, α_V , gradually increases for both selenides within the range under study. For both selenides the increase in volume expansion is caused by rising thermal atomic vibrations. The anisotropy of thermal expansion of CuSbSe_2 and Sb_2Se_3 was similar to those of the well-studied As sulfides, As_2S_3 and AsS , respectively.

The up-dated phase diagram obtained in our work now takes into consideration the existence of all the three compounds (Cu_3SbSe_3 , CuSbSe_2 and CuSb_3Se_5) and their participation in the phase equilibria. The phase identities were proven by a complex of methods including structure solution and refinement by single-crystal X-ray diffraction, powder X-ray diffraction, measurements of the energy bandgaps. The exact range of the existence of $\text{Cu}_{10.53}\text{Sb}_{33.78}\text{Se}_{55.68}$ was found from the DSC and high-temperature X-ray diffraction; previously it was only roughly estimated [19]. Six balance equations of the invariant phase transformations were suggested, that take into account the participation of all the three ternary compounds in the $\text{Cu}_{2-x}\text{Se-Sb}_2\text{Se}_3$ system. In the system, the Cu_3SbSe_3 phase is in equilibrium with the Cu_{2-x}Se solid solution of non-stoichiometric composition. The temperatures and the enthalpies of these invariant transformations were determined. The liquidus curve is calculated for this system using Redlich-Kister polynomial coincided within 1–17 °C with the DSC data. The consistence of the results obtained by many independent methods allow us to consider that new phase diagram obtained in the present work as reliable.

CRediT authorship contribution statement

M.A. Shtykova: Data curation, Visualization, Supervision, Project administration, Writing – original draft. **M.S. Molochev:** Formal analysis. **B.A. Zakharov:** Investigation, Resources, Methodology,

Formal analysis, Visualization, Data curation, Funding acquisition. **N.V. Selezneva:** Investigation, Formal analysis, Resources. **A.S. Aleksandrovsky:** Formal analysis, Writing – review & editing, Validation. **R.S. Bubnova:** Software, Formal analysis, Visualization, Funding acquisition. **D.N. Kamaev:** Formal analysis, Visualization. **A.A. Gubin:** Investigation, Resources. **N.N. Habibullaev:** Investigation, Visualization, Data curation. **A.V. Matigorov:** Resources, Investigation. **E.V. Boldyreva:** Supervision, Writing – review & editing, Validation, Data curation. **O.V. Andreev:** Conceptualization, Methodology, Software, Validation, Resources, Data curation, Writing – original draft, Project administration, Funding acquisition, Supervision.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary material

Supplementary data associated with this article can be found in the online version at [doi:10.1016/j.jallcom.2022.164384](https://doi.org/10.1016/j.jallcom.2022.164384).

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