

Cationic Disorder in Co₂AlBO₅: Effects on Magnetic and Electrical **Properties**

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1. INTRODUCTION

The disorder is a driving force throughout many of the highestprofile phenomena of solid-state physics. Frustrations of exchange interactions play a central role in low-dimensional magnets.¹ Competing antiferromagnetic exchange interactions between localized magnetic moments so that all exchanges cannot be satisfied simultaneously can prevent magnetic ordering down to very low temperatures and may even stabilize unconventional forms of ordering, such as spin liquid or noncollinear magnetic structure.^{2,3} The high-zT thermoelectric materials achieve reduced lattice thermal conductivity through disorder within the unit cell.⁴ Recently, it was reported about an unprecedentedly low thermal conductivity in layered compound AgCrSe₂ due to disordered silver atoms over two tetrahedral sites and a large Seebeck coefficient.⁵ Such a remarkable combination of properties leads to a thermoelectric figure of merit higher than 1 and opens the route to the discovery of efficient thermoelectric materials. In relaxors, the polarization is correlated on a local scale, resulting in the appearance of polar nanometer-sized regions (PNR) closely related to the structural and charge inhomogeneities. The PNRs generated from the disorder are found in all relaxors, whereas the structural or atomic origin may be different.^{6–8}

Ludwigites with the general formula Me₃BO₅ belong to the family of intrinsically disordered systems.9 These materials might be expected to exhibit structural disorder. One of the reasons is the atomic instability lying in the crystal structure itself, which contains cationic and anionic positions with a large displacement amplitude. Atomic instability is most pronounced in homometallic ludwigites and results in electronic and structural phase transitions in Fe₃BO₅. This phenomenon was extensively studied using X-ray and neutron diffraction methods, as well as Mössbauer spectroscopy.¹⁰⁻¹² Above T_{CO} = 283 K, the Fe2 cation presents a strongly anisotropic atomic displacement parameter along the rung Fe4–Fe2–Fe4, while below T_{CO} , this parameter drastically decreases, and the Fe2 cation is displaced toward Fe4, forming dimers alternating in a zigzag way along *c*-axis. These structural transformations are accompanied by a charge-order-disorder transition and the localization of an extra electron at the rung. Anomalies in the electrical resistivity and the semiconductorsemiconductor transition occur with decreasing activation energy. However, the atomic, charge, and structural stabilities have been found in Co₃BO₅ that have become the subject of intense discussions in recent decades.^{13,14} By applying neutron powder diffraction, X-ray diffraction, X-ray absorption spectroscopy, heat capacity, electrical resistivity, and magnetic susceptibility measurements, as well as theoretical calculations in the framework of density functional theory (DFT), it was shown that the low-spin state of Co³⁺ ions prevents charge hopping, stabilizing structural and charge ordering and thereby avoiding structural phase transitions.^{15–18} When heated above 500 K, the thermal energy becomes sufficient to overcome the

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spin gap, and spin state crossover occurs. In Co_3BO_5 , the interconnection between the electronic and lattice degrees of freedom is manifested in the coupled behavior of the electrical resistivity and thermal expansion. Thus, ludwigites exhibit a variety of physical phenomena, stemming from the delicate concert of trade-offs between structural order and disorder, charge ordering and disordering, and atomic stability and instability.

The great diversity of possible combinations of Me^{2+} and Me^{3+} ions provides an opportunity to study the intriguing electronic and magnetic properties of heterometallic ludwigites. Such systems can offer particularly attractive physical properties, including high crystallographic anisotropy, anomalous thermal expansion, magnetic dimensional crossover, and charge localization-delocalization phenomena. By substitution, it is possible to introduce sufficient disorder within the crystalline framework and to impact the system's ability to achieve an ordered state. Most of the research has focused on magnetic characterization, such as cascade phase transitions in Co_2FeBO_5 , $^{19}Ni_2FeBO_5$, $^{20}Cu_2MnBO_5$, 21 and $Fe_{3-x}Mn_xBO_5$, whereas the origin of cationic disorder remains to be investigated.

Al-substituted ludwigites possess the highest cationic disorder and are candidates for studying this effect. Medrano et al. reported on the emergence of ferrimagnetism at $T_{\rm N}$ = 57 K and the metamagnetic transition at 25 K in $Co_{2.38}Al_{0.62}BO_5^{23}$ The magnetization, heat capacity, and dielectric constant measurements of Co₂AlBO₅ revealed that long-range magnetic order occurs at $T_{\rm N}$ = 42 K and that the superglass state is at $T_{\rm G}$ = 10.6 K.²⁴ Although Co_2AlBO_5 has been characterized from a magnetic point of view, there are discrepancies in both the interpretation of the magnetic ground state and the transition temperature itself. The present work undertakes the synthesis of a Co₂AlBO₅ single crystal by flux and the magnetic and electronic properties were studied, with an emphasis on highlighting how cationic disorder can give rise to unusual physical properties in this long-established class of materials. We used the inversion degree parameter as a means of characterizing disorder, and we suggest that this disorder might be tuned through the rich structural chemistry of this family.

2. EXPERIMENTAL METHODS

2.1. Synthesis. Single crystals of Co_2AlBO_5 were grown using a bismuth trimolybdate-based flux, in which Bi_2O_3 is strongly bonded to MoO_3 , excluding the former entering the crystal. The system was: 71.3% mass $[Bi_2Mo_3O_{12} + Na_2O + 2.7 \cdot B_2O_3 + 0.1 \cdot CoO] + 28.7\%$ mass $[Co_2AlBO_5]$.

Flux with a weight of 30 g was prepared in a 100 cm³ platinum crucible by sequential melting of B₂O₃, Bi₂Mo₃O₁₂, Co₃O₄, and Al₂O₃, and finally, the powder of Na₂CO₃ was added in portions at 1100 °C. The excess amount of B_2O_3 (20%) was determined through preliminary calcination at 400 °C and subsequent weighing. The crucible with melted solution was rapidly cooled to 1000 °C and kept for 6 h to ensure that the powder melted into a homogeneous solution. After that, the temperature was reduced to T_{cr} = 920 °C, followed by slow cooling at 4 °C/day. After 2 days, the growth was completed, and the liquid solution melt was poured out. The single crystals grown on the walls and at the bottom of the crucible were separated by etching in a 20% solution of nitric acid. The crystals are well cut into rectangular prisms of black color with a shiny surface (Figure S1). The thin crystals are brown in color. The crystal length is up to 7 mm, and the cross-section size is about 0.4×0.4 mm². In the temperature range of $(T_{cr} - 30)$ °C < T < T_{cr} , the Co₂AlBO₅ ludwigite is only crystallizing phase. At T < 890 °C, blue-violet crystals were observed and identified as pyroborate.

2.2. Structure Determination. A single crystal of Co₂AlBO₅ was selected for structure determination. X-ray diffraction patterns were collected at 296 K using a SMART PHOTON II single-crystal diffractometer (Bruker AXS) equipped with a PHOTON II CCD-detector, graphite monochromator, and Mo K α radiation source. The structure was solved by direct methods using the SHELXT program.²⁵ The structure refinement was carried out by least-squares minimization in the SHELXL program using the anisotropic thermal parameters of all atoms.²⁶

2.3. Composition Analysis. To study the chemical composition of the grown crystals, X-ray microfluorescence analysis (micro-XRF) was carried out. The "Area" mode was used for quantitative analysis using an M4 TORNADO X-ray spectrometer (Bruker), which allows for mapping of the selected areas of the sample surface. According to a given number of points, statistics are collected and averaging and quantitative analysis are used for the determination of the concentrations of different chemical elements. The one-point mode measurements were carried out with an accumulation time of 150 s. The content-determining error of the main elements was $\approx 0.5\%$, and impurities with a content of less than 0.5% were determined qualitatively.

2.4. Magnetic Measurements. For magnetic measurements, a single crystal of 0.48 mg was selected. The sample was preliminarily oriented by using a single-crystal diffractometer and placed in a sample holder with the help of a microscope. The dc magnetization measurements were performed using a Quantum Design Physical Properties Measurement System (PPMS) with a maximum field of 90 kOe. The external magnetic field was applied directed parallel to the b- and c-axes.

2.5. Electrical Resistivity Measurements. Owing to the large size and rectangular shape of the grown crystals, it was possible to measure the electrical resistivity of Co_2AlBO_5 ludwigite. The measurements were performed in the temperature range of 400–870 K using an experimental setup for thermo-power and resistivity measurements.²⁷ The DC resistivity was measured along the *c*-direction with a standard four-point configuration. The heating/ cooling rate was 6 K/min.

3. RESULTS

3.1. Crystal Structure. The structure refinement parameters and detailed crystallographic data are summarized in Table 1. The fractional coordinates, site occupation factors, anisotropic displacement parameters, and main bond lengths are listed in the Supporting Information (Tables S1-S4). Co₂AlBO₅ crystallizes in orthorhombic symmetry, in the space group Pbam (No.55), and the lattice parameters are in good agreement with those reported earlier.^{23,24,28} There are four symmetry inequivalent metal sites, M1 (2a), M2 (2d), M3 (4g), and M4 (4h); one boron site, B (4h); and five oxygen sites, O1-O5 (4g, 4h) (Figure 1a). The Co and Al ions share four metal sites with occupation factors Co:Al = 0.78:0.22 (M1), 0.53:0.47 (M2), 0.86:0.14 (M3), and 0.50:0.50 (M4). The refined formula $Co_{2,02}Al_{0.98}BO_5$ is in agreement with the X-ray microfluorescence analysis results, showing the high uniformity of the metal ion distribution (Figure S2). The ludwigite crystal structure can be presented as a framework consisting of octahedral layers in the bc-plane built on the M1, M2, and M3 sites, which are separated along the a-axis by M4O₆ octahedra and BO₃ triangles.

The local octahedral distortions were estimated through the calculations of the main component of the electrical field gradient tensor (V_{zz}) .²⁹ The local oxygen coordination of metal ions exhibits two types of highly distorted octahedra: M1O₆ and M3O₆ preferably occupied by Co²⁺ ions (78 and 86%, respectively) have coordination, forming axially compressed octahedra and showing the largest values of V_{zz} (0.210 and

Table 1. Crystal Data and Structure Refinement for Co_2AIBO_5

	Crystal Data
space group, Z	Pbam(55), 2
size (mm ³)	$0.420 \times 0.220 \times 0.190$
T (K)	296
a (Å)	9.2072(3)
b (Å)	12.0676(4)
c (Å)	3.00170(10)
V (Å ³)	333.515(19)
$D_{\rm x} ({\rm mg/m^3})$	4.694
$\mu \ (\mathrm{mm}^{-1})$	2.645
	Data Collection
wavelength	Mo K α , $\lambda = 0.71073$ Å
measured reflections	6803
independent reflections	1036
reflections with $I > 2\sigma(I)$	851
absorption correction	multiscan
R _{int}	0.0330
$2\theta_{\rm max}$ (deg)	75.96
Н	$-15 \rightarrow 15$
Κ	$-20 \rightarrow 20$
L	$-5 \rightarrow 5$
	Refinement
$R[F^2 > 2\sigma(F^2)]$	0.0269
$wR(F^2)$	0.0622
S	1.171
weight	$w = 1/[\sigma^2(F_o^2)] + (0.0186P)^2 + 0.3149P$

0.233 e/Å³, respectively). On the contrary, the M2O₆ and M4O₆ octahedra are slightly distorted ($V_{zz} = 0.076$ and -0.030 e/Å³, respectively). The reason for the difference is, obviously, the different boron coordination: four boron atoms coordinate the M1 and M3 sites and only two ones coordinate the M2 and M4 sites, causing considerable elongation of the appropriated Me–O bond length (Table S3).

3.2. Magnetic Properties. Figure 2 displays the temperature-dependent magnetization curves of the Co₂AlBO₅ single crystal in the field of 600 Oe directed along the *b*- and *c*-axes. The *dc* magnetization along the *b*-axis shows a maximum at T_1 = 41 K, which is close to the value of T_N = 42 K obtained by Kumar et al.,²⁴ and can be attributed to the onset of long-range magnetic order. Below T_1 , a progressive divergence of the FC and ZFC curves is observed. A low-temperature magnetic



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Figure 2. Temperature-dependent dc magnetization curves of Co_2AIBO_5 measured in a field of 600 Oe along the *b*- and *c*-axes. The full and empty symbols denote the FC and ZFC measurement regimes, respectively. The magnetic transitions are indicated by arrows. Inset: FC magnetization vs temperature measured along the *b*- axis in a field of 50 kOe.

anomaly occurs near $T_2 = 20$ K, which is somewhat higher than that at $T_G = 10.6$ K.²⁴ In high magnetic fields, the difference between the FC and ZFC curves rapidly decreases and the anomaly at T_1 is smeared and becomes indistinguishable against the growing ferromagnetic moment in a field of 50 kOe (inset to Figure 2). Importantly, the magnetic transitions are clearly identified in the magnetization curves along the *b*-axis, and almost no transitions are visible along the *c*-axis is almost an order of magnitude smaller than that along the *b*-axis. This behavior indicates the high crystallographic anisotropy inherent in cobalt-containing ludwigites, which is due to the large single-ion anisotropy of Co²⁺ ions.^{15,17,30}

At high temperatures (T > 150 K), the susceptibility follows a Curie–Weiss behavior and the data can be approximated by the sum of a temperature-independent term χ_0 and the Curie– Weiss term $\chi_{CW} = C/(T - \theta)$ (Figure 3). Fitting the data yields the parameters listed in Table 2. The obtained values of χ_0 are in good agreement with the summation of Pascal's constants for the ions constituting Co₂AlBO₅ ($\chi_{dia} = -0.61 \times 10^{-4}$ emu/ mol)³¹ and the van Vleck contribution of Co²⁺ ions in octahedral coordination ($\chi_{vV} = 12 \times 10^{-3}$ emu/mol).^{32,33} Negative values of the Weiss temperature θ indicate the predominance of antiferromagnetic interactions. The exper-



Figure 1. (a) Crystal structure of Co_2AIBO_5 in *ab*-projection. The inequivalent metal sites 2*a*, 2*d*, 4*g*, and 4*h* are numbered as M1, M2, M3, and M4, respectively. (b) BO₃-triangle. (c) Ellipsoid of thermal vibrations of the O4 atom surrounded by metal atoms.



Figure 3. Temperature dependence of the inverse magnetic susceptibility $(\chi - \chi_0)^{-1}$ of the Co₂AlBO₅ single crystal for the *H* parallel *b*-axis. The straight line represents the Curie–Weiss fit.

imental data deviate significantly from the Curie–Weiss fit at T < 150 K. The progressively increasing relevance of the antiferromagnetic correlations upon cooling leads to the onset of magnetic order at T_1 . The Curie constant C yields an effective magnetic moment $\mu_{\text{eff}}^b = 7.04 \pm 0.05 \mu_{\text{B}}$ per formula unit, which corresponds to a moment of 4.97 \pm 0.02 $\mu_{\rm B}$ per Co²⁺ ion. The obtained value is in agreement with those for cobalt borates ($\mu_{\rm eff} = 4.0-5.2 \ \mu_{\rm B}$)¹⁷ and exceeds the spinonly one, 3.87 $\mu_{\rm B}$. One can conclude that in Co₂AlBO₅ under consideration, the Co^{2+} ions are in the high-spin state with a significant unquenched orbital moment. The μ_{eff}^c value is depressed, implying strong magnetic anisotropy. The presence of some Co³⁺ ions in the Co_{2.38}Al_{0.62}BO₅ sample²³ gives an uncertainty in the effective moment value due to the lack of information about their spin state. Nevertheless, an estimated value of μ_{eff} per Co ion of 5.15 μ_{B} still falls within the range of the expected values. The magnetic moment of 3.5 $\mu_{\rm B}$ reported for the Co₂AlBO₅ sample in ref 24 is smaller than that obtained in the present work.

The field dependences of the magnetizations of Co₂AlBO₅ measured for two directions of the external fields are shown in Figure 4. For the field applied along the *c*-direction, the magnetization curves are linear at all temperatures as expected for the antiferromagnet, while for the b-direction, the magnetization curves show temperature-induced evolution (inset to Figure 4). The high-field branches of the b-axis M(H) are not saturated and have a slope, probably due to an antiferromagnetic component. At $T < T_1$, all curves tend to the same high-field limit (~2.0 $\mu_{\rm B}$ /f.u.), assuming the presence of a magnetically disordered sublattice, which is affected by the ordered one. At $T < T_{2}$, the hysteresis loop opens, indicating that a noncompensated magnetic moment appears. The magnetic structure of ludwigites is complex and, in the first approximation, contains four magnetic sublattices assigned to inequivalent metal sites. The bulk magnetization is the sum of the partial contributions of the magnetization sublattices. The shape of the hysteresis loop reflects the dilution degree of these sublattices by nonmagnetic Al3+ and can differ for different



Figure 4. Field dependencies of the magnetization of the Co_2AIBO_5 single crystal over a temperature range of 4.2-100 K in the *b*-direction. The inset shows the hysteresis loops measured at T = 4.2 K and an external field applied along the *b*- and *c*-directions.

samples.^{23,24} The coercive field H_c increases as the temperature decreases, with a maximal H_c of \approx 8.0 kOe at 4.2 K.

3.3. Electrical Resistivity. The electrical resistivity of the Co_2AlBO_5 single crystal as a function of the temperature is shown in Figure 5. At room temperature, the sample resistivity



Figure 5. Resistivity of the Co_2AIBO_5 single crystal as a function of the inverse temperature. The black solid line is a linear approximation. The inset shows the temperature dependence of the electrical resistivity.

is extremely large. In fact, up to T = 400 K, the resistivity cannot be accurately measured. Above this temperature, the resistivity becomes measurable and decreases by approximately 4 orders of magnitude as the temperature increases to 870 K. Assuming that the high-temperature conductivity is due to thermally activated hopping of the carriers, the relation between the electrical resistivity and the inverse temperature is linear and yields an activation energy $E_a = 0.57 \pm 0.01$ eV. Note that Co₃BO₅ undergoes two electronic transitions: the low- to high-spin-state transition of Co³⁺ at $T_s = 500$ K, followed by the semiconductor-semiconductor transition at T_{el}

Table 2. Magnetic Parameters of Co₂AlBO₅ Extracted in the Paramagnetic Phase

	$\chi_0 \ (emu/mol)$	C (emu·K/mol)	$\mu_{\mathrm{eff}} \left(\mu_{\mathrm{B}}/\mathrm{Co}^{2+} \right)$	θ (K)
<i>b</i> -axis	$(7.4 \pm 0.5) \times 10^{-3}$	6.2 ± 0.1	4.97 ± 0.02	-14.5 ± 0.5
c-axis	$(19 \pm 1.0) \times 10^{-3}$	1.8 ± 0.3	2.68 ± 0.20	-27.0 ± 1.0

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Table 3	3. Site	Occupancies	for the	Four	Inequivalent	Metal	Sites in	Cobalt-	-Aluminum	Ludwigites

M1	M2	M3	M4	refs
Co (88%) + Al (12%)	Co (67%) + Al (33%)	Co (100%)	Co (60%) + Al (40%)	23
Co (81%) + Al (19%)	Co (55%) + Al (45%)	Co (70%) + Al (30%)	Co (46%) + Al (54%)	24
Co (78%) + Al (22%)	Co (53%) + Al (47%)	Co (86%) + Al (14%)	Co (50%) + Al (50%)	p.w.
^{<i>a</i>} The destinations of the metal si	ites are consistent with those in	the present work (p.w.) and ar	e shown in Figure 1.	

= 700 K, with a significant decrease in the activation energy from $E_{\rm a} = 0.50 \pm 0.02$ to 0.28 ± 0.02 eV.¹⁷ The Co₂AlBO₅ resistivity data obtained within the same temperature interval did not reveal any anomalies in the $\rho(T)$ curve.

4. DISCUSSION

The compound under investigation inherited the main distinctive property of the Co-containing borates: strong magnetocrystalline anisotropy, the source of which is the large single-ion anisotropy of Co^{2+} ions. The analysis of the local distortions showed that Co^{2+} ions are coordinated by strongly distorted oxygen octahedra. If the symmetry of the crystal field is not cubic, the ground state of Co^{2+} ions is described, taking into account the spin—orbit coupling, by two Kramers doublets separated by about 100 cm⁻¹. At high temperatures, the system is characterized by the effective spin S = 3/2 and a small orbital contribution, which corresponds to an effective moment of about $4.97 \mu_{\rm B}$. The population of the lowest Kramers doublet at low temperatures leads to an orbital contribution from the nearest level and a large anisotropy of the g-factor.

Although the temperature of the magnetic phase transition $T_1 = 41$ K almost does not change compared to that of Co_3BO_5 ($T_{\text{N}} = 42$ K¹⁵), the aluminum substitution effect is clearly identified through the appearance of an additional transition under cooling ($T_2 = 20$ K). The frequency-dependent behavior of the low-temperature anomaly confirmed by the results of the imaginary part of the *ac* susceptibility has been attributed to the spin-glass transition.²⁴ It is worth noting that similar behavior as well as bifurcation of the ZFC and FC magnetizations are also expected from the formation of domain walls in the ordered magnetic phase or from the spin-reorientation transition (metamagnetic transition, for instance, ref 23). Therefore, the nature of the low-temperature transition is still an open issue.

The hysteresis loop opening and rapid growth of the magnetic moment along the b-axis are probably due to the reorientation of one or several magnetic sublattices, which are weakly antiferromagnetically coupled, or their magnetic ordering. The diamagnetic dilution apparently results in the weakness of magnetic couplings, which the external magnetic field is capable of overcoming. The magnetically diluted sublattices either remain in a paramagnetic state below T_1 or make a small contribution to the magnetic order due to weak antiferromagnetic correlations. The difference in the magnetic behaviors, including the temperatures of the magnetic phase transitions, probably originates from the difference in the cationic distribution. These distributions are listed in Table 3. The cationic distribution of Co2AlBO5 determined in the present work is very close to that reported by Kumar et al.²⁴ The occupation of the M3 site by the Al atoms should induce a significant dilution of the M3-M1-M3 magnetic unit possessing the strongest antiferromagnetic coupling and, as a consequence, the weakness of the superexchange interactions. In contrast, the filling of the M3 site by magnetic Co^{2+} ions favors

strengthening of the superexchange interactions, increasing the magnetic ordering temperature ($T_N = 57 \text{ K}^{23}$).

From an experimental viewpoint, cationic disorder has a number of observable consequences. A comparison of Co₂AlBO₅ with the isostructural orthoborates Co₃BO₅ and Co2.5Ge0.5BO5 could be very helpful for understanding this effect. In terms of cationic disorder, Co₃BO₅ is a rare example of a no-disorder compound, whereas Co2.5Ge0.5BO5 and Co₂AlBO₅ are the analogues of the one-site and all-site disorder compounds. In $Co_{2.5}Ge_{0.5}BO_5$, the Ge^{4+} and Co^{2+} ions share the M4 site in the ratio of Co:Ge = 0.5:0.5, making this site structurally disordered. The magnetically active Co²⁴ ions directly participate in the establishment of long-range antiferromagnetic order instead of the nonmagnetic LS Co³⁺ ions in Co₃BO₅, providing exchange interactions between adjacent $[Co^{2+}O_6]_{\infty}$ -layers (M1, M2, and M3 sites). The antiferromagnetic order onsets at a high temperature ($T_{\rm N} = 84$ K). In Co₂AlBO₅, all metal sites are structurally disordered, and magnetic order appears at a much lower temperature, $T_1 =$ 41 K. The second magnetic transition occurs at $T_2 = 36$ K for germanium and 20 K for aluminum samples. The T_2 value is seemingly affected by the cationic distribution, as well.

Perhaps the most important effect of cationic disorder is the change in magnetic permeability, which transforms toward extraordinary magnetic hardness in the Ge-substituted sample and toward significant softness in the Al-substituted sample (Figure 6). To study this effect, we have carried out



Figure 6. Hysteresis loops measured along the *b*-axis for Co₃BO₅ (T = 4.2 K),¹⁵ Co_{2.5}Ge_{0.5}BO₅ (T = 6 K),³⁰ and Co₂AlBO₅ (T = 4.2 K).

magnetization measurements on single crystals under the same temperature, field, and magnetic field orientation conditions. The $H_c{}^bM_r$ parameter, where $H_c{}^b$ is the coercive field along the *b*-axis and M_r is a remanent magnetization, is designed to describe a mechanism of 180° domain walls and equals $3.98 \times 10^6 G^2 (T = 4.2 \text{ K})$ for Co_{2.5}Ge_{0.5}BO₅,³⁰ and only $3.02 \times 10^5 G^2 (T = 4.2 \text{ K})$ for Co₂AlBO₅. Thus, the all-site cationic disorder induces the compound to become magnetically soft, while the

	M1	M2	M3	M4	В	Σ	\sum /C.N. ^b	
01	0.445 $\frac{\times 1 \rightarrow}{\times 2 \downarrow}$		$0.512 \xrightarrow[\times1 \rightarrow]{\times1}$	$0.516 \xrightarrow{\times 2 \rightarrow}{\times 2 \downarrow}$		1.989	0.497	
O2			$0.306 \xrightarrow{\times 2 \rightarrow}{\times 2 \downarrow}$	$0.416 \xrightarrow{\times 1 \rightarrow}{\times 1 \downarrow}$	0.953 $\frac{\times 1 \rightarrow}{\times 1 \downarrow}$	1.981	0.495	
O3	$0.322 \xrightarrow{\times 2 \rightarrow}{\times 4 \downarrow}$			$0.392 \xrightarrow[\times1]{\times1}_{\times1\downarrow}$	1.008 $\frac{\times 1 \rightarrow}{\times 1 \downarrow}$	2.044	0.511	
O4		$0.385 \xrightarrow{\times 2 \rightarrow}{\times 4 \downarrow}$	$0.375 \xrightarrow{\times1 \rightarrow}{\times1 \downarrow}$	$0.349 \xrightarrow{\times 2 \rightarrow}{\times 2 \downarrow}$		1.843	0.369	
05		$0.433 \xrightarrow[\times 2]{\times 1} \xrightarrow{\times}$	$0.303 \xrightarrow{\times 2 \rightarrow}{\times 2 \downarrow}$		$0.995 \xrightarrow[\times1]{\times1}_{\times1\downarrow}$	2.034	0.509	
	2.178	2.406	2.105	2.538	2.956			
^{<i>a</i>} The calculation	The calculation was carried out for cobalt ions with $R = 1.692$ and $R_0 = 0.37$. ³⁷ ^b C.N., coordination number.							

Table 4. Bond Valence (v.u.) Analysis for Co₂AlBO₅^{*a*}

one-site disorder provides magnetic hardness. Such systems are assumed to allow a mechanism for "switching" states between magnetically hard and soft materials through the cation distribution.

The effect of the random distribution of Co and Al is quite obvious, and these inhomogeneities can act as barriers to mobile charge carriers. The obtained resistivity is about 2 orders of magnitude greater than the reported value for Co_3BO_5 .¹⁸ The introduction of Al³⁺ "cuts through" the superexchange $Co^{2+}-O-Co^{2+}$ network, which restricts the movement of charge carriers. The hopping mobility through the $Co^{2+}-O-Al^{3+}$ network becomes difficult. As a result, the hopping mobility decreases, and hence, the resistivity increases.

In addition, charge carrier localization is supposed to yield a noticeable contribution to the conductivity. The band structure calculations in the DFT+U framework showed that at low temperatures, Co_3BO_5 is an insulator with a band gap of 1.4 eV.¹⁷ The band gap for Co_2AlBO_5 is estimated to be $E_g = 2E_a = 1.14 \pm 0.01$ eV, which is very close to that for Co_3BO_5 , implying that the electronic structure near the Fermi level has common features.

With respect to the origin of the cationic disorder in the ludwigites, clear peculiarities are evident. The M2 and M4 positions are most structurally disordered (Table 3). This is consistent with the large amplitudes of the displacement parameters $U_{eq}(M2) = 0.00691(19)$ and $U_{eq}(M4) =$ 0.00656(15) Å² (Table S1). As above-mentioned, in Fe₃BO₅, the atomic instability of the Fe2 position leads to an isostructural phase transition with a doubling of the lattice parameter c_{i} accompanied by charge ordering.¹² In Co₃BO₅, the Debye–Waller coefficients σ^2 obtained using single-crystal X-ray diffraction data showed enhanced atomic disorder associated with the M4 site and the oxygen site connecting M2 and M4 at the spin-crossover temperatures.³⁴ Several works are only available on the temperature-dependent X-ray diffraction study of heterometallic ludwigites, which have shown that the crystal structure is stable with decreasing temperature and that symmetry remains (orthorhombic Pbam for $Co_2AlBO_5^{24}$ and monoclinic $P2_1/c$ for $Cu_2CrBO_5^{35}$). However, in Co₂AlBO₅, anomalous behavior of the lattice parameters is observed near the Neel temperature and 150 K. The first anomaly can be attributed to spin-lattice interactions, whereas the origin of the other one is unclear. It is important to note that in heterometallic ludwigites the effects of atomic instability, although suppressed by cationic disorder, are still present and can manifest themselves upon cooling due to the weakening of thermal vibrations of oxygen atoms.

Among the five symmetry inequivalent oxygen atoms, three, namely, O2, O3, and O5, belong to a BO_3 -triangle (Figure 1b), forming a rigid anionic framework, whereas O1 and O4 have relative freedom for displacement. The largest equivalent atomic displacement parameter is for O4 connecting the M2 and M4 sites: $U_{eq}(O4) = 0.0225(5) \text{ Å}^2$ (Table S2). The ellipsoid of the thermal vibrations of the O4 atom is elongated in the direction of the linkage with the equivalent oxygen atom, i.e., along the share edge and coinciding with the *c*-direction (Figure 1c). The atomic instability of the O4 probably results from its unique cationic environment: the coordination number of O4 is five (five metal atoms) rather than four, as is the case for O1 (four metal atoms) or for O2, O3, and O5 (three Me atoms and one B atom) (Table 4 and Figure 1c). The bonds to $2 \times M2$, M3, and M4 supply 1.843 valence units (v.u.) to O4 or 0.369 v.u. per bond only, which is much less than those for other anions (0.495–0.511 v.u.) and compatible with the long mean bond $\langle O4-Me \rangle = 2.061$ Å. The ability of O4 to shift leads to the lengthening/shortening of the corresponding Me-O4 bonds. As a result, the local symmetry of the coordination octahedra M2O₆ and M4O₆ changes, adapting to the requirements of the substitution ion. These sites are primarily filled by the substitutional ions, including the Jahn-Teller Cu²⁺ or Mn³⁺.^{20-24,28,36}

Finally, it is useful to discuss the issue of disorder control. Analogous to the spinel structure, in ludwigites, the cation distribution can be characterized by the so-called degree of inversion x, which is defined as the fraction of divalent metal ions at the octahedral M4 site

$$[Me_{2-x}^{2+}Me_{x}^{3+}]^{M1,M2,M3}(Me_{x}^{2+}Me_{1-x}^{3+})^{M4}BO_{5}$$

In this formula, the square brackets and parentheses denote the ions belonging to the octahedral layers (M1, M2, and M3 sites) or to the spacer between them (M4 site), respectively. The x = 0 corresponds to structurally ordered ludwigite, for instance, Co_3BO_5 with $[Co^{2+}O_6]_{\infty}$ octahedral layers and LS Co^{3+} ions located between them. An x = 1 yields inverse ludwigite with divalent ions at the M4 site, and the divalent and trivalent ions are distributed over the layer in equal proportions. The inversion degree of x = 2/3 corresponds to random ludwigite since divalent and trivalent ions are randomly distributed among both octahedral layers and M4 sites, and the number of divalent ions is double that of trivalent ions. The experimentally defined cation distribution has a rather wide range, yet never exceeds the random limit (Figure 7).

In ludwigites, the ionic radii relation between divalent and trivalent cations $r_i(Me^{2+})/r_iMe^{3+} \ge 1$ is always the case, suggesting that this parameter, although important, does not



Figure 7. Inversion degree *x* for the ludwigites. The red symbols show the experimental values of the *x*. The straight line is drawn by the eye. The numbering corresponds to the increase in the inversion degree: 1. $Mg_2FeBO_{5,}^{38}$ 2. $Mg_2InBO_{5,}^{36}$ 3. $Co_2FeBO_{5,}^{19}$ 4. $Ni_2VBO_{5,}^{39}$ 5. $Cu_2GaBO_{5,}^{40}$ 6. $Co_{2.38}Al_{0.62}BO_{5,}^{23}$ 7. $Cu_2FeBO_{5,}^{41}$ 8. $Ni_2AlBO_{5,}^{28}$ 9. $Cu_2AlBO_{5,}^{28}$ 10. $Co_2AlBO_{5,}^{28}$ 11. Co_2AlBO_{5} (p.w).

play a crucial role in cationic disorder. There is a sense that electronegativity is precisely the parameter that can influence the cationic distribution and be controlled in the synthesis and design of these compounds. The oxygen prefers to share its electrons with more electronegative cations, Ni²⁺, Cu²⁺, Co²⁺, Fe^{3+} , Ga^{3+} , and especially Sn^{4+} , Ge^{4+} , thus strengthening covalent bonding. Such cations by occupying the M4 site result in the effective holding back of the polymerization of the BO₃ groups, enriching the borate structure. This guess is confirmed by our DFT + U calculations of the electron structure of Co2.5Ge0.5BO5, where the Ge-O bonding was found to be more covalent than that of Co-O and commensurate with B-O one.³⁰ The less electronegative Al^{3+} or Sc^{3+} is assumed to be squeezed from this site. The M4 site occupation factor (S.O.F.) as a function of the cation's electronegativity is presented in Figure 8. The concentration of the $Me^{3+}(Me^{4+})$ cation increases as its electronegativity increases. This leads to a decrease in the degree of inversion and, hence, a decrease in the cation disorder. We assume that by combining different



Figure 8. M4 site occupation factor as a function of the cation's Pauling electronegativity in ludwigite structure. The full symbols denote the X-ray diffraction data, and the empty symbols show the predicted yttrium-containing ludwigite. The straight line is a linear approximation. 1. $Co_5SnB_2O_{10}$,⁴⁴ 2. $Mg_5SnB_2O_{10}$,⁴⁵ 3. $Co_{2.5}Ge_{0.5}BO_5$,³⁰ 4. Mg_2FeBO_5 ,³⁸ 5. Mg_2InBO_5 ,³⁶ 6. Co_2InBO_5 ,⁴⁶ 7. Ni_2AIBO_5 ,²⁸ 8. Co_2AIBO_5 (p.w.), 9. $Co_5TiB_2O_{10}$,⁴⁷ 10. $Co_{2.5}Sc_{0.5}BO_5$,⁴³ 11. Me_2YBO_5 .

electronegativity metals one can obtain ludwigites with different cationic distributions. Mg₂FeBO₅ and Ni₂ScBO₅ are proposed to be candidates for ordered and random ludwigites, respectively. There is strong experimental evidence from X-ray and Mössbauer spectroscopy measurements to support the smallest degree inversion in Mg₂FeBO₅, x = 0.13.^{38,42} To the best of our knowledge, an investigation of Ni₂ScBO₅ has not been reported; however, one might anticipate that such a study would be particularly useful for verifying whether the proposed model is indeed valid. We have grown the Co_{2.5}Sc_{0.5}BO₅ single crystals.⁴³ Although the full substitution was not achieved, the crystal structure refinement showed the statistical distribution of Co²⁺ and Sc³⁺ ions over inequivalent metal sites, supporting the above hypothesis. Reasoning further, the yttriumcontaining ludwigite, if it is obtained, can be considered a candidate for the inversion ludwigite.

Intuitively, one can expect that a more electronegative cation would cause a redistribution of the electron density at the M4 site, shifting it toward a more electronegative atom and changing the strength of the interatomic orbital overlap. This may cause a change in the hopping energy t, which describes hybridization between these orbitals, and in electrical conductivity in general. In addition to the covalent bonding effect, filling the M4 site with more electronegative cations favors a low-coordination structure with high barriers to the structure rearrangement. This can explain recent experiments on the annealing of Cu_2FeBO_5 in a reducing atmosphere,⁴⁸ which revealed a continuous collapse-recrystallization process without destroying the ludwigite structure. During annealing, Cu²⁺ ions at the M1, M2, and M3 sites are exfoliated, allowing a rearrangement of the structure of the same type, but with Fe^{2+} cations: $Cu_2FeBO_5 \rightarrow Fe_3BO_5$.

5. CONCLUSIONS

Co₂AlBO₅ single crystals were synthesized by using flux. The effects of cationic disorder on structural, magnetic, and electronic properties were studied using X-ray diffraction, dc magnetization, and electrical resistivity measurements. The Al^{3+} ions occupying the M1, M2, and M3 sites push the Co^{2+} ions into the M4 site, increasing the degree of inversion up to x \approx 0.5. The cationic disorder causes enhancement of the antiferromagnetic correlations, progressive compensation of the magnetic moments along the *b*-axis, and magnetic softness. The compound exhibits a high magnetic anisotropy. At T_1 = 41 K, the long-range magnetic order onsets, and at $T_2 = 20$ K, the hysteresis loop opens, implying that a noncompensated magnetic moment appears. The Al substitution results in an increase in the electrical resistivity compared with that of Co₃BO₅, revealing that cation disorder affects hopping mobility. The key to understanding cationic disorder in ludwigites is the crystal structure containing metal and oxygen positions with a large amplitude of displacement. One can conclude that these systems are somewhat predisposed to disorder and that this disorder might be tuned through the exploitation of the structural chemistry of this broad borate family.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.cgd.4c00582.

Photo of the Co_2AlBO_5 single crystal, fractional atomic coordinates and equivalent isotropic displacement parameters, anisotropic displacement parameters, main bond lengths, interionic distances Me–Me and average bond angles Me–O–Me, and X-ray microfluorescence mapping of some elements (PDF)

Accession Codes

CCDC 2348879 contains the supplementary crystallographic data for this paper. These data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif, by emailing data_request@ccdc.cam.ac.uk, or by contacting The Cambridge Crystallographic Data Centre, 12 Union Road, Cambridge CB2 1EZ, UK; fax: +44 1223 336033.

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